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District Heating of Buildings by Renewable Energy Using Thermochemical Heat Transmission

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Abstract: The decarbonisation of building heating in urban areas can be achieved by heat pumps connected to district heating networks. These could be 'third-generation' (85/75 °C), 'fourth-generation' (50/40 or 50/25 °C) or 'fifth-generation' (near ambient) water loops. Networks using thermochemical reactions should require smaller pipe diameters than water systems and be more economic. This work investigates thermochemical transmission systems based on liquid-gas absorption intended for application in urban district heating networks where the main heat source might be a MW scale heat pump. Previous studies of absorption for heat transmission have concentrated on long distance (e.g., 50 km) transmission of heat or cold utilizing waste heat from power stations or similar but these are not directly applicable to our application which has not been investigated before. Absorbentrefrigerant pairs are modelled using water, methanol and acetone as absorbates. Thermodynamic properties are obtained from the literature and modelling carried out using thermodynamic analysis very similar to that employed for absorption heat pumps or chillers. The pairs with the best performance (efficiency and power density) both for ambient loop (fifth-generation) and high temperature (fourth-generation) networks use water pairs. The next best pairs use methanol as a refrigerant. Methanol has the advantage of being usable at ambient temperatures below 0 °C. Of the water-based pairs, water-NaOH is good for ambient temperature loops, reducing pipe size by 75%. Specifically, in an ambient loop, heat losses are typically less than 5% and the heat transferred per volume of pumped fluid can be 30 times that of a pumped water network with 10 K temperature change. For high temperature networks the heat losses can reach 30% and the power density is 4 times that of water. The limitation with water-NaOH is the low evaporating temperature when ambient air is the heat source. Other water pairs perform better but use lithium compounds which are prohibitively expensive. For high temperature networks, a few water- and methanol-based pairs may be used, but their performance is lower and may be unattractive.

Keywords: thermochemical networks; absorption; heat pumping; heat district networks



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1. Introduction

It is commonly suggested that the decarbonisation of building heating in urban areas is best achieved by large, efficient, and adaptable heat pumps connected to district heating networks. Conventionally these would be 'third-generation' $(85/75\,^{\circ}\text{C})$, 'fourth-generation' $(50/40\,\text{or}\,50/25\,^{\circ}\text{C})$ or 'fifth-generation' (near ambient) water loops [1]. In urban environments the costs of retrofitting a district heating network are very high and the installation can be very disruptive. Both the cost and level of disruption increase rapidly with the pipe diameter used. The networks using thermochemical (TC) reactions should require far smaller pipe diameters than pumped water systems, and be far less costly to install and, correspondingly, more economical.

This paper seeks to evaluate possible sorption TC reactions that might be used in this way. This section surveys some of the previous work in this area, explains the TC system and components, and suggests suitable figures of merit to characterize and compare them. Section 2 presents the different absorption pairs that are considered, and Section 3 describes

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the mathematical approach to modelling the performance, presenting the equations used for all the components: desorber, absorber, condenser, pump, evaporator and solution heat exchangers. The results are firmly grounded in sorption thermodynamics and use robust measured data on material pairs from the literature. Section 4 presents the results for ambient, fifth-generation loops, (Section 4.1) and for higher temperature fourth-generation loops (Section 4.2). Within these sections different absorption pairs using a number of refrigerants (water, methanol and acetone) are compared and contrasted. Finally, Section 5 presents the discussion and conclusions. Appendices A and B contain the thermochemical data used, enabling replication or further exploration of our results. A methodical thermodynamic study based on a practical district heating application/requirement and comparing so many absorption pairs is a new contribution to the topic.

Previously, there have been studies using both open and closed thermochemical systems to transfer heat. Closed systems have included the possibility of using the decomposition/composition of methanol [2] or metal hydride reactions [3,4]. However, the temperatures in the methanol reaction are not applicable in district heating and the exotic metal alloys employed in hydride reactions are prohibitively expensive. Kang et al. [5] proposed a 'solution transportation absorption' (STA) similar to that analysed in this paper but intended for district cooling powered by waste heat from remote power stations. Both lithium bromide—water and ammonia—water absorption pairs were analysed. Wang [6] suggested the absorption of ammonia refrigerant into water absorbent as a means of transferring heat over long distances. However, in our application of district heating, safety considerations preclude the use of large quantities of pressurized ammonia solution.

Open systems utilize concentrated and dilute solutions of liquid desiccants such as LiBr in which water absorption (either for humidity control or the heating effect) occurs at the point of use. Geyer et al. [7,8] develops ideas for waste heat utilization and storage in addition to transport but the concept is particularly useful when integrated with drying or humidification needs as part of the demand. Our focus is purely on heat transportation within a district heating system and the performance of possible absorption pairs. A closed system using water, acetone or an alcohol as a low-pressure refrigerant that is absorbed or desorbed into a hydroxide, bromide or similar salt is proposed. The simplest such arrangement to transport heat would be as shown in Figure 1.

Heat for distribution, typically from a heat pump or industrial waste heat, is used to desorb water from the dilute solution. The water vapour is condensed at as low a temperature as possible to maximise the concentration change. The liquid water and concentrated solution can then be pumped to the delivery location. At the delivery point the liquid water can be evaporated by ambient temperature heat and be absorbed into the concentrated solution, releasing the heat of absorption to the load. The concentrated solution is then pumped back to the heat source side of the system. Because the heat of absorption is, in general, large compared to the sensible heat of the solutions above ambient, the basic system would be feasible, but not as efficient as it could be. Even with very high levels of pipe insulation the three liquid lines would lose significant amounts of sensible heat as they are pumped over long distances. This loss can be reduced by at least 80% by the use of solution heat exchangers (SHEs), as shown in Figure 2.

On the source side, the SHE preheats the incoming dilute ambient temperature solution (the worst case is that it is at ambient temperature) with the outgoing hot concentrated solution. Thus, the hot solution enters the network only a little above ambient, minimizing the sensible heat loss. On the delivery side the SHE performs a similar role, preheating the incoming concentrated solution with the hot exiting dilute solution. The other practical difference between the basic and proposed systems is that the pumped liquids would be at atmospheric pressure or a little higher and throttled down to absorption/desorption pressure at point of use. Pumping at a sub-atmospheric pressure would both be impractical and encourage air ingress that would reduce the system efficiency.

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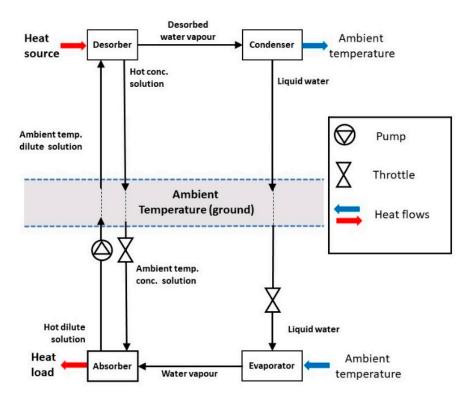


Figure 1. Basic heat transmission using absorption/desorption.

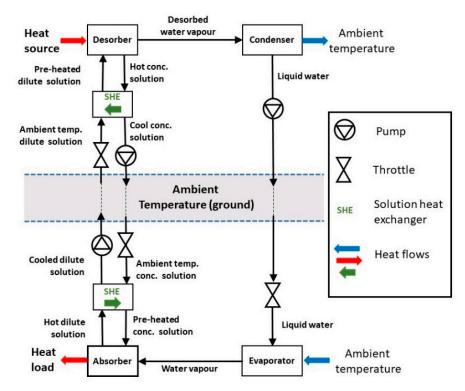


Figure 2. Proposed thermochemical heat transmission system.

In this paper, the possible use of a number of absorption pairs that might be suitable for district heating TC networks is investigated. Most use water as the refrigerant as in Figures 1 and 2 above, but a few use methanol or acetone. At low ambient temperatures (below about 5 $^{\circ}$ C) it becomes impracticable to boil water in the evaporator since the pressure is very low and the water may freeze. It is possible to boil water out of an anti-

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freeze solution or a very dilute solution of the sorbate, but it would be better to avoid the complexity. If a ground source can be used, the evaporating temperature can be kept high enough to avoid problems but using the air as an ambient heat source needs another approach. One possibility is to use methanol or acetone as the refrigerant rather than water. They both can be used down to $-10\,^{\circ}\text{C}$ or less but they have lower latent and absorption heats than water. This results in less energy being transmitted per unit volume pumped around the network. One other possibility that would allow the use of water would be to boost the temperature level of the ambient by 5 or 10 K using a vapour compression heat pump. At such a small temperature lift, it is feasible to do this with a COP > 9 and so it may be a technically viable approach. However, in this study a number of water, acetone and methanol absorption pairs are simply characterised.

There are two characteristics that define the performance of a pair under set conditions of ambient temperature, desorption temperature and absorption temperature. These are the efficiency, simply the heat delivered divided by the heat from the source, and a measure of the heat transferred per unit volume of fluid that must be pumped through the network. Since the objective is to achieve lower diameter and hence lower pipework installation costs than with a conventional water network, a physically meaningful comparison has been chosen. The energy transferred by the volume flowing in the three pipe TC system is calculated and then the temperature differential that would be necessary to transfer the same energy using the sensible heat in a conventional two pipe (flow and return) water system is obtained. This is referred to as $\Delta T H_2O$. Thus, if the calculated value were only 10 K the total flow would be the same as a conventional water system with a 10 K difference between flow and return (as is typical). If however $\Delta T H_2O$ were 100 K, it implies that the total volume being pumped was roughly 1/10 of that needed by a conventional district heating system. Should a TC system be compared with a water system having a higher flow–return temperature difference of say 20 K then $\Delta T H_2O$ would have to exceed 20 K for there to be any advantage

In the methodology section below, the thermodynamic calculations are described. They require full mixture property data obtained from sources in the literature. The results plot ΔT H₂O v. the efficiency for combinations of ambient temperature (strictly the evaporating and condensing temperature), absorption temperature (heat delivery) and desorption temperature (heat supply). The results are used to suggest which pairs may be of interest and worthy of further investigation in future, more detailed, studies.

2. Materials

The absorbate is a refrigerant that must be capable of boiling at ambient temperature and ideally should have a high latent heat to ensure high energy transport per unit mass. Water is ideal apart from its low vapour pressure. The lowest practicable evaporating temperature is about 5 $^{\circ}$ C. Alcohols and acetone do not have such high latent heat but can be boiled at lower (sub-zero) temperatures which is advantageous in certain climatic conditions.

Different groups of substances such as salts, alkalis, acids, organic compounds and ionic liquids can be used as absorbents. In addition to their good thermodynamic properties when forming a solution, other criteria such as availability, price, recyclability, environmental compatibility, toxicity and chemical stability should be considered in their selection.

The absorbent pairs that have been modelled in this paper are:

- Water-based pairs: LiBr, LiCl, LiI, LiBr + LiI, LiBr + LiNO₃, LiCl + LiNO₃, LiBr + ZnCl₂ + CaBr₂, NaOH, Ca(NO₃)₂
- Methanol-based pairs: ZnBr₂, LiBr, LiI + ZnBr₂, LiBr + ZnBr₂, LiBr + ZnCl₂
- Acetone-based pair: ZnBr₂

A full list of the thermophysical properties of the refrigerants and of the correspondent absorbent pairs extracted from the literature can be found in Appendices A and B, respectively.

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3. Methods

This section describes the approach developed to model and simulate the absorption cycle described in Figure 3.

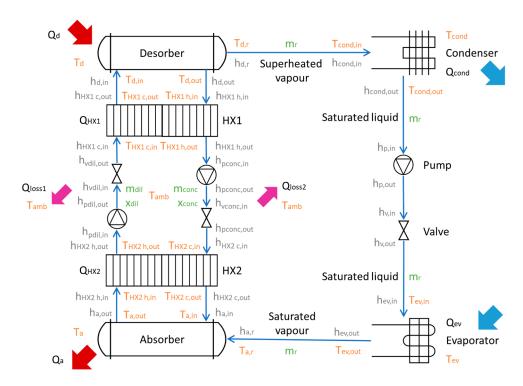


Figure 3. Thermochemical network system schematic.

The salt concentration in the solution that is circulated between the desorber and absorber and vice versa is represented by the symbol x and it is given as the mass percentage of the solution. It is defined as:

$$x = \frac{m_{salt}}{m_{solution}} \cdot 100 \tag{1}$$

where:

$$m_{solution} = m_{salt} + m_{abs} (2)$$

 m_{salt} being the mass of salt and m_{abs} the mass of absorbent.

The mass of the concentrated solution (m_{conc} , solution flowing between the desorber and the absorber) is equal to the sum of the mass of the salt (m_{salt}) and the mass of the absorbent (m_{abs}) (refrigerant that has not been desorbed in the desorbed and that gets pumped to and from the desorber/absorber).

$$m_{conc} = m_{salt} + m_{abs} (3)$$

The mass of the dilute solution (m_{dil} , solution flowing between the absorber and desorber) is equal to the sum of the mass of the concentrated solution (m_{conc}) and the mass of the desorbed refrigerant (m_r , refrigerant flowing through the condenser and evaporator).

$$m_{dil} = m_{conc} + m_r = m_{salt} + m_{abs} + m_r \tag{4}$$

In the simulation, attention must be paid to the maximum and minimum concentration limits of the solution modelled as reported in the Appendices A and B. Higher salt% in the solution can result in reaching the crystallization limit and could cause blockages in the system.

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The concentrations of the dilute and concentrated solutions are defined as:

$$x_{conc} = \frac{m_{salt}}{m_{salt} + m_{abs}} \cdot 100 \tag{5}$$

$$x_{dil} = \frac{m_{salt}}{m_{salt} + m_{abs} + m_r} \cdot 100 \tag{6}$$

The mass of refrigerant flowing through the condenser and evaporator is the difference between the mass of the dilute (x_{dil}) and concentrated (x_{conc}) solutions. For simplicity the calculations are all based on a value of $1 \, \text{kg/s}$.

$$m_r = m_{dil} - m_{conc} = 1 \,\mathrm{kg/s} \tag{7}$$

The concentration of the concentrated solution (x_{conc}) is set by the temperature of the desorber (T_d) and by the temperature of the condenser (T_{cond}) . On the other hand, the concentration of the dilute solution (x_{dil}) is set by the temperature of the absorber (T_a) and by the temperature of the evaporator (T_{ev}) . Both concentrations can be calculated with the Saturated Pressure equations corresponding to each salt/refrigerant pair included in Appendices A and B.

The masses of salt and absorbent in the solutions can be calculated from the dilute and concentrated concentrations with the following equations:

$$m_{salt} = -\frac{m_r}{\frac{100}{x_{conc}} - \frac{100}{x_{dil}}} \tag{8}$$

$$m_{abs} = \frac{m_r}{\frac{100}{x_{conc}} - \frac{100}{x_{dil}}} - \frac{100 \cdot m_r}{x_{conc} \cdot \left(\frac{100}{x_{conc}} - \frac{100}{x_{dil}}\right)}$$
(9)

3.1. Desorber

The heat driving the desorption (Q_d) is delivered to the desorber and solution at T_d . It is assumed that the temperature of the desorbed refrigerant $(T_{d,r}$, flowing towards the condenser) and the temperature of the concentrated solution $(T_{d,out}$, flowing towards the absorber) are both equal to the desorbing temperature (T_d) .

$$T_{d,r} = T_{d,out} = T_d \tag{10}$$

In addition, assuming there are no losses between desorber and condenser their pressures are equal:

$$p_d = p_{cond} \tag{11}$$

The refrigerant leaving the desorber is assumed to be in a superheated state since it will be at the desorber temperature but at a pressure lower than the saturation pressure for that temperature, which is the saturation pressure of the condenser at ambient temperature. Its enthalpy can be calculated by the corresponding equation for each refrigerant included in the Appendices A and B.

The energy balance of the desorber is calculated using the following equation:

$$Q_d = m_r h_{d,r} + m_{conc} h_{d,out} - m_{dil} h_{d,in}$$
(12)

where Q_d is the heat input to the desorber, m_{conc} is the mass of the concentrated solution, m_{dil} is the mass of the dilute solution, m_r is the mass of the refrigerant leaving the desorber, $h_{d,in}$ is the enthalpy of the dilute solution as it enters the desorber, $h_{d,out}$ is the enthalpy of the concentrated solution as it leaves the desorber and $h_{d,r}$ is the enthalpy of the superheated refrigerant as it leaves the desorber.

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3.2. Absorber

The heat output of the absorbent (Q_a) is delivered in the absorber and to the solution at T_a . It is assumed that the temperature of the dilute solution $(T_{a,out}$, flowing towards the desorber) is equal to the absorbing temperature (T_a) .

$$T_{a,out} = T_a \tag{13}$$

In addition, assuming there are no losses between absorber and evaporator their pressures are equal:

$$p_a = p_{ev} \tag{14}$$

In addition, it is assumed that there are no heat losses or gains to the refrigerant flowing from the evaporator to the absorber, therefore the enthalpy of the refrigerant entering the absorber is:

$$h_{a,r} = h_{ev,out} \tag{15}$$

The energy balance of the absorber is calculated using the following equation:

$$Q_a = m_r h_{a,r} + m_{conc} h_{a,in} - m_{dil} h_{a,out}$$
(16)

where Q_a is the energy released in the absorber, m_{dil} is the mass of the dilute solution, m_{dil} is the mass of the concentrated solution, m_r is the mass of the refrigerant entering the absorber, $h_{a,in}$ is the enthalpy of the concentrated solution entering the absorber, $h_{a,out}$ is the enthalpy of the dilute solution leaving the absorber and $h_{a,r}$ is the enthalpy of the saturated vapour refrigerant entering the absorber.

3.3. Condenser

In the system, both the condenser and the evaporator are assumed to be air-cooled and therefore dependent on both ambient conditions and on the effectiveness of the heat exchangers used. For the purpose of this simulation study, it is assumed that perfect heat exchangers are used between the ambient air and the condenser/evaporator resulting in their temperatures being equal. If required, a particular temperature difference can be assumed when interpreting the results.

$$T_{cond} = T_{ev} = T_{amb} \tag{17}$$

Assuming there are no heat losses between the desorber and condenser, the hot flow input temperature $(T_{cond,in})$ corresponds to the refrigerant leaving the desorber $(T_{d,r})$ at the desorbing temperature (T_d) .

$$T_{cond.in} = T_{d.r} = T_d \tag{18}$$

The enthalpy of the refrigerant entering the condenser is:

$$h_{cond,in} = h_{d,r} (19)$$

Once the refrigerant condenses, it will leave the condenser at ambient temperature.

$$T_{cond.out} = T_{amb} (20)$$

The refrigerant leaves the condenser as a saturated liquid and its enthalpy can be calculated by the corresponding equation for each refrigerant included in Appendices A and B. The heat released by the condenser (Q_{cond}) is found using the following energy balance:

$$Q_{cond} = m_r \cdot (h_{cond.in} - h_{cond.out}) \tag{21}$$

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where m_r is the mass of the refrigerant flowing through the evaporator, $h_{cond,in}$ is the enthalpy of the refrigerant entering the condenser at T_d and in a superheated state and $h_{cond,out}$ is the enthalpy of the refrigerant leaving the condenser in a saturated liquid state. These enthalpies can be calculated by the corresponding equation for each refrigerant included in Appendices A and B.

3.4. Refrigerant and Refrigerant Pump

The refrigerant is assumed to be in a saturated liquid state when leaving the condenser and it is pumped to a higher than atmospheric pressure (sub-cooled liquid) in order to go through the pipework without air leaking in and also to allow for frictional pressure drop. Before entering the evaporator, a throttle is used to reduce the pressure and control the flow rate.

The pumping work is assumed to be very small and pumping is considered an isenthalpic process, as is that in the throttle. Thus, the enthalpy of the refrigerant when entering the evaporator, when leaving the throttle, when entering the throttle, when leaving the pump, when entering the pump and when leaving the condenser are all assumed to be equal:

$$h_{cond,out} = h_{v,in} = h_{v,out} = h_{v,in} = h_{v,out} = h_{ev,in}$$
 (22)

3.5. Evaporator

The heat absorbed by the evaporator (Q_{ev}) is found using the following energy balance:

$$Q_{ev} = m_r \cdot (h_{ev,out} - h_{ev,in}) \tag{23}$$

where m_r is the mass of the refrigerant flowing through the evaporator, $h_{ev,in}$ is the enthalpy of the refrigerant entering the evaporator at T_{ev} and in a saturated liquid state and $h_{ev,out}$ is the enthalpy of the refrigerant leaving the evaporator in a dry saturated vapour state. These enthalpies can be calculated by the corresponding equation for each refrigerant included in Appendices A and B.

3.6. Solution Heat Exchangers-HX1 & HX2 and Solution Pumps

The dilute solution stream prior to entering the desorber is preheated from ambient temperature by the concentrated solution stream leaving the desorber in HX1. The effectiveness of HX1 can be calculated with the following equations and in our case it is assumed to be 80%.

$$\epsilon_{HX1} = \frac{c_{p_{conc}} \cdot m_{conc} \cdot (T_{HX1 \ h,in} - T_{HX1 \ h,out})}{c_{p_{min,1}} \cdot (T_{HX1 \ h,in} - T_{HX1 \ c,in})}$$
(24)

$$\epsilon_{HX1} = \frac{c_{p_{dil}} \cdot m_{dil} \cdot (T_{HX1 \ c,out} - T_{HX1 \ c,in})}{c_{p_{min,1}} \cdot (T_{HX1 \ h,in} - T_{HX1 \ c,in})}$$
(25)

where $c_{p_{conc}}$ is the specific heat of the concentrated solution, $c_{p_{conc}}$ is the specific heat of the dilute solution, $T_{HX1\ h,in}$ is the temperature of the concentrated solution entering HX1 from the desorber, $T_{HX1\ h,out}$ is the temperature of the concentrated solution leaving HX1 to HX2, $T_{HX1\ c,in}$ is the temperature of the dilute solution entering HX1 from HX2, $T_{HX1\ c,out}$ is the temperature of the dilute solution leaving HX1 to the desorber and $c_{p_{min,1}}$ denotes the minimum value of specific heat times mass flow of each stream that exchanges heat in HX1, it can be calculated with the following equation:

$$c_{p_{min,1}} = min\left(c_{p_{dil}}(T_{HX1\ c,in}, x_{dil}) \cdot m_{dil}, c_{p_{conc}}(T_{HX1\ h,in}, x_{conc}) \cdot m_{conc}\right)$$
(26)

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The concentrated solution prior to entering the absorber is preheated from ambient temperature by the dilute solution leaving the desorber in HX2. The effectiveness of HX2 can be calculated with the following equations and in this case, it is assumed to be 80%.

$$\epsilon_{HX2} = \frac{c_{p_{conc}} \cdot (T_{HX2\ c,out} - T_{HX2\ c,in})}{c_{p_{min\ 2}} \cdot (T_{HX2\ h,in} - T_{HX2\ c,in})} \tag{27}$$

$$\epsilon_{HX2} = \frac{c_{p_{dil}} \cdot (T_{HX2 \ h,in} - T_{HX2 \ h,out})}{c_{p_{min \ 2}} \cdot (T_{HX2 \ h,in} - T_{HX2 \ c,in})}$$
(28)

where $c_{p_{conc}}$ is the specific heat of the concentrated solution, $c_{p_{dil}}$ is the specific heat of the dilute solution, $T_{HX2\ h,in}$ is the temperature of the dilute solution entering HX2 from the absorber, $T_{HX2\ h,out}$ is the temperature of the dilute solution leaving HX2 to the network, $T_{HX2\ c,in}$ is the temperature of the concentrated solution entering HX2 from the network, $T_{HX2\ c,out}$ is the temperature of the concentrated solution leaving HX2 to the absorber and $c_{p_{min,2}}$ denotes the minimum value of specific heat times mass flow of each streams that exchange heat in HX2, it can be calculated with the following equation:

$$c_{p_{min,2}} = min\left(c_{p_{dil}}(T_{\text{HX2 }h,in}, x_{dil}) \cdot m_{dil}, c_{p_{conc}}(T_{\text{HX2 }c,in}, x_{conc}) \cdot m_{conc}\right)$$
(29)

It is assumed that there are no heat gains or losses in the pipes between the desorber and HX1 and between the absorber and HX2 since they are physically close and the pipes are short and well-insulated, therefore the following temperatures are defined as:

- The temperature of the dilute solution entering the desorber is equal to the temperature of the solution leaving HX1: $T_{d,in} = T_{HX1}$ $_{c,out}$
- The temperature of the concentrated solution leaving the desorber is equal to the temperature of the solution entering HX1: $T_{d,out} = T_{HX1 \ h,in}$
- The temperature of the dilute solution entering HX1 is equal to ambient temperature: $T_{HX1\ c,in} = T_{amb}$
- The temperature of the concentrated solution entering HX2 is equal to ambient temperature: $T_{HX2\ c,in} = T_{amb}$
- The temperature of the concentrated solution entering the absorber is equal to the temperature of the solution leaving HX2: $T_{a,in} = T_{HX2 \ c,out}$
- The temperature of the dilute solution leaving the absorber is equal to the temperature of the solution entering HX2: $T_{a,out} = T_{HX2 h,in}$

Therefore, the temperature of the concentrated solution leaving HX1 can be calculated as a function of the ambient temperature (T_{amb}), temperature of the concentrated solution leaving the desorber ($T_{d,out}$) and the heat exchanger effectiveness:

$$T_{HX1\ h,out} = T_{HX1\ h,in} - \frac{\epsilon_{HX1} \cdot c_{p_{min,1}} \cdot (T_{HX1\ h,in} - T_{HX1\ c,in})}{c_{p_{conc}} \cdot m_{conc}}$$
(30)

The heat being exchanged in HX1 (Q_{HX1}) is calculated using the following equation:

$$Q_{HX1} = c_{p_{conc}} \cdot m_{conc} \cdot (T_{HX1 \ h,in} - T_{HX1 \ h,out})$$
(31)

The temperature of the dilute solution leaving HX2 can be calculated as a function of the ambient temperature (T_{amb}) , temperature of the dilute solution leaving the absorber $(T_{a,out})$ and the heat exchanger effectiveness:

$$T_{HX2\ h,out} = T_{HX2\ h,in} - \frac{\epsilon_{HX2} \cdot c_{p_{min,2}} \cdot (T_{HX2\ h,in} - T_{HX2\ c,in})}{c_{p_{dil}} \cdot m_{dil}}$$
(32)

The heat being exchanged in HX2 (Q_{HX2}) is calculated using the following equation:

$$Q_{HX2} = c_{p,ij} \cdot m_{dil} \cdot (T_{HX2\ h.in} - T_{HX2\ h.out})$$

$$\tag{33}$$

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The solution, when travelling between the solution heat exchangers, losses all its remaining heat reaching ambient temperature. The heat losses of the dilute stream (Q_{loss1}) and of the concentrated stream (Q_{loss2}) are quantified with the following equations:

$$Q_{loss1} = c_{p_{dil}} \cdot m_{dil} \cdot (T_{HX2\ h.out} - T_{amb}) \tag{34}$$

$$Q_{loss2} = c_{p_{conc}} \cdot m_{conc} \cdot (T_{HX1\ h,out} - T_{amb})$$
(35)

3.7. System Performance

In order to assess the performance of the system, there are two main defining characteristics to evaluate. The first one is its efficiency, defined as the heat delivered in the absorber (Q_a) divided by the heat obtained in the desorber (Q_d) .

$$\varepsilon_{system} = Q_a/Q_d \tag{36}$$

The second one is the measure of the heat transferred per unit volume of fluid that must be circulated throughout the network. This is referred to as ΔT_{H_2O} , being the equivalent temperature differential in a sensible water loop that would transfer the same heat using the same pumped volume. It can be calculated with the following equation:

$$\Delta T_{H_2O} = \frac{Q_a}{1000 \cdot \frac{m_{dil}}{\rho_{dil}} \cdot c_{p,H_2O}} \tag{37}$$

4. Results

In this section, the results obtained in the simulations of the thermochemical network with different absorption pairs are presented. In the diagrams below, the performance of each pair at different temperature conditions is presented as a heat ratio efficiency (Q_a/Q_d) vs. a comparative measure of the energy density, the equivalent temperature differential in a sensible water loop that would transfer the same heat using the same pumped volume (ΔT_{H_2O}) .

4.1. Ambient Temperature (Fifth-Generation) Network

The results presented in this section examine the applicability of sorption pairs to the ambient loop network concept. In an ambient temperature loop the primary network is at roughly ambient temperature (between 5 and 14 °C) and the secondary network delivers heat to the building load at temperatures between 45 and 55 °C. A heat pumping technology is used to achieve this, upgrading heat from the ambient temperature loop to the secondary network.

The refrigerant is desorbed in the desorber at temperatures between 13 and 15 $^{\circ}$ C and the heat delivered to the primary network is at temperatures between 8 and 10 $^{\circ}$ C. Two different ambient temperatures were simulated, 5 $^{\circ}$ C for the case of the water, acetone and methanol and 0 $^{\circ}$ C only for the case of the acetone and methanol (since water cannot operate at such low temperature without freezing).

The whole range of absorbent pairs were simulated, and their results are shown in Figure 4, offering a general overview of how the water, methanol and acetone pairs modelled in this paper compare.

As can be observed in Figure 4, the performance of the acetone pair is lower than either water or methanol pairs and so its results are not be presented in any further detail below.

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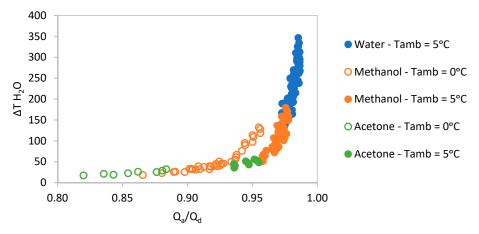


Figure 4. Water, methanol and acetone pairs performance for $T_{amb} = 5$ °C, $T_a = 8,9,10$ °C and $T_d = 13,14,15$ °C.

4.1.1. Water-Based Pairs

Figure 5 contains the performance of feasible water-based pairs suitable for an ambient temperature loop network. The different points correspond to a range of desorbing and absorbing temperatures ($T_a = 8$, 9, 10 °C and $T_d = 13$, 14, 15 °C) but keeping the ambient temperature to 5 °C.

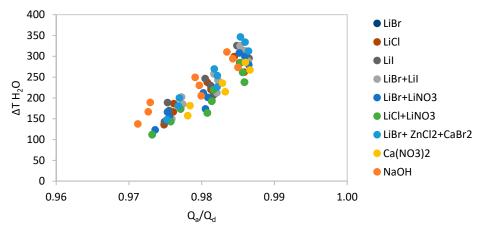


Figure 5. Water-based pairs performance for $T_{amb} = 5$ °C, $T_a = 8$, 9, 10 °C and $T_d = 13$, 14, 15 °C.

As can be observed, all the modelled pairs perform similarly and it can be concluded that on a simple thermal performance criterion there is little to choose between the pairs at these conditions.

Nevertheless, sodium hydroxide (NaOH) has been chosen to be looked at in more detail since it performs relatively well and is a low cost material (much lower cost compared to salts that contain lithium). The performance points for $T_{amb}=3$, 5, 7, 9 °C, $T_a=8$, 10, 12 °C and $T_d=13$, 14, 15 °C were obtained and plotted in Figure 6a. As can be observed, all the points present a very good Heat Ratio (Q_a/Q_d) between 90 and 99%. On the other hand, the equivalent ΔT_{H_2O} varies significantly between 40 and 465 °C.

Figure 6b–d disaggregate the combined data of Figure 6a to identify trends and understand the network performance.

Looking at Figure 6b–d trends can be observed but there is no 'best result' for an optimum T_a and T_d at a given T_{amb} .

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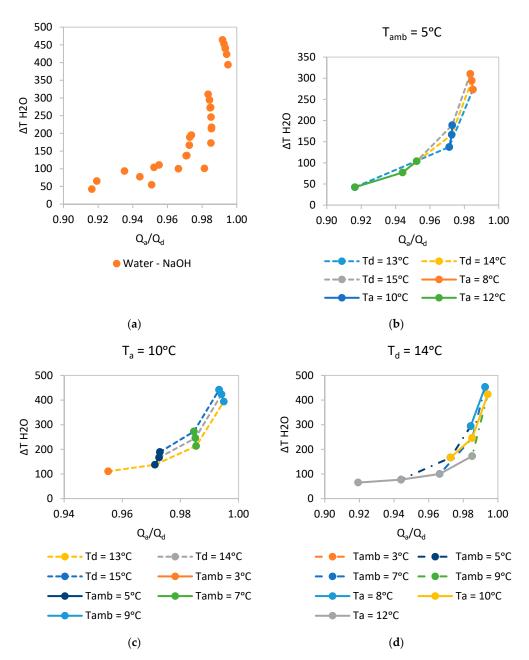


Figure 6. (a) Water–NaOH pair performance data points for $T_{amb} = 3$, 5, 7, 9 °C, $T_a = 8$, 10, 12 °C and $T_d = 13$, 14, 15 °C, (b) Data points for $T_{amb} = 5$ °C linked by T_a and T_d . (c) Water-NaOH pair performance data points for $T_d = 14$ °C linked by T_{amb} and T_a , (d) Data points for $T_a = 10$ °C linked by T_{amb} and T_d .

When T_{amb} is fixed, lower T_a provide the best performance also enhanced with a choice of T_d as close to T_a as possible. A drawback of choosing a low T_a is that the heat pumping technology of choice will have to upgrade heat to the user from a lower temperature level achieving a lower COP.

When T_a is fixed, higher T_{amb} provide the best performance, as expected, and as mentioned above, a choice of T_d as close to T_a as possible also improves the performance.

4.1.2. Methanol-Based Pairs

Figure 7 contains the performance of feasible methanol-based pairs suitable for an ambient temperature loop network. The different points correspond to a set range of desorbing and absorbing temperatures and they are divided into two groups: the hollow

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points correspond to an ambient temperature of 0 $^{\circ}$ C and the solid points correspond to an ambient temperature of 5 $^{\circ}$ C.

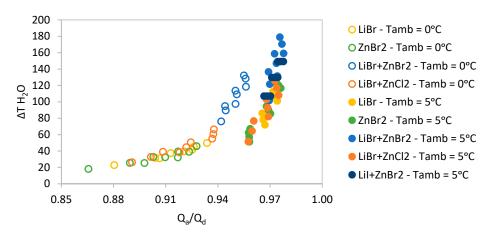


Figure 7. Methanol-based pairs performance for $T_{amb}=0$, 5 °C, $T_a=8$, 9, 10 °C and $T_d=13$, 14, 15 °C.

Although methanol-based pairs can be used at an ambient temperature of 0 °C, their ΔT and heat ratio drop quite significantly. At higher ambient temperatures ($T_{amb} = 5$ °C) their performance is much lower compared to water-based pairs, as observed in Figure 7.

The best performing pair corresponds to CH₃OH-LiBr + ZnBr₂, as seen in Figure 7. Both $T_{amb} = 0.5$ °C perform with heat ratios between 0.94 and 0.98 and ΔT between 80 and 180 °C (depending on T_a and T_d conditions).

4.1.3. Example Calculations for Ambient Loop Applications

In the following section the potential reduction of the network's pipe size by using some of the modelled TC pairs has been calculated.

The example used is for a building heat demand of 3 MW that is being delivered by a conventional water heat district network (the approximated ΔT_{H_2O} would be 10 °C). Assuming the specific heat of the water is constant and corresponds to 4.2 kJ/kgK, it is possible to calculate the mass flow of water needed to deliver that heat:

$$\dot{Q} = c_p \cdot \Delta T \cdot \dot{m}$$

$$\dot{m} = O/c_p \cdot \Delta T = 3 \cdot 10^3 / 4.2 \cdot 10 = 71.43 \text{ kg/s}$$
(38)

This means the network needs two pipes (flow and return) that carry 71.5 kg/s \approx 71.5 l/s of water, \approx 143 l/s in total.

Water-NaOH for Ambient Loop Applications

For a Water-Sodium Hydroxide pair working in an ambient loop temperature network desorbing at 14 $^{\circ}$ C, absorbing at 10 $^{\circ}$ C, and with an ambient temperature of 5 $^{\circ}$ C, the heating power delivered in the absorber would be 2494 kW with a 97% efficiency.

In order to deliver that heating power, the TC network would need to pump $4.28\,l/s$ of dilute solution, $3.15\,l/s$ of concentrated solution and $1.20\,l/s$ of water, being the total sum of mass flows $\approx 8.6\,l/s$. This corresponds to approximately 6% of the original mass flow, using a pipe diameter approximately 75% smaller.

Methanol-LiBr + ZnBr₂ for Ambient Loop Application

For the same heat demand but instead using methanol as the refrigerant, the improvements would be lower but as mentioned earlier, methanol can work at lower ambient temperatures.

For a methanol–lithium bromide+zinc bromide pair working in the same ambient loop temperature network and with an ambient temperature of 5 $^{\circ}$ C, the heating power

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delivered in the absorber would be 1190 kW with a 97% efficiency. The mass flow pumped in the TC network would corresponds to approximately 8.5% of the originally mass flow, and it would use a pipe diameter approximately 71% smaller.

In the case of the same pair working with an ambient temperature of 0 $^{\circ}$ C, the mass flow pumped in the TC network would corresponds to approximately 11.2% of the originally mass flow, and it would use a pipe diameter approximately 66% smaller.

4.2. Network for High Temperature Loop

Similar to the ambient loop network, the high temperature network works between two higher desorption and absorption temperature levels (absorbing between 45 and 55 °C and desorbing between 2 and 10 °C above T_a). By doing this, the TC network can be used to produce useful heating in the delivery point (absorber) using a low temperature heat input to the desorber and having the advantage of not requiring insulated pipes.

The whole range of suitable absorbent pairs for these conditions were simulated and the results are shown in Figure 8.

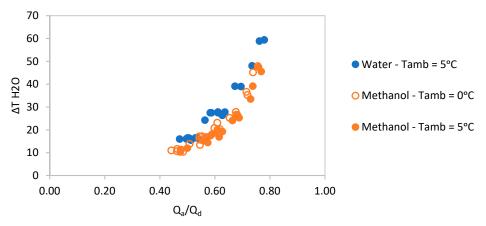


Figure 8. Performance of water and methanol pairs performance for $T_{amb} = 0$, 5 °C, $T_a = 45$, 50, 55 °C and $T_d = T_a + 2$, 4, 6, 8, 10 °C.

Due to sary sitallization, not all the pairs presented previously are suitable for these temperature conditions and their performance is quite low. The two best performing water-based solutions are Lithium Bromide and Lithium Bromide + Lithium Nitrate as it can be observed in Figure 9a. In the case of methanol, the best performing solution is Lithium Bromide as it can be observed in Figure 9b.

4.2.1. Example Calculations for High Temperature Loop Applications

In the following section, the potential reduction of the network's pipe size that can be potentially achieved by using some of the modelled TC pairs for a high temperature loop network has been calculated for the same example building heat demand presented above. As previously mentioned, the conventional network needs two pipes (flow and return) that carry 71.5 kg/s \approx 71.5 l/s of water, \approx 143 l/s in total.

Water–LiBr + ZnCl₂ + CaBr₂ for High Temperature Loop Applications

For a water–lithium bromide + zinc chloride + calcium bromide pair working in a high temperature loop network desorbing at 55 $^{\circ}$ C, absorbing at 50 $^{\circ}$ C, and with an ambient temperature of 5 $^{\circ}$ C, the heating power delivered in the absorber would be 1854 kW with a 50% efficiency.

In order to deliver that heating power, the TC network would need to pump $26.48\,l/s$ of dilute solution, $25.49\,l/s$ of concentrated solution and $1.62\,l/s$ of water being the total sum of mass flows $\approx 53.6\,l/s$. This corresponds to approximately 38% of the originally mass flow, using a pipe diameter approximately 38% smaller.

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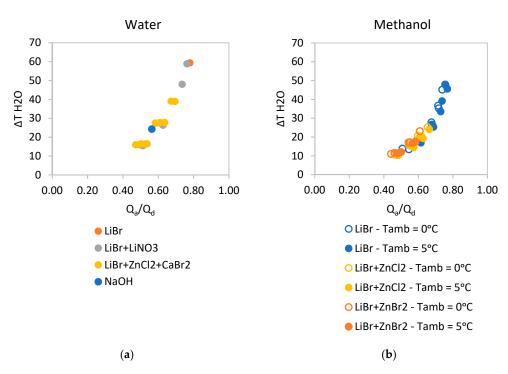


Figure 9. (a) Contains the performance of feasible water-based pairs at an ambient temperature of 5 °C and (b) Feasible methanol-based pairs. The different points correspond to a range of desorbing and absorbing temperatures ($T_a = 45$, 50, 55 °C and $T_d = T_a + 2$, 4, 6, 8, 10 °C). In the case of water, the ambient temperature is 5 °C and in the case of the methanol two ambient temperatures were simulated, 5 and 0 °C.

Methanol–LiBr for High Temperature Loop Applications

For the same heat demand but instead using methanol as the refrigerant, the performance is better than the water-based pair. It also has the added advantage of being able to work at lower ambient temperatures.

For a methanol–lithium bromide pair working in the same high temperature loop network and with an ambient temperature of 5 $^{\circ}$ C, the heating power delivered in the absorber would be 1239 kW with a 65% efficiency. The mass flow pumped in the TC network would corresponds to approximately 20% of the originally mass flow, and it would use a pipe diameter approximately 53% smaller.

In the case of the same pair working with an ambient temperature of 0 °C, the mass flow pumped in the TC network would corresponds to approximately 19% of the originally mass flow, and it would use a pipe diameter approximately 56% smaller.

5. Discussion

This paper seeks to evaluate possible sorption TC reactions that might be used in a district heating network. A closed system using water, alcohol or acetone as a low-pressure refrigerant that is absorbed or desorbed into a hydroxide, bromide or similar salt is proposed. The main difference with other published papers on this subject is the detailed presentation of the thermodynamic model of the thermochemical network and the range of absorption pairs considered.

Considering the modelled refrigerants, water is not suitable for ambient temperatures of 0 $^{\circ}$ C or below (freezing point). Methanol and acetone pair performance is not as good as water but they can be used below 0 $^{\circ}$ C ambient temperature. The Acetone-Zinc Bromide pair is not recommended.

Detailed simulation results for both ambient temperature loops and high temperature loops are presented along with example calculations which compare their capacity with conventional networks.

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From the presented graphs it is possible to observe that the pairs with the best performance (heat ratio and ΔT_{H_2O}) both for ambient loop and high temperature networks are water pairs, due to water's exceptionally high latent heat of vaporization. Heat ratios of 98% and ΔT_{H_2O} of 200 °C are easily achievable for ambient temperature loops and heat ratios of 70% and ΔT_{H_2O} of 40 °C for high temperature loops both working at ambient temperatures of 5 °C.

The next best performing pairs use methanol, which has the benefit that methanol can be used as a working fluid with evaporating temperatures below 0 °C. In the case of an ambient temperature of 5 °C, heat ratios of 97% and ΔT_{H_2O} of 150 °C are obtained for ambient temperature loops and heat ratios of 70% and ΔT_{H_2O} of 35 °C for high temperature loops. For an ambient temperature of 0 °C the performance drops significantly in ambient temperature loops and slightly in high temperature loops. Heat ratios of 94% and ΔT_{H_2O} of 60 °C are obtained for ambient temperature loops and heat ratios of 70% and ΔT_{H_2O} of 30 °C for high temperature loops.

Finally, the least well performing refrigerant is acetone. For ambient temperature loops at 5 °C heat ratios of 95% and ΔT_{H_2O} of 45 °C are obtained and for ambient temperature loops at 0 °C the heat ratio achieved is 86% and ΔT_{H_2O} of 25 °C.

Of the water-based pairs, water–NaOH has been chosen for further analysis and future experimental testing at the authors' institution. It is attractive for ambient temperature loop applications, dramatically reducing the pipe size of the network by 75% (corresponds to approximately 6% of the original mass flow) and its cost makes it economically competitive. The only identified limitation is the evaporating temperature of the network if the ambient air is used as the heat source (ambient temperature should be above 0 $^{\circ}$ C). Ways to overcome this issue might include using a ground or aquifer heat source or the possible the use of water alcohol mixtures. Other water pairs perform very well but they are based on lithium compounds, which due to their price, make the cost of the network prohibitive.

In the case of high temperature networks, a few water and methanol-based solutions perform similarly, but their heat ratio and ΔT_{H_2O} are substantially lower, not making them economically attractive enough to implement in a network.

In summary, a detailed thermodynamic model of a thermochemical heat distribution network has been presented, many potential absorption pairs have been modelled and one good performing and economically viable absorption pair has been identified.

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Informed Consent Statement: Not applicable.

Data Availability Statement: Please refer to References.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A. Refrigerant Properties

The following sections present the equations used to calculate the thermophysical properties of the analysed refrigerants.

Appendix A.1. Acetone

Appendix A.1.1. Specific Heat

The specific heat (c_p) of pure acetone liquid can be calculated with the following equation [9]:

 $c_p = 2.110 - 1.631 \cdot 10^{-3} \cdot t + 2.781 \cdot 10^{-5} \cdot t^2 (\text{kJ/kg K}) \tag{A1} \label{eq:A1}$

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where t is the temperature in $^{\circ}$ C. The given correlation can be used in the temperature range between -10 and 60 $^{\circ}$ C.

Appendix A.1.2. Enthalpy

The enthalpy of acetone as a saturated liquid (h_f) can be calculated with the following equation [10]:

$$h_f = 177.185 + 2.154 \cdot t_{sat} + 1.06 \cdot 10^{-5} t_{sat}^3 (kJ/kg)$$
 (A2)

The enthalpy of acetone as a saturated gas (h_g) can be calculated with the following equation [10]:

$$h_f = 177.185 + 2.154 \cdot t_{sat} + 1.06 \cdot 10^{-5} t_{sat}^3 (kJ/kg)$$
 (A3)

The enthalpy of acetone as a superheated gas (h_{sh}) can be calculated with the following equation [10]:

$$h_{sh} = exp(6.62 + 0.00170 \cdot t - 0.003 \cdot p)(kJ/kg) \tag{A4}$$

where t and t_{sat} are the temperature and saturated temperature respectively both in $^{\circ}C$ and p is the pressure in bar.

Appendix A.1.3. Density

The density (ρ) of the acetone liquid can be obtained using the following equation [11]:

$$\rho = 1.091 - 9.272 \cdot 10^{-4} \text{T} - 3.233 \cdot 10^{-7} \text{T}^2 (\text{kg/m}^3) \tag{A5}$$

where T is the temperature in K.

Appendix A.1.4. Saturated Pressure

The saturation vapour pressure (p_{sat}) of pure acetone can be calculated with the following equation [10]:

$$p_{sat} = 10^{4.424 - (\frac{1312.253}{t_{sat} + 240.71})} (bar)$$
 (A6)

where t_{sat} is the saturated temperature in ${}^{\circ}C$.

Appendix A.1.5. Saturated Temperature

The saturation temperature t_{sat} can be found by rearranging the previous (p_{sat}) equation:

$$t_{sat} = \frac{1312.253}{4.42448 - \log_{10}(p_{sat})} - 240.705 \, (^{\circ}C) \tag{A7}$$

where p_{sat} is the saturation pressure in bar.

Appendix A.2. Methanol

Appendix A.2.1. Specific Heat

The specific heat (c_p) of pure methanol liquid can be calculated with the following equations [12]:

$$c_{p} = S_{n} \cdot x \cdot f(J/mol K) \tag{A8}$$

where $f=-A_1\cdot\beta\cdot u^{\rho-1}+\frac{A_2}{x}+\sum\limits_{i=3}^5A_i\cdot(i-2)x^{i-3}$, x and u are defined as: $x=T/T_c$ and u=(1-x).

The coefficients used in the equations are A_1 = 0.352, A_2 = -1.316, A_3 = 4.062, A_4 = -3.605, A_5 = 1.275, β = 0.35, T_c = 513.15 K, S_n = -106.045 and T is the temperature in K.

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Appendix A.2.2. Enthalpy

The enthalpy of methanol as a saturated liquid (h_f) can be calculated with the following equation [13]:

$$h_f = 2.96833 \cdot 10^{-3} t^2 + 2.40423 t - 1.21727 \cdot 10^3 (kJ/kg)$$
 (A9)

where t is the temperature in $^{\circ}$ C. The given correlation can be used in the temperature range between -30 and 73 $^{\circ}$ C.

The enthalpy of methanol as a saturated gas (h_g) can be calculated with the following equation [13]:

$$h_g = -1.09858 \cdot 10^{-3} t^2 + 1.05359 t - 1.21724 \cdot 10^1 (kJ/kg) \tag{A10}$$

where t is the temperature in $^{\circ}$ C. The given correlation can be used in the temperature range between -30 and 73 $^{\circ}$ C.

The enthalpy of methanol as a superheated gas (h_{sh}) can be calculated with the following equation [13]:

$$\begin{split} h_{sh} &= -8.626 + 1.108 \cdot t_{sat} - 8.353 \cdot 10^{-4} \cdot t_{sat}^2 - 5.812 \cdot 10^{-6} \cdot t_{sat}^3 \\ &+ 1.600 \cdot xx + 7.986 \cdot 10^{-3} xx \cdot t_{sat} + 3.564 \cdot 10^{-5} xx \cdot t_{sat}^2 \\ &- 7.088 \cdot 10^{-8} xx \cdot t_{sat}^3 - 1.561 \cdot 10^{-3} xx^2 - 5.011 \cdot 10^{-5} xx^2 \cdot t_{sat} \\ &- 2.363 \cdot 10^{-7} xx^2 \cdot t_{sat}^2 + 1.098 \cdot 10^{-9} xx^2 \cdot t_{sat}^3 + 7.709 \cdot 10^{-6} xx^3 \\ &+ 1.379 \cdot 10^{-7} xx^3 \cdot t_{sat} + 5.367 \cdot 10^{-10} xx^3 \cdot t_{sat}^2 \\ &- 3.330 \cdot 10^{-12} xx^3 \cdot t_{sat}^3 \left(kJ/kg \right) \end{split} \tag{A11}$$

where $xx = t - t_{sat}$, t is the temperature and t_{sat} is the saturation temperature both in $^{\circ}C$. The given correlation can be used in the temperature range between -30 and 73 $^{\circ}C$ and in the range of t between 5 and 200 $^{\circ}C$.

Appendix A.2.3. Density

The density (ρ) of pure methanol liquid can be calculated with the following equation [12]:

$$\rho = M \rho_c \Big(\Big(au^\beta + b(x-1) + c\Big(x^2-1\Big) + d\Big(x^3-1\Big) \Big) + 1 \Big) (kg/m^3) \tag{A12} \label{eq:alpha_constraint}$$

where $x = T/T_c$ and u = (1 - x).

The coefficients used in the equations are M = 32.04 g/mol, a = 2.517, b = -2.467, c = 3.067, d = -1.325, β = 0.35, T_c = 513.15 K, ρ_c = 8.455 mol/L and T is the temperature in K

Appendix A.2.4. Saturated Pressure

The saturation pressure (p_{sat}) of methanol is calculated with the following equation [12]:

$$p_{sat} = exp(\frac{a}{x} + b + cx + dx^2 + ex^3 + f(1 - x)^p)(bar)$$
 (A13)

where $x = T/T_c$.

The coefficients used in the equations are a=-10.753, b=16.758, c=-3.603, d=4.373, e=-2.381, f=4.572, p=1.70, $T_c=513.15$ K and T in the temperature in K.

Appendix A.3. Water

Appendix A.3.1. Specific Heat

The pure water specific heat at constant pressure (c_p) can be calculated with the following equation [14]:

$$c_p = a + b \cdot t + c \cdot t^{1.5} + d \cdot t^2 + e \cdot t^{2.5} (kJ/kg K)$$
 (A14)

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where a = 4.217, b = -0.00562, c = 0.00130, d = -0.000115, and e = 4.150×10^{-6} are constants and t is the temperature in $^{\circ}$ C.

Appendix A.3.2. Enthalpy

The enthalpy of water as a saturated liquid (h_f) can be calculated using the following equation [14]:

$$h_f = d_1 + d_2 \cdot t + d_3 \cdot t^2 + d_4 \cdot t^3 + d_5 \cdot t^4 + d_6 \cdot t^5 (kJ/kg)$$
(A15)

where $d_1 = -2.844699 \cdot 10^{-2}$, $d_2 = 4.211925$, $d_3 = -1.017034 \cdot 10^{-3}$, $d_4 = 1.31105 \cdot 10^{-5}$, $d_5 = -6.756469 \times 10^{-8}$, and $d_6 = 1.724481 \times 10^{-10}$ are constants and t is the temperature in °C.

The enthalpy of water as a saturated gas (h_g) can be obtained by adding the enthalpy of saturated liquid (h_f) plus the latent heat of vaporisation (h_{fg}) [14]:

$$h_g = h_f + h_{fg}(kJ/kg) \tag{A16}$$

The latent heat of vaporisation h_{fg} of the water can be approximated with the following equation:

$$h_{\rm fg} = a + b \cdot t + c \cdot t^{1.5} + d \cdot t^{2.5} + e \cdot t^3 (kJ/kg) \tag{A17} \label{eq:A17}$$

where a = 2500.304, b = -2.252, c = -0.0215, d = $3.175 \cdot 10^{-3}$, and e = -2.861×10^{-5} are constants and t is the temperature in $^{\circ}$ C.

The enthalpy of the water as a superheated gas (h_{sh}) can be calculated with the following equation [15]:

$$\mathbf{h}_{sh} = h_C \sum_{k=1}^{16} a_k (T_C/T)^{m_k} (p/p_C)^{n_k} (kJ/kg)$$
 (A18)

where p_C = 22.055 MPa, T_C = 647.126 K, h_C = 2086 kJ/kg and p is the pressure in bar. The coefficients used in the equation can be found in Table A1.

Table A1. Coefficients of the water superheated enthalpy

k	m_k	n_k	a _J	k
1	-5	1	-7.226	10^{-3}
2	-4	1	1.767	10^{-2}
3	-2	0	7.114	10^{-2}
4	-1	0	4.874	10^{-1}
5	-1	1	-3.596	10^{-2}
6	0	0	9.935	10^{-1}
7	1	0	-5.504	10^{-3}
8	1	3	4.874	10^{-3}
9	3	1	-1.449	10^{-1}
10	4	4	5.302	10^{-3}
11	5	3	-7.348	10^{-3}
12	7	1	-9.027	10^{-3}
13	9	2	-9.697	10^{-2}
14	24	5	-6.634	10^{-2}
15	36	9	1.974	10^{-2}
16	57	11	-8.783	10 - 2

Appendix A.3.3. Density

The pure water density (ρ) can be calculated with the use of the following equation [14]:

$$\rho = a + b \cdot t + c \cdot t^2 + d \cdot t^{2.5} + e \cdot t^3 (kg/m^3)$$
(A19)

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where a = 999.797, b = 0.0683, c = -0.0107, d = 0.000821, and e = -2.303×10^{-5} are constants and t is the temperature in $^{\circ}$ C. This equation is valid in the range of temperatures between 0 and 150 $^{\circ}$ C.

Appendix A.3.4. Saturated Pressure

The saturation pressure (p_{sat}) of water is calculated with the following equation [16]:

$$\ln\left(\frac{p_{sat}}{p_c}\right) = \frac{T_c}{T} \left(a_1 \cdot \tau + a_2 \cdot \tau^{1.5} + a_3 \cdot \tau^3 + a_4 \cdot \tau^{3.5} + a_5 \cdot \tau^4 + a_6 \cdot \tau^{7.5} \right) \tag{A20}$$

where: $\tau = 1 - \theta$ and $\theta = \frac{T}{T_c}$.

The coefficients used in the equations are $a_1 = -7.85951783$, $a_2 = 1.84408259$, $a_3 = -11.7866497$, $a_4 = 22.6807411$, $a_5 = -15.9618719$, $a_6 = 1.08122502$, $p_c = 220.64$ bar and $T_c = 647.096$ K, T is the temperature in K and p_{sat} is the saturated pressure in MPa.

The given correlation can be used in the temperature range between 273.16 and 647.10 K.

Appendix B. Solution Properties

The following sections present the equations used to calculate the thermophysical properties of the analysed solutions:

Appendix B.1. Water Based

Appendix B.1.1. H₂O-LiBr

Specific Heat

The specific heat (c_p) of the solution water–lithium bromide can be calculated using the following equation [17]:

$$\begin{split} c_p &= -2 \, T \cdot \left(C_0 + C_1 x + C_2 x^2 + C_3 x^3 + C_4 x^{1.1} \right) \\ &- 6 \, T^2 \cdot \left(D_0 + D_1 x + D_2 x^2 + D_4 x^{1.1} \right) - 12 \, T^3 \cdot \left(E_0 + E_1 x \right) \\ &- 2 \frac{\left(F_0 + F_1 x \right) \cdot T}{\left(T - T_0 \right)^3} - 2 \cdot p \cdot T \cdot \left(V_6 + V_7 x \right) \\ &+ \frac{1}{T} \left(L_0 + L_1 x + L_2 x^2 + L_3 x^3 + L_4 x^{1.1} \right) \\ &- \left(M_0 + M_1 x + M_2 x^2 + M_3 x^3 + M_4 x^{1.1} \right) (kJ/kg \, K) \end{split} \tag{A21}$$

where $p = 3.06 \cdot 10^{-5}$ kPa, $T_0 = 220$ K, and x is the salt concentration of the solution in%. The coefficients C_n , D_n , E_n , $E_$

Table A2. Coefficients of the H₂O-LiBr specific heat equation.

n	C _n	D _n	En	F _n	L _n	M _n	V _n
0	2.65×10^{-2}	-8.53×10^{-6}	-3.84×10^{-11}	-5.16×10^{1}	-2.18×10^{3}	-2.27×10^{1}	-
1	-2.31×10^{-3}	1.32×10^{-6}	2.63×10^{-11}	1.11×10^{0}	-1.27×10^{2}	2.98×10^{-1}	-
2	7.56×10^{-6}	2.79×10^{-11}	-	-	-2.36×10^{0}	-1.26×10^{-2}	-
3	-3.76×10^{-8}	-	-	-	1.39×10^{-2}	6.85×10^{-5}	-
4	1.18×10^{-3}	-8.51×10^{-7}	-	-	1.85×10^{2}	2.77×10^{-1}	-
5	-	-	-	-	-	-	-
6	-	-	-	-	-	-	3.06×10^{-9}
7	-	-	-	-	-	-	-5.13×10^{-11}

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Enthalpy

The enthalpy (h) of the solution water–lithium bromide can be calculated using the following equation [18]:

$$h = \sum_{n=0}^{4} A_n \cdot x^n + t \sum_{n=0}^{4} B_n \cdot x^n + t^2 \sum_{n=0}^{4} C_n \cdot x^n (kJ/kg)$$
 (A22)

where t is the temperature in ${}^{\circ}C$ and x is the salt concentration in the solution in%. The coefficients used in the equations can be found in Table A3:

Table A3. Coefficients of the H₂O-LiBr enthalpy equation.

n	A_n	B _n	C _n
0	2.024×10^{3}	1.828×10^{1}	-3.701×10^{-2}
1	1.633×10^{2}	-1.169×10^{0}	2.888×10^{-3}
2	-4.882×10^{0}	3.248×10^{-2}	-8.131×10^{-5}
3	6.303×10^{-2}	-4.034×10^{-4}	9.912×10^{-7}
4	$-2.914 imes 10^{-4}$	$1.852 \times 10^{-6} \times 10^{-2}$	-4.444×10^{-9}

This equation is valid for concentration ranges between 40 and 70% and temperatures between 15 and 165 $^{\circ}$ C.

Density

The density (ρ) of the solution water–lithium bromide can be calculated using the following equation [19]:

$$\rho = \sum_{i=0}^{3} \sum_{i=0}^{4} A_{ji} t^{j} \cdot x^{i} (kg/m^{3})$$
(A23)

where t is the temperature in ${}^{\circ}C$, x is the salt concentration of the solution in% and the coefficients A_{ii} can be found in Table A4:

Table A4. Coefficients of the H₂O-LiBr density equation.

j∖i	0	1	2	3	4
0	1.17×10^{3}	-6.89×10^{0}	4.77×10^{-1}	-5.77×10^{-3}	3.87×10^{-5}
1	-5.80×10^{-1}	1.32×10^{-2}	-1.45×10^{-4}	-1.74×10^{-6}	0
2	-9.29×10^{-4}	-5.37×10^{-5}	1.19×10^{-6}	0	0
3	-1.55×10^{-6}	1.52×10^{-7}	-2.40×10^{-9}	0	0

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium bromide can be calculated with the following equation [18]:

$$p_{sat} = exp(C + D/T_{sat} + E/T_{sat}^2)(kPa)$$
 (A24)

where C = 7.05, D = -1596.49, E = -104095.5 and T_{sat} is the saturation temperature in K. The given correlation can be used in the saturation temperature range between -15 and $110\,^{\circ}$ C and in the salt concentration range between 45 and 70%.

Saturated Temperature

The saturation vapour pressure (t_{sat}) of the solution water–lithium bromide can be calculated with the following equation [18]:

$$t_{sat} = t - \sum_{0}^{3} B_{n} x^{n} / \sum_{0}^{3} A_{n} x^{n} (^{\circ}C)$$
 (A25)

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The given correlation can be used in the temperature range between 5 and 175 $^{\circ}$ C and in the salt concentration range between 45 and 70%.

The coefficients A_n and B_n can be found in Table A5:

Table A5. Coefficients of the H₂O-LiBr saturated temperature equation.

n	$\mathbf{A}_{\mathbf{n}}$	B _n
0	-2.008×10^{0}	1.245×10^{2}
1	1.698×10^{-1}	-7.716×10^{0}
2	-3.133×10^{-3}	1.523×10^{-1}
3	1.977×10^{-5}	-7.951×10^{-4}

Appendix B.1.2. H₂O-LiI (4:1)

Specific Heat

The specific heat (c_p) of the solution water–lithium bromide+lithium iodide can be calculated using the following equation [20]:

$$c_p = \sum_{n=0}^4 A_n x^n + T \sum_{n=0}^4 B_n x^n + T^2 \sum_{n=0}^4 C_n x^n (kJ/kg K)$$
 (A26)

where T is the temperature in K and x is the salt concentration of the solution in%.

The calculated values are valid in the range of temperatures between 283.15 and 343.15 K and in the range of absorbent concentration between 15.4 and 66.6%.

The coefficients A_n , B_n , and C_n used in the equation can be found in Table A6:

Table A6. Coefficients of the H₂O-LiI specific heat equation.

n	A _n	B _n	C _n
0	5.505×10^{0}	-8.57×10^{-3}	$1.371 \times 10 - 5 \times 10^{-1}$
1	-5.867×10^{-2}	1.199×10^{-4}	-1.891×10^{-7}
2	-1.001×10^{-3}	3.361×10^{-6}	-3.415×10^{-9}
3	2.065×10^{-5}	-6.617×10^{-8}	7.270×10^{-11}
4	-9.018×10^{-8}	2.796×10^{-10}	-3.230×10^{-13}

Enthalpy

The enthalpy (h) of the solution water–lithium bromide+lithium iodide (salt mole ratio 4:1) can be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
(A27)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

The integral enthalpy of mixing (h_m) is calculated with the following equation [16]:

$$h_{m} = w \cdot (1 - w) \sum_{i=0}^{6} a_{i} (1 - 2w)^{i} (kJ/kg)$$
 (A28)

where w is the mass ratio of absorbent in kg/kg.

The equation can be used in solutions with a salt mass ratio between 0 and 0.623. The coefficients a_i used in the equation can be found in Table A7:

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i	$a_{ m i}$
0	-8.39×10^{2}
1	3.88×10^{2}
2	5.16×10^{2}
3	-1.13×10^{3}
4	-8.18×10^{1}
5	7.67×10^{2}
6	-9.25×10^{1}

Table A7. Coefficients of the H₂O-LiI enthalpy equation.

Density

The density (ρ) of the solution water–lithium chloride can be calculated using the following equation [21]:

$$\rho = \sum_{i=0}^{n} x^{i} \left(a_{i} + b_{i} \cdot T + c_{i} \cdot T^{2} \right) (kg/m^{3})$$
(A29)

where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 283.15 and 353.15 K and in the salt concentration range between 10.2 and 65.5%.

The coefficients a_i , b_i and c_i can be found in Table A8:

Table A8. Coefficients of the H₂O-LiI density equation.

i	A_{i}	B _i	C _i
0	7.539×10^{2}	1.883×10^{0}	-3.589×10^{-3}
1	1.185×10^{1}	-2.186×10^{-2}	2.744×10^{-5}
2	1.334×10^{-1}	-9.834×10^{-4}	1.711×10^{-6}
3	2.222×10^{-6}	1.057×10^{-5}	-1.976×10^{-8}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium bromide+lithium iodide can be calculated with the following equations [22]:

$$log(p_{sat}) = \sum_{n=0}^{6} (A_n + {}^{1000 \cdot B_n}/_{T-43.15}) \cdot x^n$$
(A30)

$$log(p_{sat}) = \sum_{n=0}^{4} (A_n + {}^{1000 \cdot B_n/T} - {}^{43.15}) \cdot x^n$$
(A31)

where p_{sat} is the saturated pressure in Pa, T is the temperature in K and x is the salt concentration of the solution in%.

Correlation 1 can be used in the temperature range between 313.45 and 383.05 K and in the salt concentration range between 10 and 64.1%.

Correlation 1 can be used in the temperature range between 280.85 and 343.15 K and in the salt concentration range between 47.7 and 64.5%.

The coefficients A_n and B_n used in the equation can be found in Table A9:

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n	$\mathbf{A_n}(1)$	$\mathbf{B_n}(1)$	$A_n(2)$	B _n (2)
0	1.01×10^{1}	-1.69×10^{0}	1.12×10^{1}	-7.00×10^{0}
1	9.48×10^{-5}	2.87×10^{-4}	-2.14×10^{-1}	4.53×10^{-1}
2	1.88×10^{-5}	-1.67×10^{-4}	1.02×10^{-2}	-1.43×10^{-2}
3	-4.45×10^{-6}	1.07×10^{-5}	$-1.87 imes 10^{-4}$	1.98×10^{-4}
4	3.02×10^{-7}	-3.49×10^{-7}	1.20×10^{-6}	-1.04×10^{-6}
5	-7.70×10^{-9}	5.10×10^{-9}		
6	6.73×10^{-11}	-3.20×10^{-11}		

Table A9. Coefficients of the H₂O-LiI saturated pressure equation.

Appendix B.1.3. $H_2O-LiBr + LiNO_3$ (0.7:0.3)

Specific Heat

The specific heat (c_p) of the solution water–lithium bromide+lithium nitrate can be calculated using the following equation [23]:

$$c_p = \sum_{n=0}^4 A_n x^n + T \sum_{n=0}^4 B_n x^n + T^2 \sum_{n=0}^4 C_n x^n (kJ/kg K)$$
 (A32)

where T is the temperature in K and x is the salt concentration of the solution in%.

The calculated values are valid in the range of temperatures between 283.15 and 343.15 K and in the range of absorbent concentration between 9.9 and 64.1%.

The coefficients A_n , B_n , and C_n used in the equation can be found in Table A10:

Table A10. Coefficients of the H₂O-LiBr + LiNO₃ specific heat equation.

n	A _n	B _n	C _n
0	5.449×10^{0}	-7.985×10^{-3}	1.257×10^{-5}
1	-9.707×10^{-2}	2.354×10^{-4}	-2.542×10^{-7}
2	5.708×10^{-4}	-2.144×10^{-6}	1.852×10^{-9}
3	2.284×10^{-6}	4.533×10^{-9}	-1.085×10^{-12}
4	-2.559×10^{-8}	1.233×10^{-11}	-3.721×10^{-14}

Enthalpy

The enthalpy (h) of the solution water–lithium bromide+lithium nitrate be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg) \tag{A33}$$

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

The integral enthalpy of mixing (h_m) is calculated with the following equation [18]:

$$h_{m} = x_{1}x_{2} \sum_{n=0}^{6} G_{n}(x_{2} - x_{1})^{n}(kJ/kg)$$
(A34)

where x_1 is the salt concentration and x_2 is the refrigerant concentration in the solution in%. The equation can be used in solutions with a salt concentration between 0 and 61.5%.

The coefficients G_n used in the equations can be found in Table A11:

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n	G _n	n	G _n
0	8.41×10^{-2}	4	-1.72×10^{-10}
1	-4.09×10^{-4}	5	-6.50×10^{-12}
2	-2.28×10^{-6}	6	4.51×10^{-14}
3	7.17×10^{-8}		

Table A11. Coefficients of the H₂O-LiBr + LiNO₃ enthalpy equation.

Density

The density (ρ) of the solution water–lithium bromide+lithium nitrate can be calculated using the following equation [23]:

$$\rho = \sum_{n=0}^{4} A_n x_1^n + T \sum_{n=0}^{4} B_n x_1^n + T^2 \sum_{n=0}^{4} C_n x_1^n (kg/m^3)$$
 (A35)

where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 283.15 and 353.15 K and in the salt concentration range between 11.6 and 62.4%.

The coefficients A_n , B_n and C_n can be found in Table A12:

Table A12. Coefficients of the H_2O -LiBr + LiNO₃ density equation.

n	$\mathbf{A}_{\mathbf{n}}$	B_n	C_n
0	7.51×10^{2}	1.91×10^{0}	-3.64×10^{-3}
1	1.64×10^{1}	-6.19×10^{-2}	9.44×10^{-5}
2	-5.77×10^{-3}	4.27×10^{-4}	-8.59×10^{-7}
3	-6.50×10^{-4}	2.47×10^{-6}	2.44×10^{-9}
4	2.66×10^{-5}	-9.00×10^{-8}	6.34×10^{-11}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium bromide+lithium Nitrate can be calculated with the following equations [23]:

$$\log(p_{sat}) = \sum_{n=0}^{4} A_n x^n + (1000/T - 43.15) \sum_{n=0}^{4} B_n x^n$$
 (A36)

$$log(p_{sat}) = \sum_{n=0}^{6} A_n x^n + {\scriptstyle (1000/T-43.15)} \sum_{n=0}^{6} B_n x^n \tag{A37} \label{eq:A37}$$

where p_{sat} is the saturated pressure in Pa, T is the temperature in K and x is the salt concentration of the solution in%.

Correlation 1 can be used in the temperature range between 278.35 and 335.95 K and in the salt concentration range between 30.4 and 62.2%.

Correlation 1 can be used in the temperature range between 320.55 and 442.75 K and in the salt concentration range between 10.3 and 72.7%.

The coefficients A_n and B_n used in the equation can be found in Table A13:

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n	$\mathbf{A_n}(1)$	$B_n(1)$	$\mathbf{A_n}(2)$	B _n (2)
0	3.560×10^{0}	-6.695×10^{-1}	1.012×10^{1}	-1.689×10^{0}
1	6.305×10^{-1}	-1.020×10^{-1}	-6.284×10^{-3}	3.978×10^{-3}
2	-2.171×10^{-2}	3.553×10^{-3}	9.478×10^{-4}	-6.925×10^{-4}
3	3.145×10^{-4}	-5.127×10^{-5}	-6.388×10^{-5}	4.015×10^{-5}
4	-1.628×10^{-6}	2.437×10^{-7}	1.596×10^{-6}	-9.840×10^{-7}
5			-1.658×10^{-8}	1.008×10^{-8}
6			6.228×10^{-11}	-3.734×10^{-11}

Table A13. Coefficients of the H₂O-LiBr + LiNO₃ saturated pressure equation.

Appendix B.1.4. H_2O –LiBr + $ZnCl_2$ + $CaBr_2$ (1:1:0.13) Specific Heat

The specific heat (c_p) of the solution water–lithium bromide+zinc chloride+calcium Bromide can be calculated using the following equation [24]:

$$c_p = \sum_{n=0}^{6} A_n x^n + T \sum_{n=0}^{6} B_n x^n + T^2 \sum_{n=0}^{6} C_n x^n (kJ/kg K)$$
 (A38)

where T is the temperature in K and x is the salt concentration of the solution in%.

The calculated values are valid in the range of temperatures between 283.15 and 343.15 K and in the range of absorbent concentration between 10 and 74.4%.

The coefficients A_n , B_n , and C_n used in the equation can be found in Table A14:

Table A14. Coefficients of the H_2O -LiBr + LiNO₃ specific heat equation.

n	A_n	B_n	C_n
0	5.221×10^{0}	-6.985×10^{-3}	1.163×10^{-5}
1	-7.858×10^{-2}	1.456×10^{-4}	$-9.226 \times 10 - 8$
2	1.010×10^{-3}	-2.049×10^{-6}	-2.390×10^{-9}
3	-1.378×10^{-5}	6.424×10^{-8}	1.724×10^{-11}
4	$-4.405 imes 10^{-8}$	-1.334×10^{-9}	5.232×10^{-13}
5	2.671×10^{-9}	1.220×10^{-11}	-1.679×10^{-15}
6	-1.498×10^{-11}	-3.968×10^{-14}	2.826×10^{-17}

Enthalpy

The enthalpy (h) of the solution water–lithium bromide+zinc chloride+calcium bromide be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
 (A39)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

The integral enthalpy of mixing (h_m) is calculated with the following equation [24]:

$$h_{m} = x_{1}x_{2} \sum_{n=1}^{7} G_{n}(x_{2} - x_{1})^{n-1} (kJ/kg)$$
(A40)

where x_1 is the salt concentration and x_2 is the refrigerant concentration in the solution in%. The equation can be used in solutions with a salt concentration between 0 and 78%.

The coefficients G_n used in the equations can be found in Table A15:

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Table A15. Coefficie	ents of the H2O-LiBr +	 LiNO₃ enthalpy equation.

n	G_n	n	G_n
1	-5.774×10^{-2}	5	-3.243×10^{-11}
2	-2.883×10^{-4}	6	1.245×10^{-11}
3	$-3.641 \times 10^{-}6$	7	8.107×10^{-14}
4	-6.153×10^{-8}		

Density

The density (ρ) of the solution water–lithium bromide + zinc chloride + calcium bromide are given in Table A16 [24]:

Table A16. Density of the solution H₂O-LiBr + LiNO₃.

Absorbent Concentration (wt%) Temperature (C)	29.8	40.2	50.1	59.8	70.7	75.5
10	1276	1390	1524	1687	1935	2077
20	1270	1383	1517	1679	1926	2065
30	1264	1376	1509	1671	1916	2054
40	1258	1369	1502	1663	1907	2043
50	1251	1362	1494	1655	1898	2032
60	1244	1354	1487	1647	1889	2022
70	1236	1347	1479	1639	1879	2012
80	1228	1339	1471	1631	1870	2002

The given values are valid in the temperature range between 283.15 and 353.15 K and in the salt concentration range between 29.8 and 75.5%.

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium bromide + zinc chloride + calcium bromide can be calculated with the following equation [24]:

$$h_m = x_1 x_2 \sum_{n=1}^{7} G_n (x_2 - x_1)^{n-1} (kJ/kg)$$
 (A41)

where p_{sat} is the saturated pressure in Pa, T is the temperature in K and x is the salt concentration of the solution in%. The given correlation can be used in the temperature range between 318.35 and 443.35 K and in the salt concentration range between 9.9 and 78.8%.

The coefficients A_n and B_n used in the equation can be found in Table A17:

Table A17. Coefficients of the H₂O-LiBr + LiNO₃ saturated pressure equation.

n	A _n	B _n
0	1.012×10^{1}	-1.689×10^{0}
1	-7.829×10^{-4}	-1.111×10^{-3}
2	1.996×10^{-4}	1.638×10^{-4}
3	-6.974×10^{-6}	$-1.278 \times 10^{-}5$
4	6.709×10^{-8}	3.772×10^{-7}
5	-9.405×10^{-10}	-4.412×10^{-9}
6	1.377×10^{-11}	1.389×10^{-11}

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Appendix B.1.5. H₂O-LiCl

Specific Heat

The specific heat (c_p) of the solution water–lithium chloride can be calculated using the following equation [25]:

$$c_p = c_{P_{H_2O}} \cdot (1 - f_1 \cdot f_2) (kJ/kgK)$$
 (A42)

The function f_1 is defined as: For $0 \le w \le 0.31$: $f_1 = A_1 \cdot w + B_1 \cdot w^2 + C_1 \cdot w^3$

For w > 0.31: $f_1 = D_1 + E_1 \cdot w$

The function f_2 is defined as: $f_2 = F_1 \cdot \theta^{0.02} + G_1 \cdot \theta^{0.04} + H_1 \cdot \theta^{0.06}$

 θ is defined as: $\theta = T/228 - 1$

where T is the temperature in K and w is the ratio of salt in the solution.

The specific heat capacity of the liquid water $\left(c_{p_{H_2O}}\right)$ is calculated with the following equation:

$$c_{p_{H_2O}} = A_2 + B_2 \theta^{0.02} + C_2 \theta^{0.04} + D_2 \theta^{0.06} + E_2 \theta^{1.8} + F_2 \theta^8 (kJ/kg\, K) \tag{A43} \label{eq:A43}$$

The coefficients A_n , B_n , C_n , D_n , E_n , F_n , G_n , and H_n used in the equation can be found in Table A18:

Table A18. Coefficients of the H₂O-LiCl specific heat equation.

n	An	B _n	Cn	D _n	En	Fn	Gn	H _n
1	1.440	-1.243	-0.121	0.128	0.629	58.523	-105.634	47.795
2	88.789	-120.196	-16.926	52.465	0.108	0.470	-	-

Enthalpy

The enthalpy (h) of the solution water–lithium chloride can be calculated using the following equation [26]:

$$h = A + B \cdot t + C \cdot t^2 (kJ/kg) \tag{A44}$$

where t is the temperature in $^{\circ}$ C. The coefficients A, B and C can be calculated with the equations below:

$$A = -66.232 + 11.271x - 0.799x^2 + 2.153 \cdot 10^{-2}x^3 - 1.664 \cdot 10^{-4}x^4$$
 (A45)

$$B = 4.575 - 0.147x + 6.307 \cdot 10^{-3}x^2 - 1.381 \cdot 10^{-4}x^3 + 1.067 \cdot 10^{-6}x^4$$
(A46)

$$C = -8.097 \cdot 10^{-4} + 2.181 \cdot 10^{-4} x - 1.362 \cdot 10^{-5} x^2 + 3.210 \cdot 10^{-7} x^3 - 2.643 \cdot 10^{-7} x^4$$
 (A47)

where x is the salt concentration in the solution in%.

Density

The density (ρ) of the solution water–lithium chloride can be calculated using the following equation [25]:

$$\rho = \rho_{H_2O} \cdot \sum_{i=0}^{3} \rho_i \cdot (w/_{1-w})^i (kg/_{m^3})$$
(A48)

with

$$\begin{split} \rho_{H_2O} &= \rho_{c,H_2O} \cdot \Big(1 + B_0 \cdot \tau^{\frac{1}{3}} + B_1 \cdot \tau^{\frac{2}{3}} + B_2 \cdot \tau^{\frac{5}{3}} + B_3 \cdot \tau^{\frac{16}{3}} + B_4 \cdot \tau^{\frac{43}{3}} + B_5 \cdot \tau^{110/3} \Big) (kg/m^3) \quad (A49) \\ \text{and } \tau &= 1 - {^{T/}}{T_c}. \end{split}$$

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Where T_c is the critical temperature of water 647.3 K, T is the temperature of the solution in K, w is the ratio of salt in the solution, ρ_{H_2O} is the density of pure water, ρ_{c,H_2O} is the density of water at the critical point 322 kg/m³. The given correlation can be used in the salt ratio range between 0 and 0.56.

The coefficients ρ_i and B_n can be found in Table A19:

Table A19. Coefficients of the H₂O-LiCl density equation.

n	$ ho_{ m i}$	B_n
0	1.000×10^{0}	1.994×10^{0}
1	5.410×10^{-1}	1.099×100
2	$-3.038 imes 10^{-1}$	-5.095×10^{-1}
3	1.008×10^{-1}	-1.762×10^{0}
4		-4.590×10^{1}
5		-7.237×10^5

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium bromide + zinc chloride + calcium bromide can be calculated with the following equation [26]:

$$\log(p_{sat}) = A + B/T + C/T^2 \tag{A50}$$

where p_{sat} is the saturated pressure in mmHg, T is the temperature in K and the coefficients A, B and C are defined below:

$$A = 8.203 - 0.135 \cdot m + 0.0179 \cdot m^2 - 0.000529 \cdot m^3$$
 (A51)

$$B = -1727.8 + 58.385 \cdot m - 10.208 \cdot m^2 + 0.313 \cdot m^3$$
 (A52)

$$C = -95014 - 4701.526 \cdot m + 929.081 \cdot m^2 - 31.766 \cdot m^3$$
(A53)

where m corresponds to the molality of the salt in mol/kg.

Appendix B.1.6. H_2O –LiCl + LiNO₃ (2.8:1) Specific Heat

The specific heat (c_p) of the solution water–lithium choride + lithium nitrate (salt mole ratio 2.8:1) can be calculated using the following equation [27]:

$$c_p = \sum_{i=0}^{6} x^i (a_i + b_i \cdot T + c_i \cdot T^2) (kJ/kgK)$$
 (A54)

where T is the temperature in K and x is the salt concentration of the solution in%. The calculated values are valid in the range of temperatures between 283.15 and 433.15 K and in the range of absorbent concentration between 9.1 and 63.5%.

The coefficients a_n , b_n , and c_n used in the equation can be found in Table A20:

Table A20. Coefficients of the H₂O-LiCl + LiNO₃ specific heat equation.

i	a _i	b	c _i
0	5.448×10^{0}	-7.990×10^{-3}	1.257×10^{-5}
1	-6.168×10^{-2}	9.942×10^{-5}	-1.430×10^{-7}
2	1.826×10^{-4}	-1.314×10^{-6}	1.905×10^{-9}
3	1.070×10^{-5}	5.321×10^{-8}	-8.028×10^{-11}
4	-2.145×10^{-7}	-1.038×10^{-9}	1.606×10^{-12}
5	1.485×10^{-9}	9.695×10^{-12}	-1.522×10^{-14}
6	-3.292×10^{-12}	-3.464×10^{-14}	5.488×10^{-17}

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Enthalpy

The enthalpy (h) of the solution water–lithium chloride+lithium nitrate can be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
 (A55)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

The integral enthalpy of mixing (h_m) is calculated with the following Equation (21):

$$h_{m} = w \cdot (1 - w) \sum_{i=0}^{6} a_{i} (1 - 2w)^{i} (kJ/kg)$$
(A56)

where w is the mass ratio of absorbent (kg/kg). The equation can be used in solutions with a salt mass ratio between 0 and 0.518.

The coefficients a_i used in the equation can be found in Table A21:

Table A21. Coefficients of the H₂O-LiCl + LiNO₃ enthalpy equation.

i	a _i
0	-6.512×10^2
1	-1.643×10^2
2	-7.208×10^{0}
3	5.210×10^{2}
4	2.116×10^{2}
5	-4.898×10^2
6	4.229×10^{-2}

Density

The density (ρ) of the solution water–lithium chloride+lithium nitrate can be calculated using the following equation [21]:

$$\rho = \sum_{i=0}^{n} x^{i} \cdot \left(a_{i} + b_{i} \cdot T + c_{i} \cdot T^{2}\right) (kg/m^{3}) \tag{A57} \label{eq:A57}$$

where T is the temperature in K, x is the salt concentration of the solution in% and the coefficients a_i , b_i and c_i can be found in Table A22:

Table A22. Coefficients of the H₂O-LiCl + LiNO₃ density equation.

i	a_{i}	b_i	$c_{\mathbf{i}}$
0	7.431×10^{2}	1.953×10^{0}	-3.688×10^{-3}
1	1.756×10^{1}	-7.793×10^{-2}	1.214×10^{-4}
2	-5.465×10^{-2}	6.194×10^{-4}	-1.026×10^{-6}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water–lithium chloride + lithium nitrate can be calculated with the following equations [28]:

$$\log(p_{sat}) = \sum_{n=0}^{4} (A_i + B_i/T - 43.15) \cdot x^i$$
 (A58)

$$log(p_{sat}) = \sum_{n=0}^{6} (A_i + B_i/T - 43.15) \cdot x^i$$
(A59)

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where p_{sat} is the saturated pressure in Pa, T is the temperature in K and x is the salt concentration of the solution in%.

Correlation 1 can be used in the temperature range between 274.15 and 328.15 K. Correlation 1 can be used in the temperature range between 310.95 and 422.65 K.

The coefficients A_n and B_n used in the equation can be found in Table A23:

Table A23. Coefficients of the H₂O-LiCl+LiNO₃ saturated pressure equation.

n	$\mathbf{A_n}(1)$	$\mathbf{B_n}(1)$	$\mathbf{A_n}(2)$	$B_n(2)$
0	1.097×10^{1}	-1.830×10^{3}	1.012×10^{1}	-1.689×10^{3}
1	$-9.245 imes 10^{-2}$	1.164×10^{-1}	-3.503×10^{-4}	-2.844×10^{1}
2	3.226×10^{-3}	-2.348×10^{-1}	-2.080×10^{-4}	-1.219×10^{-3}
3	-5.026×10^{-5}	-2.604×10^{-3}	-5.560×10^{-6}	1.860×10^{-3}
4	3.246×10^{-7}	3.813×10^{-5}	3.898×10^{-7}	$-1.479 imes 10^{-4}$
5			-5.327×10^{-9}	2.144×10^{-6}
6			2.331×10^{-11}	-9.964×10^{-9}

Appendix B.1.7. H₂O-LiI

Specific Heat

The specific heat (c_p) of pure lithium iodide can be calculated using the following equation [29]:

$$c_p = A + A \cdot \theta + C \cdot \theta^2 + D \cdot \theta^3 + \text{E}/\theta^2 (\text{kJ/kg}\,\text{K}) \tag{A60} \label{eq:A60}$$

where θ is $\theta = T(K)/1000$.

The specific heat of pure water can be calculated with Equation (A53).

According to the literature [30] the specific heat of a 50% aqueous LiI solution at 30 °C is 2.27 kJ/(kg·K).

The specific heat of the aqueous salt mixture was therefore calculated interpolating concentration values, from pure water to 50% salt mixture to pure LiI. For a particular concentration, the specific heat of the mixture does not vary much with temperature [30].

Enthalpy

The enthalpy (h) of the solution water–lithium chloride can be calculated using the following equation [30]:

$$c_p = A + A \cdot \theta + C \cdot \theta^2 + D \cdot \theta^3 + E/\theta^2(kJ/kgK)$$
(A61)

where t is the temperature in °C. The coefficients A, B and C can be calculated with the equations below:

$$A = -1866.39 + 90.605x - 1.025x^{2} - 7.318 \cdot 10^{-3}x^{3} + 1.304 \cdot 10^{-4}x^{4}$$
 (A62)

$$B = 15.538 - 0.602x + 6.583 \cdot 10^{-3}x^{2} + 3.897 \cdot 10^{-5}x^{3} - 7.190 \cdot 10^{-7}x^{4}$$
 (A63)

$$C = -2.613 \cdot 10^{-2} + 1.271 \cdot 10^{-3} x - 1.400 \cdot 10^{-5} x^{2} - 1.081 \cdot 10^{-7} x^{3} + 1.778 \cdot 10^{-9} x^{4}$$
 (A64)

where x is the salt concentration in the solution in%. These equations are valid for solutions with a salt concentration between 45 and 70% at temperatures between 0 and 100 $^{\circ}$ C. Additionally, a table with the enthalpy values of a wider range of salt concentrations can be found in [30].

Density

The density (ρ) of the solution water–lithium iodide can be calculated using the following equation [31]:

$$\rho = \sum_{n=0}^{3} (A_n + B_n T) \cdot x^n (kg/m^3)$$
 (A65)

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where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 303.15 and 343.15 K and in the salt concentration range between 14.96 and 27.02%.

The coefficients A_n and B_n can be found in Table A24:

Table A24. Coefficients of the H₂O-LiI density equation.

n	A_n	B _n
0	-2.22×10^{2}	3.91×10^{0}
1	2.12×10^{2}	-6.56×10^{-1}
2	-9.66×10^{0}	3.10×10^{-2}
3	1.51×10^{-1}	-5.00×10^{-4}

Saturated Temperature

The saturation temperature (t_{sat}) of the solution water–lithium iodide can be calculated with the following equation [30]:

$$t_{sat} = x - B/A(^{\circ}C) \tag{A66}$$

where t_{sat} is the saturated temperature in ${}^{\circ}C$, x is the salt concentration of the solution in% and the coefficients A and B can be calculated with the following equations:

$$A = a_0 + a_1 x + a_2 x^2 + a_3 x^3 \tag{A67}$$

$$B = b_0 + b_1 x + b_2 x^2 + b_3 x^3 \tag{A68}$$

The coefficients a_n and b_n of the previous equations can be found in Table A25:

Table A25. Coefficients of the H₂O-LiI saturated temperature equation.

n	a _n	b_n
0	2.79×10^{0}	-2.15×10^{2}
1	-1.13×10^{-1}	$1.45 imes 10^1$
2	2.34×10^{-3}	-3.23×10^{-1}

The given correlation can be used in the temperature range between 20 and 100 $^{\circ}$ C and in the salt concentration range between 45 and 66%.

Appendix B.1.8. H₂O-Ca(NO₃)₂

Specific Heat

The specific heat (c_p) of the solution water–calcium nitrate can be calculated using the following equation [32]:

$$c_p = (m \cdot C_{p,\phi} + c_p^0) / (1 + m \cdot M_2) (kJ/kg K)$$
 (A69)

where $c_{p,\Phi}$ is the apparent molar heat capacity of the solution (J/(mol·K)), c_p^0 is the specific heat capacity of pure water (kJ/(kg·K)), m is the molality of the solution (mol/kg) and M_2 is the molar mass of solute (g/mol).

The apparent molar heat capacities of the solution at different molalities and temperatures can be found in Table A26:

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m (mol/kg) T (K)	273	298.15	323	348	373
0.005	-341	-169	-124	-118	-133
0.750	-207	-45	-8.2	-6	-21
1.50	-133	7.4	38	39	27
2.50	-63	54	78	79	70
4.0	45	99	116	116	111
6.0	58	134	145	144	141
10.0	113	172	176	172	166
14.0	150	203	201	190	175
0.005	-341	-169	-124	-118	-133

Table A26. Apparent molar heat capacities of the solution $H_2O-Ca(NO_3)_2$.

Enthalpy

The enthalpy (h) of the solution water–calcium nitrate be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
 (A70)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

In order to obtain the enthalpy of the solution, firstly the enthalpy of mixing needs to be calculated using the following equation:

$$h_{m} = w \cdot h_{s} + z \cdot h_{d}(kJ/kg)$$
 (A71)

where w is the mass fraction of salt in the solution in kg/kg and z is the mass fraction of refrigerant in the solution, h_s is the heat of solution and h_d is the hat of dilution. Both the heats of solution and dilution at different molalities (m) can be found in Table A27 [33]:

m	$H_{s}\left(J/mol\right)$	$\mathbf{H_d}(J/mol)$
1.542	-24,100	100
2.687	-25,100	190
6.021	-22,250	-90
8.805	-17,600	-815
12.150	-13,150	-1830
15.826	-8500	-2765
17.530	-6350	-3425
19.620	-3700	-4545
20.290	-2750	-4805
20.870	-2000	-5110

Density

The density (ρ) of the solution water–calcium nitrate at a set molality (m) can be calculated using the following equation [34]:

$$\rho = A + B \cdot t + c \cdot t^2 (kg/m^3) \tag{A72}$$

where t is the temperature in °C.

The molality and parameters A, B and C can be found in Table A28:

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Molality	A	В	С
0.0093	0.997	-4.78×10^{-5}	5.49×10^{-6}
0.466	1.057	9.68×10^{-5}	4.65×10^{-6}
1.08	1.125	1.98×10^{-4}	4.01×10^{-6}
2.07	1.227	4.47×10^{-4}	2.36×10^{-6}
3.01	1.309	5.20×10^{-4}	2.29×10^{-6}
3.99	1.376	6.00×10^{-4}	1.61×10^{-6}
7.00	1.546	7.49×10^{-4}	5.90×10^{-7}
9.94	1.663	8.32×10^{-4}	2.00×10^{-8}
17.6	1.847	1.02×10^{-3}	-2.01×10^{-6}

Table A28. Coefficients of the H₂O-Ca(NO₃)₂ density equation.

Saturated Pressure

The saturation vapour pressure (p_{sat}) in mmHg of the solution water–calcium nitrate at different salt fractions and temperatures can be found in Table A29 [35]:

Table A29. Coefficients of the H₂O-Ca(NO₃)₂ saturated pressure equation.

x (% salt) t (°C)	20.2	30.6	49.7	59.1	66.6	72.2	74.2	74.7	76.3	76.9	77.4
20	16.4	15.3	11.3	8.2	5.4	3.7	3.2	3.1	2.5	2.4	2.3
30	29.9	27.6	20.6	15.1	10.4	6.9	6.0	5.8	4.9	4.6	4.5
40	52.6	48.0	36.1	26.6	18.7	12.7	10.7	10.4	9.2	8.6	8.4
50	86.8	80.2	61.3	45.3	31.6	21.9	18.9	18.0	16.2	15.1	14.8
60	140.6	130.5	99.7	75.0	52.7	36.8	31.9	30.0	27.5	25.5	25.0

Appendix B.1.9. H₂O–NaOH

Specific Heat

The specific heat (c_p) of the solution water-sodium hydroxide can be calculated using the following equation [36]:

$$c_{p} = c_{p_{H_{2}O}} - \sum_{i=1}^{j=5} \sum_{i=0}^{i=5} a_{ij} \tau^{i} m^{j} (kJ/kg K)$$
(A73)

 τ is defined as: $\tau = T/T_0$

where c_{PH_2O} is the heat capacity of water in kJ/(kg·K), $T_0 = 273.15$ K and m is the molality of the solution in mol/kg.

The values for the a_{ij} coefficients are presented in Table A30:

Table A30. Coefficients of the H₂O-NaOH specific heat equation.

a _{ij}	1	2	3	4	5
0	9.86×10^{1}	-3.44×10^{1}	1.98×10^{0}	-5.62×10^{-2}	7.99×10^{-3}
1	-3.45×10^{1}	1.17×10^{2}	-5.38×10^{0}	8.59×10^{-2}	-1.54×10^{-2}
2	4.82×10^{2}	-1.58×10^{2}	5.51×10^{0}	-1.70×10^{-2}	7.50×10^{-3}
3	-3.34×10^{2}	1.06×10^{2}	-2.54×10^{0}	-1.49×10^{-2}	-
4	1.15×10^{2}	-3.51×10^{1}	4.59×10^{-1}	-	-
5	-1.57×10^{1}	4.59×10^{0}	-	-	-

The calculated values are valid in the range of molalities up to 4 mol/kg at a pressure up to 7 MPa and between the temperatures of 283.15 and 343.15 K. Other values of specific heat at higher molalities can be found in [37].

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Enthalpy

The enthalpy (h) of the solution water-sodium hydroxide can be calculated using the following equation [38]:

$$h = c_1 + c_2 \cdot t + c_3 \cdot t^2 + c_4 \cdot t^3 (kJ/kg)$$
(A74)

where t is the temperature in ${}^{\circ}C$ and the coefficients c_1 , c_2 , c_3 and c_4 are polynomial functions of z, the mass fraction of the water in the solution.

$$c_1 = \frac{k_0 + k_2 \cdot z + k_4 \cdot z^2 + k_6 \cdot z^3}{1 + k_1 \cdot z + k_3 \cdot z^2 + k_5 \cdot z^3 + k_7 \cdot z^4}$$
(A75)

$$c_2 = l_0 + l_1 \cdot z + l_2 \cdot z^2 + l_3 \cdot z^3 + l_4 \cdot z^4 + l_5 \cdot z^5 + l_6 \cdot z^6 + l_7 \cdot z^7 + l_8 \cdot z^8$$
(A76)

$$c_3 = m_0 + m_1 \cdot z + m_2 \cdot z^2 + m_3 \cdot z^3 + m_4 \cdot z^4 + m_5 \cdot z^5 + m_6 \cdot z^6 + m_7 \cdot z^7$$
 (A77)

$$c_4 = n_0 + n_1 \cdot z + n_2 \cdot z^2 + n_3 \cdot z^3 + n_4 \cdot z^4 + n_5 \cdot z^5 + n_6 \cdot z^6 + n_7 \cdot z^7 \tag{A78} \label{eq:A78}$$

The constants needed in the equations can be found in Table A31:

Table A31. Coefficients of the H₂O-NaOH enthalpy equation.

i	k _i	l _i	m _i	n _i
0	1.29×10^{3}	2.31×10^{0}	2.30×10^{-2}	-8.51×10^{-5}
1	$-4.96 imes 10^{-1}$	-9.00×10^{0}	-3.79×10^{-1}	1.37×10^{-3}
2	-4.39×10^{3}	1.68×10^{2}	2.45×10^{0}	-8.76×10^{-3}
3	-4.09×10^{0}	-1.00×10^{3}	-8.27×10^{0}	2.92×10^{-2}
4	4.94×10^{3}	3.39×10^{3}	$1.57 imes 10^{1}$	-5.49×10^{-2}
5	7.29×10^{0}	-6.12×10^{3}	-1.69×10^{1}	5.84×10^{-2}
6	-1.84×10^{3}	6.22×10^{3}	9.63×10^{0}	-3.28×10^{-2}
7	-3.02×10^{0}	-3.35×10^{3}	-2.24×10^{0}	7.54×10^{-3}
8	-	7.44×10^2	-	-

It should be noted that the enthalpy correlation only must be used within the temperature and concentration ranges indicated Table A32:

Table A32. Temperature range of the H_2O -NaOH enthalpy equation.

Temperature Range (°C)	Concentration Range (kg H ₂ O/kg sol.)
$0 \le t < 4$	$0.78 \le x \le 1$
$4 \le t < 10$	$0.68 \le x \le 1$
$10 \le t < 15$	$0.58 \le x \le 1$
$15 \le t < 26$	$0.54 \le x \le 1$
$26 \le t < 37$	$0.44 \le x \le 1$
$37 \le t < 48$	$0.40 \le x \le 1$
$48 \le t < 60$	$0.34 \le x \le 1$
$60 \le t < 71$	$0.30 \le x \le 1$
$71 \le t < 82$	$0.28 \le x \le 1$
$82 \le t < 93$	$0.24 \le x \le 1$
93 ≤ t < 204	$0.22 \le x \le 1$

Density

The density (ρ) of the solution acetone-zinc bromide can be calculated using the following equation [38]:

$$\rho = b_1 + b_2 \cdot t + b_3 \cdot t^2 (kg/m^3) \tag{A79}$$

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where the coefficients b_1 , b_2 and b_3 are functions of z, the water mass fraction in the solution (kg/kg) and can be obtained with the following equations:

$$b_1 = k_{p0} + k_{p1} \cdot z^{1/2} + k_{p2} \cdot z + k_{p3} \cdot z^{3/2} + k_{p4} \cdot z^2 + k_{p5} \cdot z^{5/2}$$
(A80)

$$b_2 = l_{p0} + l_{p1} \cdot z^{1/2} + l_{p2} \cdot z + l_{p3} \cdot z^{3/2} + l_{p4} \cdot z^2 + l_{p5} \cdot z^{5/2}$$
(A81)

$$b_3 = m_{p0} + m_{p1} \cdot z^{1/2} + m_{p2} \cdot z + m_{p3} \cdot z^{3/2} + m_{p4} \cdot z^2 + m_{p5} \cdot z^{5/2}$$
(A82)

The given correlation can be used in the temperature range between 0 and 200 °C.

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution water-sodium hydroxide can be calculated with the following equations [38]:

$$a_1 + a_2 \cdot t + a_3 \cdot \ln p_{sat} = t \cdot \ln p_{sat} \tag{A83}$$

where p_{sat} is the saturated pressure in kPa, t is the temperature in ${}^{\circ}C$ and the coefficients a_1 , a_2 and a_3 are polynomial functions defined below:

$$a_{1} = k_{0} + k_{1} \ln x + k_{2} (\ln x)^{2} + k_{3} (\ln x)^{3} + k_{4} (\ln x)^{4} + k_{5} (\ln x)^{5} + k_{6} (\ln x)^{6} + k_{7} (\ln x)^{7} + k_{8} (\ln x)^{8}$$
(A84)

$$a_{2} = l_{0} + l_{1} \ln x + l_{2} (\ln x)^{2} + l_{3} (\ln x)^{3} + l_{4} (\ln x)^{4} + l_{5} (\ln x)^{5} + l_{6} (\ln x)^{6} + l_{7} (\ln x)^{7} + l_{8} (\ln x)^{8} + l_{9} (\ln x)^{9} + l_{10} (\ln x)^{10}$$

$$(A85)$$

$$\begin{aligned} a_3 &= m_0 + m_1 \ln x + m_2 (\ln x)^2 + m_3 (\ln x)^3 + m_4 (\ln x)^4 + m_5 (\ln x)^5 \\ &+ m_6 (\ln x)^6 + m_7 (\ln x)^7 + m_8 (\ln x)^8 + m_9 (\ln x)^9 \\ &+ m_{10} (\ln x)^{10} \end{aligned} \tag{A86}$$

where x is the salt concentration of the solution in% and the coefficients k_i , l_i and m_i used in the equations can be found in Table A33:

Table A33. Coefficients of the H₂O-NaOH saturated pressure equation.

i	k_i	l_i	m_i
0	-1.14×10^{2}	1.62×10^{1}	-2.27×10^{2}
1	2.10×10^{2}	-1.19×10^{1}	2.93×10^{2}
2	4.95×10^{2}	-2.23×10^{2}	5.08×10^{3}
3	6.86×10^{3}	-1.65×10^{3}	3.68×10^{4}
4	2.68×10^{3}	-6.00×10^{3}	1.31×10^{5}
5	-2.17×10^4	-1.23×10^4	2.59×10^{5}
6	-3.48×10^{4}	-1.53×10^4	3.02×10^{5}
7	-2.01×10^{4}	-1.17×10^4	2.09×10^{5}
8	-4.10×10^{3}	-5.36×10^{3}	8.18×10^{4}
9	-	-1.34×10^{3}	1.56×10^{4}
10	-	-1.38×10^{2}	9.06×10^{2}

It should be noted that the enthalpy correlation only must be used within the temperature and concentration ranges indicated Table A34:

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Table A34. Temperature range of the H ₂ O-NaOH saturated pressure equation	Table A34. Ten	nperature range o	of the H2O-I	NaOH saturated	pressure equation.
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Temperature Range (°C)	Concentration Range (kg H ₂ O/kg sol.)
$0 \le t < 20$	$0.582 \le x \le 1$
$20 \le t < 60$	$0.500 \le x \le 1$
$60 \le t < 70$	$0.353 \le x \le 1$
$70 \le t < 150$	$0.300 \le x \le 1$

Appendix B.2. Acetone-Based

Appendix B.2.1. (CH₃)₂CO–ZnBr₂

Specific Heat

The specific heat (c_p) of the solution acetone-zinc bromide can be calculated using the following equation [10]:

$$c_p = \frac{1}{0.609 - 0.000978 \,t + 8.121 \cdot 10^{-5} \,x^2} (kJ/kgK) \tag{A87}$$

where t is the temperature in $^{\circ}$ C and x is the concentration of salt in the solution in%. The given correlation can be used in the temperature range between 0 and 70 $^{\circ}$ C and in the salt concentration range between 30 and 70%.

Enthalpy

The enthalpy (h) of the solution acetone-zinc bromide can be calculated using the following equation [10]:

$$h = \sum_{i=0}^{1} \sum_{j=0}^{4} a_{ij} x^{i} t^{j} (kJ/kg)$$
 (A88)

where t is the temperature in $^{\circ}$ C and x is the salt concentration of the solution in%. The given correlation can be used in the temperature range between 0 and 70 $^{\circ}$ C and in the salt concentration range between 30 and 70%.

The constants needed in the equations can be found in Table A35:

Table A35. Coefficients of the (CH₃)₂CO-ZnBr₂ enthalpy equation.

a ₀₀	176.64×10^{0}	a ₁₀	-2.95×10^{2}
a ₀₁	1892×10^{0}	a ₁₁	-1.31×10^{-2}
a_{02}	$-1616 imes 10^{-4}$	a ₁₂	2.87×10^{-5}
a_{03}	1486×10^{-5}	a ₁₃	-5.02×10^{-7}
a_{04}	-2439×10^{-8}	a ₁₄	1755×10^{-9}

Density

The density (ρ) of the solution Acetone-Zinc Bromide can be calculated using the following equation [10]:

$$\rho = 1.051 - 0.00258 \cdot t + 4.752 \cdot 10^{-6} \ x^3 (\text{kg/m}^3) \tag{A89} \label{eq:approx}$$

where t is the temperature in ${}^{\circ}C$ and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 0 and 70 $^{\circ}$ C and in the salt concentration range between 30 and 70%.

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Saturated Pressure

The saturated pressure (p_{sat}) of the solution acetone-zinc bromide can be calculated using the following equation [10]:

$$p_{sat} = \exp \sum_{i=0}^{2} \sum_{j=0}^{2} a_{ij} t^{i} x^{j} (bar)$$
 (A90)

where t is the temperature in ${}^{\circ}C$ and x is the salt concentration of the solution in%.

The constants needed in the equations can be found in Table A36:

Table A36. Coefficients of the (CH₃)₂CO-ZnBr₂ saturated pressure equation.

a ₀₀	-2.41×10^{0}	a ₁₀	5.35×10^{-2}	a ₂₀	-2.13×10^{-4}
a_{01}	1.72×10^{-2}	a ₁₁	-1.16×10^{-4}	a ₂₁	3.66×10^{-6}
a_{02}	-5.58×10^{-4}	a ₁₂	2.38×10^{-6}	a ₂₂	-4.61×10^{-8}

Appendix B.3. Methanol-Based

Appendix B.3.1. CH₃OH-LiBr

Specific Heat

The specific heat (c_p) of the solution methanol–lithium bromide can be calculated using the following equation [39]:

$$c_p = C_p(t_0) \cdot \left\{ 1 + a_t(w)(t - t_0) + b_t(w)(t - t_0)^2 \right\} (kJ/kgK) \tag{A91}$$

where t is the temperature in ${}^{\circ}C$, t_0 is 25 ${}^{\circ}C$ and w is the salt concentration of the solution. $c_p(t_0)$, $a_t(w)$, and $b_t(w)$ are described below:

$$c_p(t_0) = a_w w^3 + b_w w^2 + c_w w + d_w \text{ is the specific heat at } t_0. \tag{A92} \label{eq:A92}$$

$$a_t(w) = a_1 w^3 + a_2 w^2 + a_3 w + a_4$$
 (A93)

$$b_{t}(w) = b_{1}w^{3} + b_{2}w^{2} + b_{3}w + b_{4}$$
(A94)

The constants needed in the equations can be found in Table A37:

Table A37. Coefficients of the CH₃OH-LiBr specific heat equation.

a _w b _w	1.81×10^{0} -2.52×10^{0}	a ₁ a ₂	$1.11 \times 10^{-2} \\ -2.25 \times 10^{-2}$	b ₁ b ₂	$1.51 \times 10^{-4} \\ -2.88 \times 10^{-4}$
$egin{array}{c} & & & \\ c_{\mathbf{w}} & & \\ d_{\mathbf{w}} & & \end{array}$	2.58×10^{0} 6.38×10^{-1}	a ₃ a ₄	$1.59 \times 10^{-2} \\ -2.07 \times 10^{-3}$	b ₃ b ₄	$1.85 \times 10^{-4} \\ -3.62 \times 10^{-5}$

Enthalpy

The enthalpy (h) of the solution methanol–lithium bromide be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
 (A95)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

In order to obtain the enthalpy of the solution, firstly the enthalpy of mixing needs to be calculated using the following equation [40]:

$$h_{\rm m} = \sum_{i=0}^{4} G_{\rm n} x^{\rm n} (kJ/kg)$$
 (A96)

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where x is the absorbent concentration in%.

The coefficients G_n used in the equation can be found in Table A38:

Table A38. Coefficients of the CH₃OH-LiBr enthalpy equation.

n	G_n	n	G _n
0	-2.40×10^{1}	3	8.49×10^{-3}
1	1.00×10^{1}	4	-8.64×10^{-5}
2	-3.35×10^{-1}		

Density

The density (ρ) of the solution methanol–lithium bromide can be calculated using the following equation [40]:

$$\rho = \sum_{n=0}^{5} x^{n} \left(A_{n} + B_{n} T + C_{n} T^{2} \right) (kg/m^{3})$$
(A97)

where T is the temperature in K and x is the salt concentration of the solution in%. The given correlation can be used in the temperature range between 278.15 and 368.15 K and in the salt concentration range between 6.78 and 46%.

The constants needed in the equations can be found in Table A39:

Table A39. Coefficients of the CH₃OH-LiBr density equation.

n	A	В	С
0	-1620.83	17.1537	-0.0303477
1	721.992	-4.76916	0.00791908
2	-100.217	0.669436	-0.0011116
3	5.72691	-0.0382586	6.35817×10^{-5}
4	-0.135968	0.000909044	-1.51178×10^{-6}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution methanol–lithium bromide can be calculated with the following equation [40]:

$$\log p_{\text{sat}} = \sum_{n=0}^{2} A_n x^n + \frac{1}{t + 230} \sum_{n=0}^{2} B_n x^n - 0.874792$$
 (A98)

where p_{sat} is the saturated pressure in kPa, t is the temperature in $^{\circ}$ C and x is the salt concentration of the solution in%. The given correlation can be used in the saturation temperature range between 19.9 and 70 $^{\circ}$ C and in the salt concentration range between 10 and 48%.

The values of the constants A_n and B_n are presented in Table A40:

Table A40. Coefficients of the CH₃OH-LiBr saturated pressure equation.

n	$\mathbf{A_n}$	B _n
0	7.68×10^{0}	1.45×10^{3}
1	8.79×10^{-3}	-7.73×10^{-1}
2	-6.39×10^{-5}	1.30×10^{-1}

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Appendix B.3.2. CH₃OH–LiBr + ZnCl₂ (1:1) Specific Heat

The specific heat (c_p) of the solution methanol–lithium bromide+zinc chloride can be calculated using the following equation [41]:

$$c_p = \sum_{n=0}^4 A_n x^n + T \sum_{n=0}^4 B_n x^n + T^2 \sum_{n=0}^4 C_n x^n \left(\frac{kJ}{kg K} \right) \tag{A99}$$

where T is the temperature in K and x is the salt concentration of the solution in%. The calculated values are valid in the range of temperatures between 283.15 and 343.15 K and in the range of absorbent concentration between 9.8 and 64.7%.

The coefficients A_n , B_n , and C_n used in the equation can be found in Table A41:

Table A41. Coefficients of the CH₃OH-LiBr + ZnCl₂ specific heat equation.

n	A _n	B _n	C _n
0	3.90×10^{0}	-1.55×10^{-2}	3.66×10^{-5}
1	2.55×10^{-2}	-1.66×10^{-4}	-3.25×10^{-9}
2	-1.50×10^{-3}	7.96×10^{-6}	-6.78×10^{-9}
3	1.57×10^{-5}	-7.09×10^{-8}	7.05×10^{-12}
4	-1.02×10^{-7}	4.48×10^{-10}	-5.13×10^{-14}

Enthalpy

The enthalpy (h) of the solution methanol–lithium bromide+zinc chloride be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
(A100)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

In order to obtain the enthalpy of the solution, firstly the enthalpy of mixing needs to be calculated using the following equation [41]:

$$h_m = x \cdot y \sum_{i=0}^{6} G_n (x - y)^n (kJ/kg)$$
 (A101)

where x is the absorbent concentration in% and y is the concentration% of working medium. Values of the constant G_n are shown in Table A42:

Table A42. Coefficients of the CH₃OH-LiBr+ZnCl₂ enthalpy equation.

n	G_n	n	G_n
0	-7.17×10^{-2}	4	3.78×10^{-10}
1	-8.90×10^{-5}	5	-4.63×10^{-14}
2	4.08×10^{-6}	6	-3.87×10^{-15}
3	7.18×10^{-8}		

Density

The density (ρ) of the solution Methanol–lithium bromide+zinc chloride can be calculated using the following equation [40]:

$$\rho = \sum_{n=0}^{6} x^{n} \left(A_{n} + B_{n} T + C_{n} T^{2} \right) (kg/m^{3})$$
 (A102)

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where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 278.15 and 333.15 K and in the salt concentration range between 5.9 and 59.8%.

The constants needed in the equations can be found in Table A43:

Table A43. Coefficients of the CH₃OH-LiBr+ZnCl₂ density equation.

n	A	В	С
0	953.194	-3.43923	0.00429622
1	19.9451	-0.056638	-0.0010869
2	-0.438282	0.64392	9.47677×10^{-5}
3	0.00543066	0.0023045	-3.82168×10^{-6}
4	-	-4.67307×10^{-5}	7.69761×10^{-8}
5	-	4.57966×10^{-6}	-7.49146×10^{-10}
6	-	-1.7251×10^{-9}	2.79391×10^{-12}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution methanol-lithium bromide+zinc chloride can be calculated with the following equation [40]:

$$\log p_{sat} = \sum_{n=0}^{6} A_n x^n + \left[\frac{1000}{T - 43.15} \right] \sum_{n=0}^{6} B_n x^n - 3$$
 (A103)

where p_{sat} is the saturated pressure in kPa, T is the absolute temperature in K and x is the salt concentration of the solution in%. The given correlation can be used in the saturation temperature range between 273.15 and 391.25 K and in the salt concentration range between 8.1 and 66.4%.

The values of the constants A_n and B_n are presented in Table A44:

Table A44. Coefficients of the CH₃OH-LiBr + ZnCl₂ saturated pressure equation.

n	$\mathbf{A_n}$	B _n
0	9.98×10^{0}	-1.47×10^{0}
1	-3.46×10^{-3}	-2.08×10^{-4}
2	1.74×10^{-4}	6.15×10^{-5}
3	-2.97×10^{-7}	-8.52×10^{-6}
4	-8.18×10^{-8}	3.09×10^{-7}
5	7.22×10^{-10}	-4.91×10^{-9}
6	7.61×10^{-12}	2.33×10^{-11}

Appendix B.3.3. $CH_3OH-LiBr + ZnBr_2$ (2:1)

Specific Heat

The specific heat (c_p) of the solution methanol–lithium bromide+zinc bromide can be calculated using the following equation [39]:

$$c_p = c_p(t_0) \cdot \left\{ 1 + a_t(w) \cdot (t - t_0) + b_t(w) \cdot (t - t_0)^2 \right\} (kJ/kg \, K) \tag{A104} \label{eq:A104}$$

 $c_p(t_0)$, $a_t(w)$ and $b_t(w)$ are described below:

$$c_p(t_0) = a_w w^3 + b_w w^2 + c_w w + d_w$$
 is the specific heat at t_0 (A105)

$$a_t(w) = a_1 w^3 + a_2 w^2 + a_3 w + a_4$$
 (A106)

$$b_t(w) = b_1 w^3 + b_2 w^2 + b_3 w + b_4 (A107)$$

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where t is the temperature in ${}^{\circ}C$, t_0 is 25 ${}^{\circ}C$ and w is the ratio of salt in the solution (kg/kg). The constants needed in the equations can be found in Table A45:

Table A45. Coefficients of the CH₃OH-LiBr+ZnBr₂ specific heat equation.

$a_{\mathbf{w}}$	-3.06×10^{-1}	a_1	0×10^{0}	b_1	8.95×10^{-5}
$\mathbf{b_w}$	1.24×10^{0}	a_2	-1.68×10^{-3}	b_2	-1.48×10^{-4}
$c_{\mathbf{w}}$	7.65×10^{-1}	a_3	4.63×10^{-3}	b_3	8.13×10^{-5}
$d_{\mathbf{w}}$	8.14×10^{-1}	a_4	-5.38×10^{-3}	b_4	-1.09×10^{-5}

Enthalpy

The enthalpy (h) of the solution methanol–lithium bromide+zinc bromide can be calculated using the following equation [40]:

$$h = \sum_{n=0}^{3} A_n x^n + t \sum_{n=0}^{3} B_n x^n + t^2 \sum_{n=0}^{3} C_n x^n (kJ/kg)$$
 (A108)

where t is the temperature in K and x is the salt concentration of the solution in%. The given correlation can be used in the temperature range between 10 and 100 $^{\circ}$ C and in the salt concentration range between 30 and 52%.

The values of the constants A_n , B_n and C_n are presented in Table A46:

Table A46. Coefficients of the CH₃OH-LiBr + ZnBr₂ enthalpy equation.

n	A _n	B _n	C _n
0	-3.46×10^{-1}	4.34×10^{0}	-3.54×10^{-2}
1	-3.17×10^{0}	-2.72×10^{-1}	2.83×10^{-3}
2	-1.76×10^{-1}	7.36×10^{-3}	-7.35×10^{-5}
3	3.58×10^{-3}	-6.20×10^{-5}	6.34×10^{-7}

Density

The density (ρ) of the solution methanol–lithium bromide+zinc bromide can be calculated using the following equation [40]:

$$\rho = \sum_{n=0}^{4} x^{n} \Big(A_{n} + B_{n} T + C_{n} T^{2} \Big) (kg/m^{3})$$
(A109)

where T is the temperature in K and x is the salt concentration of the solution in%. The given correlation can be used in the temperature range between 278.15 and 333.15 K and in the salt concentration range between 9 and 59.8%.

The constants needed in the equations can be found in Table A47:

Table A47. Coefficients of the CH₃OH-LiBr + ZnBr₂ density equation.

n	Α	В	С
0	1071.75	-0.984162	9.0221×10^{-5}
1	-21.1574	0.204756	-0.000322142
2	2.45735	-0.0166866	2.62866×10^{-5}
3	-0.0639115	0.000440603	-6.93698×10^{-7}
4	0.000545047	-3.64216×10^{-6}	5.73216×10^{-9}

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Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution methanol–lithium bromide+zinc bromide can be calculated with the following equation [40]:

$$\log p_{\text{sat}} = \sum_{n=0}^{4} A_n x^n + \frac{1}{t + 230} \sum_{n=0}^{4} B_n x^n - 0.874792$$
 (A110)

where p_{sat} is the saturated pressure in kPa, t is the temperature in $^{\circ}$ C and x is the salt concentration of the solution in%. The given correlation can be used in the saturation temperature range between 10 and 100 $^{\circ}$ C and in the salt concentration range between 30 and 52%.

The values of the constants A_n and B_n are presented in Table A48:

Table A48. Coefficients of the CH₃OH-LiBr + ZnBr₂ saturated pressure equation.

n	A _n	B _n
0	-2.80×10^{2}	1.23×10^{5}
1	2.89×10^{1}	-1.27×10^{4}
2	-1.03×10^{0}	4.59×10^{2}
3	1.60×10^{-2}	-7.20×10^{0}
4	-9.16×10^{-5}	4.16×10^{-2}

Appendix B.3.4. CH₃OH-LiI + ZnBr₂ (2:1)

Specific Heat

The specific heat (c_p) of the solution methanol–lithium iodide+zinc bromide can be calculated using the following equation [40]:

$$c_p = \sum_{n=0}^{2} A_n x^n + T \sum_{n=0}^{2} B_n x^n + T^2 \sum_{n=0}^{2} C_n x^n (kJ/kg K)$$
 (A111)

where T is the temperature in K and x is the salt concentration of the solution in%.

The calculated values are valid in the range of temperatures between 278.15 and 333.15 K and in the range of absorbent concentration between 5 and 51.28%.

The coefficients A_n , B_n , and C_n used in the equation can be found in Table A49:

Table A49. Coefficients of the CH₃OH-LiI + ZnBr₂ specific heat equation.

n	A _n	B _n	Cn
0	-1.47×10^{1}	1.08×10^{-1}	-1.67×10^{-4}
1	9.02×10^{-1}	-6.20×10^{-3}	1.03×10^{-5}
2	$-1.27 imes 10^{-2}$	8.34×10^{-5}	-1.35×10^{-7}

Enthalpy

The enthalpy (h) of the solution methanol–lithium iodide+zinc bromide can be calculated using the following equation [40]:

$$h = \sum_{n=0}^{2} A_n x^n + T \sum_{n=0}^{2} B_n x^n + T^2 \sum_{n=0}^{2} C_n x^n (kJ/kg)$$
 (A112)

where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 233 and 393.15 K and in the salt concentration range between 0 and 70%.

The values of the constants A_n , B_n , and C_n are presented in Table A50:

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Table A50. Coefficients of	the CH3OH-LiI + ZnBr2	specific heat equation.

n	A _n	B _n	C _n
0	-2.09×10^{2}	2.14×10^{0}	6.85×10^{-4}
1	1.53×10^{3}	-1.21×10^{1}	1.55×10^{-2}
2	-5.54×10^{2}	6.89×10^{0}	-9.83×10^{-3}

Density

The density (ρ) of the solution methanol–lithium iodide+zinc bromide can be calculated using the following equation [40]:

$$\rho = \sum_{n=0}^{5} x^{n} \left(A_{n} + B_{n} T + C_{n} T^{2} \right) (kg/m^{3})$$
(A113)

where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 278.15 and 333.15 K and in the salt concentration range between 5 and 51.28%.

The constants needed in the equations can be found in Table A51:

Table A51. Coefficients of the CH₃OH-LiI + ZnBr₂ density equation.

n	A	В	С
0	2142.37	-8.120	0.0121
1	-367.703	2.489	-0.00415
2	42.189	-0.280	0.000465
3	-1.948	0.0132	-2.191×10^{-5}
4	0.0409	-0.000272	4.517×10^{-7}
5	-0.000302	2.0146×10^{-6}	-3.349×10^{-9}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution methanol–lithium iodide+zinc bromide can be calculated with the following equation [40]:

$$\log p_{sat} = \sum_{n=0}^{2} A_n x^n + \frac{1}{t + 230} \sum_{n=0}^{2} B_n x^n - 0.874792$$
 (A114)

where p_{sat} is the saturated pressure in kPa, t is the temperature in ${}^{\circ}C$ and x is the salt concentration of the solution in%.

The values of the constants A_n and B_n for temperatures between 20 and 90 °C are presented in Tables A52 and A53.

• For salt concentration range of 0–30%:

Table A52. Coefficients of the CH₃OH-LiI + ZnBr₂ saturated pressure equation.

n	$\mathbf{A}_{\mathbf{n}}$	B_n
0	7.90×10^{0}	1.45×10^{3}
1	-9.41×10^{-3}	1.73×10^{0}
2	1.45×10^{-5}	-4.57×10^{-2}

• For salt concentration range of 30–50%:

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	Table A53. Coeffic	ients of the CH3OH-L	LiI + ZnBr2 saturated	pressure equation.
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n	A _n	B _n
0	$7.22 imes 10^0$	9.62×10^{2}
1	1.38×10^{-2}	2.46×10^{1}
2	-8.72×10^{-5}	2.68×10^{-1}

Appendix B.3.5. CH₃OH–ZnBr₂

Specific Heat

The specific heat (c_p) of the solution methanol-zinc bromide can be calculated using the following equation [39]:

$$c_p = c_p(t_0) \cdot \left\{ 1 + a_t(w) \cdot (t - t_0) + b_t(w) \cdot (t - t_0)^2 \right\} (\text{kJ/kg} \, \text{K}) \tag{A115}$$

 $c_p(t_0)$, $a_t(w)$ and $b_t(w)$ are described below:

$$c_p(t_0) = a_w w^3 + b_w w^2 + c_w w + d_w$$
 is the specific heat at t_0 (A116)

$$a_t(w) = a_1 w^3 + a_2 w^2 + a_3 w + a_4$$
 (A117)

$$b_t(w) = b_1 w^3 + b_2 w^2 + b_3 w + b_4 (A118)$$

where t is the temperature in ${}^{\circ}$ C, t_0 is 20 ${}^{\circ}$ C and w is the ratio of salt in the solution (kg/kg). The constants needed in the equations can be found in Table A54:

Table A54. Coefficients of the CH₃OH-ZnBr₂ specific heat equation.

a_{w}	2.62×10^{-1}	a_1	1.15×10^{-2}	b_1	-1.00×10^{-4}
$b_{\mathbf{w}}$	-1.02×10^{0}	a_2	-2.46×10^{-2}	b_2	2.40×10^{-4}
$c_{\mathbf{w}}$	2.69×10^{-1}	\mathbf{a}_3	2.19×10^{-2}	b_3	-1.74×10^{-4}
d _w	5.35×10^{-1}	a_4	-6.48×10^{-3}	b_4	4.57×10^{-5}

Enthalpy

The enthalpy (h) of the solution methanol-zinc bromide be calculated using the following equation:

$$h = c_p \cdot (T - 298.15) + h_m(kJ/kg)$$
(A119)

where T is the temperature in K, h_m is the integral enthalpy of mixing measured at 298.15 K and c_p is the specific heat of the solution at the given temperature and salt%.

In order to obtain the enthalpy of the solution, firstly the enthalpy of mixing needs to be calculated using the following equation [40]:

$$h_{\rm m} = \sum_{i=0}^{6} G_{\rm n} x^{\rm n} (kJ/kg)$$
 (A120)

where x is the absorbent concentration in%.

Values of the constant G_n are shown in Table A55:

Table A55. Coefficients of the CH₃OH-ZnBr₂ enthalpy equation.

n	G _n	n	G _n
0	1.88×10^{1}	4	8.91×10^{-4}
1	4.49×10^{0}	5	-1.15×10^{-5}
2	5.84×10^{-1}	6	5.58×10^{-8}
3	-3.37×10^{-2}		

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Density

The density (ρ) of the solution methanol-zinc bromide can be calculated using the following equation [40]:

$$\rho = \sum_{n=0}^{5} x^{n} \left(A_{n} + B_{n} T + C_{n} T^{2} \right) (kg/m^{3})$$
 (A121)

where T is the temperature in K and x is the salt concentration of the solution in%.

The given correlation can be used in the temperature range between 278.15 and 333.15 K and in the salt concentration range between 5.9 and 59.8%.

The constants needed in the equations can be found in Table A56:

Table A56. Coefficients of the CH₃OH-ZnBr₂ density equation.

n	A	В	С
0	1443.15	-3.28956	0.003746
1	-99.6888	0.659735	-0.0010617
2	10.8756	-0.0669845	0.000102403
3	-0.10843	0.00252739	-3.84077×10^{-6}
4	0.00654907	-4.01314×10^{-5}	6.03165×10^{-8}
5	-3.74906×10^{-5}	2.277×10^{-7}	-3.37872×10^{-10}

Saturated Pressure

The saturation vapour pressure (p_{sat}) of the solution methanol-zinc bromide can be calculated with the following equation [40]:

$$\log p_{\text{sat}} = \sum_{n=0}^{2} A_n x^n + \frac{1}{t + 230} \sum_{n=0}^{2} B_n x^n - 0.874792$$
 (A122)

where p_{sat} is the saturated pressure in kPa, t is the temperature in $^{\circ}C$ and x is the salt concentration of the solution in%.

The values of the constants A_n and B_n for temperatures between 20 and 60 $^{\circ}$ C are presented in Tables A57 and A58.

• For salt concentration range of 0–50%:

Table A57. Coefficients of the CH₃OH-ZnBr₂ saturated pressure equation.

n	$\mathbf{A}_{\mathbf{n}}$	B _n
0	7.94×10^{0}	1.48×10^{3}
1	4.07×10^{-4}	2.48×10^{-1}
2	-7.57×10^{-5}	-7.63×10^{-3}

• For salt concentration range of 50–70%:

Table A58. Coefficients of the CH₃OH-ZnBr₂ saturated pressure equation.

n	A _n	B _n
0	5.08×10^{0}	1.66×10^{3}
1	1.12×10^{-1}	-5.97×10^{0}
2	-1.20×10^{-3}	4.77×10^{-2}

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