

Hybrid Solid Oxide Fuel Cell/Gas Turbine Model Development for Electric Aviation

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Simulation Package

Bryan Research & Engineering's ProMax 5.0 is a chemical process simulation package that was used to model this hybrid SOFC-GT aviation power system. It is built on top of Microsoft Visio and Excel, giving it a familiar user interface and lending to its ease of use. ProMax is typically used in the upstream (production), midstream (gas processing and conditioning, cryogenic separation, etc.), and downstream (crude oil refining) sectors of the oil and gas industry. Within the last two years, BR&E has expanded ProMax's application in Sustainable Hydrogen Technologies and Carbon Capture Storage/Utilization by developing prebuilt models and classes covering steam methane reforming (SMR), water-gas shift (WGS) optimization, CO₂ removal for compression and sequestration, ammonia production, ammonia cracking and membrane separation, and electrolysis with proton exchange membrane (PEM) fuel cells for energy storage. The model outlined below contains the first SOFC model built in ProMax, to date.

Detailed Model Development

1. Top Level Inputs and Key Features

The first top level inputs needed are the Equation of State (EOS) and component definitions. These are specified in the "Active Environment" window found in the "General" section within the ProMax tab.

While a large selection of general and specialized EOSs are available, the main two options for this type of model are either **Peng-Robinson** or **SRK**.

Once the EOS is defined, the user clicks into the "Components" tab in the same window to specify the chemical species used in the model.

Table S1. Top level inputs.

| <u>Parameter</u> | <u>Value</u> |
|---------------------|--|
| Equation of State | Peng-Robinson |
| Chemical Components | n-Dodecane (simple jet fuel surrogate) CH ₄ ; H ₂ ; CO (fuel reforming products) CO ₂ ; H ₂ O (SOFC and combustion products) O ₂ ; N ₂ (simplified air surrogate) |

Jet fuels are typically made from mixtures of 40+ hydrocarbon components that combine to produce fuel with desired C:H ratios and LHV-values. Jet-A, for instance, has a large subset of hydrocarbon components that produce a C:H ratio of 12:23 and typically has an LHV of 18,500 Btu/lb [43,031 kJ/kg]. Simplified jet fuel surrogate streams can be created by mixing hydrocarbons together and using "Simple Solvers" to vary

composition/component flow rates until a desired C:H and LHV combination are achieved. These solvers can be added to virtually any process stream value and serve as a key feature in this model.

To add a solver, right click on any input value within a process stream and choose the “Create Simple Solver...” option. The user then paths in variables needed and writes in the function ProMax will use to close in on the necessary value. See the following example where a solver was used to change the molar flowrate of the “m-Xylene” process stream until the resultant jet fuel stream has the 12:23 ratio required of Jet-A.

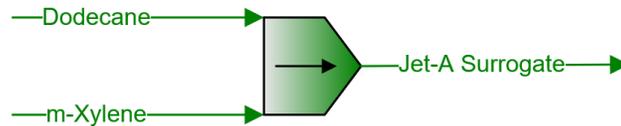


Figure S1. ProMax process stream setup for Jet-A Surrogate model.

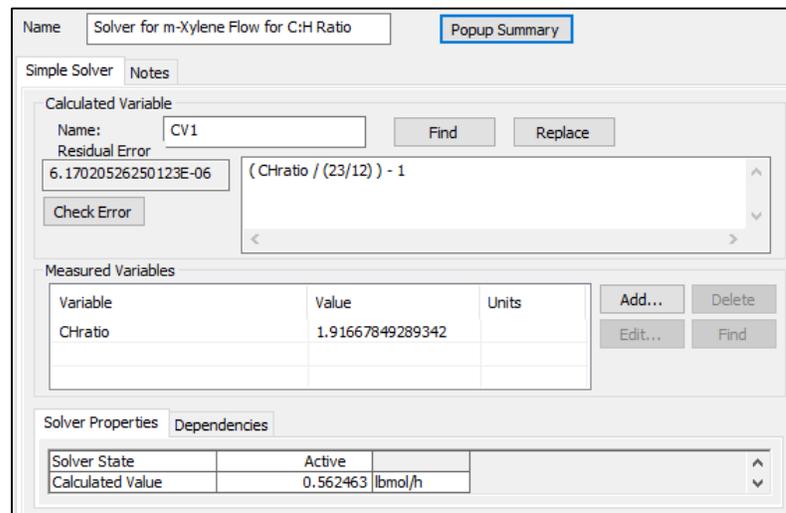


Figure S2. ProMax Simple Solver window with user-defined equation for C:H ratio.

This solver was used in tandem with Promax’s scenario tool to analyze LHV values when various BTEX components were mixed into a 1 mol/s n-Dodecane stream while achieving the targeted 12:23 Jet-A ratio. The results were as follows:

Table S2. Jet-A Surrogate candidates.

| BTEX Component | Molar Flowrate (lbmol/hr) | LHV (Btu/lb) |
|-----------------------|----------------------------------|---------------------|
| Benzene | 0.5453 | 18,621.5 |
| Toluene | 0.5538 | 18,607.5 |
| Ethylbenzene | 0.5624 | 18,607.7 |
| o-Xylene | 0.5624 | 18,594.9 |
| m-Xylene | 0.5624 | 18,546.4 |
| p-Xylene | 0.5624 | 18,547.9 |

Here, ProMax solver identified the molar ratio of n-dodecane and m-xylene to act as a Jet-A surrogate that meets the C:H specifications with a slightly elevated LHV. A third hydrocarbon component could be added to the model with cascading solvers to close in on the exact LHV without changing the C:H ratio. Examples like this show how and why ProMax solvers are integral to the simulation environment.

2. Hybrid SOFC/GT Flowsheet and Unit Specifications

When building out a process in ProMax, users can opt to input required process stream properties and unit operation values as each stream and block are added, or they can specify values once the entire flowsheet is built. In either case, the following highlights the values and specifications for each unit included in this model.

Process Inputs

Fuel Feed:

- For model simplification, pure n-dodecane was used as the jet fuel surrogate in this study. This made it easier to validate the jet fuel steam reformer as n-dodecane reforming has been cited in open literature.
- Temperature = 25°C
- Pressure should be set to match what the reformer and SOFC are operating at. For aerospace modeling, the operating pressure range is defined by current altitude and the air compression ratio.

This pressure should not prove critical since a physical system would likely use an atomizer to efficiently disperse fuel into the reformer. This fact combined with the small mass flow rates meant model pressures simply needed to be high enough to not drop the pressure of the recycled anode gas.

- A solver was used to change the fuel flow rate to achieve the desired fuel utilization (U_f) in the SOFC based on Eq[14] from the main text.

The screenshot displays the configuration for a solver named "Solver for Fuel Flow to Get Uf". It includes a "Calculated Variable" section where the name is "CV1" and the residual error is $7.99505261994682 \times 10^{-8}$. The equation for the residual error is
$$\frac{(((H2_{in} + CO_{in} + CH4_{in}) - (H2_{out} + CO_{out} + CH4_{out})) / (H2_{in} + CO_{in} + CH4_{in})) / (U_f/100) - 1}{}$$
. The "Measured Variables" table is as follows:

| Variable | Value | Units |
|----------|-------------------|-------|
| Uf | 75 | % |
| CH4in | 0.438470233769... | mol/s |
| H2in | 2.29062893141998 | mol/s |
| COin | 1.56284619643665 | mol/s |

The "Solver Properties" section shows the solver is "Active", the "Calculated Value" is 22.4216 g/s, and the "Error" is 7.99505e-08.

Figure S3. Fuel Feed solver used to achieve specified U_f – ‘in’ vs ‘out’ is relative to SOFC reactor.

Steam:

- This stream was only used to initially charge the system with the water required in the reforming process. There is more than enough steam produced in the SOFC anode for n-dodecane reforming, so recycling enough of the anode exhaust allows users to zero-out this process stream.
- Temperature was arbitrary and was set to 700°C to ensure 100% vapor when first getting the simulation to converge.
- Pressure was set to reflect what the reformer was operating at for initial runs.
- A solver was used at startup to target a specific O:C ratio in the reformer. An O:C operating range of 1.8 – 3.0 was chosen based on results from literature. This solver was set to “Disabled” after initial convergence.

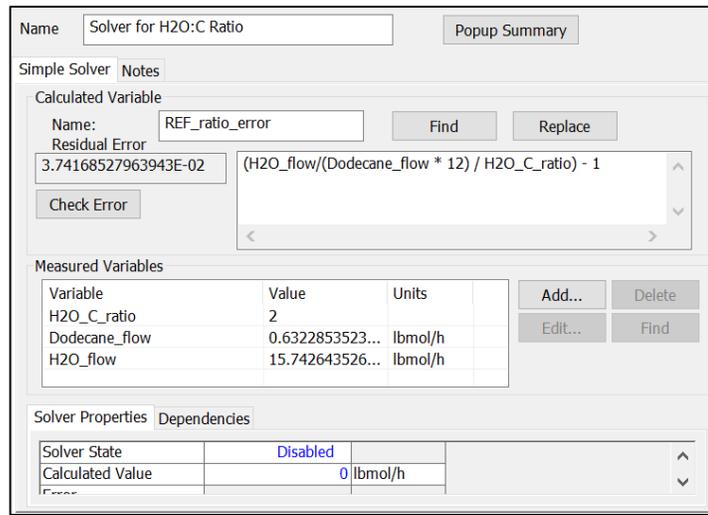


Figure S4. Steam solver used to get a first pass model convergence within desired O:C range.

Outside Air:

- A simplified air composition of 79 mol% N₂ and 21 mol% O₂ was used.
- Temperature and pressure of this stream was set to reflect ambient conditions for commercial aircraft flight path altitudes. The data shown in this paper was based on a 36,000' – cruise altitude – condition.

Table S3. Ambient air conditions as a function of altitude.

| <u>Altitude (ft)</u> | <u>Temperature (°C)</u> | <u>psia</u> | <u>atm</u> |
|----------------------|-------------------------|-------------|------------|
| 0 | 15 | 14.7 | 1.00 |
| 8,000 | -0.8 | 10.92 | 0.74 |
| 30,000 | -44.4 | 4.364 | 0.30 |
| 36,000 | -56.3 | 3.297 | 0.22 |
| 42,000 | -56.5 | 2.471 | 0.17 |

- A solver was used to change the air flow rate needed to achieve an SOFC current density of 1.25 A/cm² (1,250 mA/cm²) for all runs.

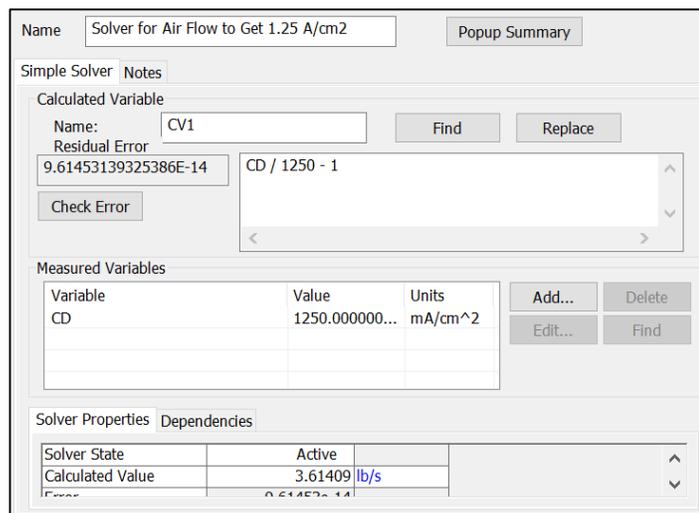


Figure S5. Outside Air solver used to get flow rate required for target SOFC current density.

Fuel Spray:

- This process stream was included to provide additional chemical energy upstream of the combustor for two main purposes: 1) many turbines have turbine inlet temperature (TIT) requirements for efficient operation and 2) there must be sufficient energy remaining in the process stream after expansion to satisfy the Second Law of Thermodynamics in the cathode air heat exchanger.

It should be noted that any amount of additional fuel requirement drastically decreases total system efficiency.

- Temperature and pressure were set to reflect the Fuel Feed stream properties since it would be drawn from the same fuel tank.
- A solver was used to change this flowrate to meet either a desired TIT or TET (turbine exit temperature).

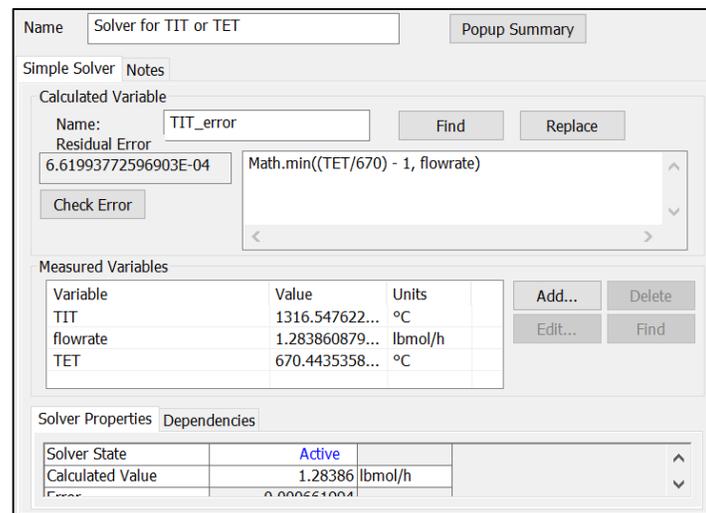


Figure S6. Fuel Spray solver used to get flow rate required for target TIT or TET.

ProMax Blocks (Units)

External Reformer (C12 REF):

- Reactor type = Gibbs Minimization
- Gibbs Set = General
- Pressure Drop = 0 psi
- Temp Change = 0 °C
- Linear Constraint set on “Dodecane” with a Change of 0.01

This limited the n-dodecane conversion to 99%. Literature did reference conditions in which 100% conversion was achieved in steam reforming, but we did not want to make that assumption in this study.

If a multi-component jet fuel surrogate was used, a method would need to be used to limit the combined conversion of all sub-components to the 99% set for n-dodecane.

SOFC:

- Reactor type = Gibbs Minimization
- Gibbs Set = General
- Pressure Drop = 0 psi
- Temp Change – the average operating SOFC temperature is set on the stream leaving the reactor block (800°C for the case shown), therefore the temperature change field is not accessible in this reactor block once that specification was set.

- Linear Constraint set on “O2” with a Simple Specifier set in the Change field.

Simple Specifiers are like Solvers, but they do not rely on methods to converge on a value. They reference static values and use equations to immediately determine and assign a value.

This Specifier uses the desired air utilization user-value to set the O2 conversion in the SOFC.

The screenshot shows a software interface for defining a simple specifier. The main window is titled 'Specifier for SOFC O2 Conversion'. It has two tabs: 'Simple Specifier' (selected) and 'Notes'. Under 'Simple Specifier', there is a 'Specified Variable' section with a 'Value = 0.81' field and a dropdown menu. Below this is a text area containing the equation '1 - (U_air/100)'. To the left of the text area are buttons for 'Find', 'Replace', 'Check Error', 'Calculate', and 'Active'. Below the text area is an 'Independent Variables' table with columns for 'Variable', 'Value', and 'Units'. The table contains one row for 'U_air' with a value of 19 and units of '%'. To the right of the table are buttons for 'Add...', 'Delete', 'Edit...', and 'Find'.

| Variable | Value | Units |
|----------|-------|-------|
| U_air | 19 | % |
| | | |
| | | |
| | | |
| | | |

Figure S7. Oxygen Conversion specifier used to operate the SOFC at the desired air utilization.

Combustor:

- Reactor Type = Gibbs Minimization
- Gibbs Set = Burner
- Pressure Drop = 0 psi
- By not connecting an energy stream to the combustor, ProMax assumes it will operate in an adiabatic setting and convert all exothermic energy to sensible heat, increasing the temperature of the outlet process stream.
- Combustion analyses on the Fuel Spray and unrecycled anode exhaust (stream 2) showed an average of 3x the required O₂ for complete combustion depending on the U_f and U_{air}.

It is possible this ratio of air to combustible fuel causes a dilution and therefore hinders combustion, but the reported simulation assumed this was not the case.

Turbine:

- Adiabatic efficiency set to 81%.

This value came from the assumption that there would be two sets of blades in series – high and low pressure – each with efficiencies of 90%.

- TIT and TET could either float if a specific simulation case proved to have enough energy leaving the turbine – again, ensuring the 2nd Law of Thermodynamics is not violated in the CAHx – or they were controlled by the Fuel Spray flow solver.
- Exit pressure was back calculated from the plane exhaust and therefore becomes a function of ambient air pressure at a given altitude, condenser dP, and CAHx dP.

Compressor:

- Adiabatic efficiency set to 90%.
- Compression ratio would be static across the flight envelope.

For sensitivity and performance analyses, outlet pressure can be varied to see the effect that operating pressure has on the entire system.

Compression ratio should remain the same when comparing one altitude to another.

We set the compression ratio to 16 when comparing cases.

- Air mass flow rate through the compressor increases as altitude decreases since there is an inverse relationship between altitude and ambient air density.

Turbogenerator:

- This was an empty box on the flowsheet to provide a visual with the calculations performed in a User Value Set in the background.
- Turbine Duty (kW) were subtracted from Compressor Duty (kW) to get Net Available Power (kW). This was then multiplied by a generator efficiency to get the Turbogenerator electricity production (kW).
- Turbogenerator Efficiency set to 90% for all runs.

Heat Exchangers:

- CAHx

Double-sided heat exchanger with 3% dP on each process stream.

Used to preheat the Cathode Air to within a 250 – 50°C dT vs the specified SOFC operating temperature.

20°C Minimum End Approach Temperature on hot inlet vs cold outlet was used as a lowest acceptable case for plausible designs.

- HX1

Single-sided heat exchanger with 5% dP to simulate SOFC cathode pressure drop.

Used to convert SOFC Heat Generation to sensible heat added to the SOFC exhaust.

SOFC Heat Generation is the difference between the SOFC Duty and SOFC Power with 10% loss to environment assumption.

- REF Heat

Single-sided heat exchanger with a 3% dP.

Used to provide heat needed in the endothermic n-dodecane reforming process.

- CNDSR

Doubled-sided heat exchanger with 3% dP on each process stream.

Special consideration needed to ensure H₂O Recovery stream operates above the ice formation temperature.

Water Recovery:

- CNDSR heat exchanger combined with a 0 dP Flash unit to condense and separate water out of the plane exhaust.

- H₂O Recovery stream temperature should change with altitude to ensure operation above ice formation temperature.

“Degrees above Solids (Ice) Formation” can be calculated with the “Freeze Out, Hydrate, H₂O Dew Point” analysis in the Analyses tab within the H₂O Recovery process stream.

- H₂O Recovery pressure set to reflect ambient air pressures as a function of altitude, shown in Table S3.

3. ProMax User Value Sets

User Value Sets (UVSs) are generatable groups within which users can define properties or variables not available in ProMax. User values are commonly used in a few ways: 1) can be referenced by Simple Specifiers/Solvers in the flowsheet for a variety of reason (e.g. converging on process targets, setting multiple streams to the temperature/pressure, etc.), 2) can pull values from the flowsheet to perform background calculations, and 3) to

display process data in flowsheet property tables through the moniker builder. This model contained 5 UVSs in which all three of these functions were leveraged to create a user-friendly interface.

Process Values UVS:

- Reformer O:C Target used by the Steam process stream during startup and initial convergence.
- Reformer O:C used a Simple Specifier to pull in and display the actual O:C ratio at the end of each converged simulation.
- Cathode dP used to set the HX1 dP to 5%.
- Heat Exchanger dPs used to set all other heat exchangers dPs to 3%.
- Thermal Losses to Environment used to derate the sensible heat added to the cathode exhaust in HX1 by 10%.

SOFC Conversions UVS:

- CH4 Conversion used Simple Specifier to display CH4 single-pass conversion.
- H2 Conversion used Simple Specifier to display H2 single-pass conversion.
- CO Conversion used Simple Specifier to display CO single-pass conversion.
- Air Utilization used Simple Specifier to display achieved U_{air} .
- Fuel Utilization used Simple Specifier to display achieved U_f .

SOFC Stack and Electrochemistry UVS:

This UVS was too extensive to list out all values and info. It contained the U_f and U_{air} targets, physical SOFC stack sizes and configurations, internal electrochemical static values, voltage and current calculations, and stack power and efficiency calculations.

| Name | Units | Parameter | Enforce Bounds | Lower Bound | Upper Bound |
|---------------------------------|---------------------|------------|--------------------------|-------------|-------------|
| Fuel Utilization (U_f) | % | 75 | <input type="checkbox"/> | | |
| Air Utilization | % | 19 | <input type="checkbox"/> | | |
| Cell Active Area | cm ² | 500 | <input type="checkbox"/> | | |
| # Cells per Stack | | 200 | <input type="checkbox"/> | | |
| # Stacks | | 7 | <input type="checkbox"/> | | |
| O2 Consumption per Stack | mol/s | 0.323883 | <input type="checkbox"/> | | |
| O2 Consumption per Cell | mol/s | 0.00161942 | <input type="checkbox"/> | | |
| Stack Current | A | 625 | <input type="checkbox"/> | | |
| Total Current | A | 4375 | <input type="checkbox"/> | | |
| Current Density | mA/cm ² | 1250 | <input type="checkbox"/> | | |
| Internal Current Density | mA/cm ² | 2 | <input type="checkbox"/> | | |
| Exchange Current Density | mA/cm ² | 840 | <input type="checkbox"/> | | |
| Limiting Current Density | mA/cm ² | 2700 | <input type="checkbox"/> | | |
| r (total cell resistance) | Ohm*cm ² | 0.071 | <input type="checkbox"/> | | |
| alpha (charge transfer coef.) | | 1.67 | <input type="checkbox"/> | | |
| Gibbs Formation of H2O | J/mol | -188790 | <input type="checkbox"/> | | |
| V_nernst | V | 0.934753 | <input type="checkbox"/> | | |
| V_activation | V | 0.01105 | <input type="checkbox"/> | | |
| V_ohmic | V | 0.088892 | <input type="checkbox"/> | | |
| V_concentration | V | 0.0288097 | <input type="checkbox"/> | | |
| V_operating | V | 0.803887 | <input type="checkbox"/> | | |
| Stack Voltage | V | 160.777 | <input type="checkbox"/> | | |
| SOFC Power | kW | 703.401 | <input type="checkbox"/> | | |
| SOFC Heat Generation | kW | 33.0821 | <input type="checkbox"/> | | |
| SOFC Overall Efficiency | % | 71.6311 | <input type="checkbox"/> | | |
| SOFC Electrochemical Efficiency | % | 86 | <input type="checkbox"/> | | |

Figure S8. SOFC Stack and Electrochemistry UVS; blue cells contain Simple Specifiers for background calculations.

Turbomachinery Calculations UVS:

- Turbogenerator Efficiency set to 90% and used to calculate generator electricity.

-
- Turbine Power Generated used Simple Specifier to pull in TRBN Duty.
 - Compressor Power Consumed used Simple Specifier to pull in COMP Duty.
 - Available Power used Simple Specifier to calculate difference between turbine and compressor powers.
 - Turbogenerator Power used Simple Specifier to calculate electricity multiplying available power to turbogenerator efficiency.
- System Power and Efficiency UVS:
- Hybrid System Power used Simple Specifier to calculate combine generated electricity.
 - Hybrid System Efficiency used Simple Specifier to calculate combined system efficiency based on generated electricity and total chemical energy added to the system.

Table S4. ProMax n-Dodecane External Reformer and SOFC inlet and outlet process streams.**ProMax Process Stream Values**

| Process Streams | | REFin | SynGas | Cathode Air | Anode | Cath Ex |
|-----------------------------|---------------------|------------|------------|-------------|---------------|-----------|
| Composition | Status: | Solved | Solved | Solved | Solved | Solved |
| Phase: Total | From Block: | MIX-100 | C12 REF | CAHX | Div-1 | HX1 |
| | To Block: | C12 REF | MIX-101 | MIX-101 | Recycle Split | MIX-102 |
| Mole Fraction | | % | % | % | % | % |
| Dodecane | | 1.7017 | 0.0136 | 0* | 0.0121 | 0 |
| CH4 | | 0.0001 | 6.3143 | 0* | 0.0001 | 0 |
| H2 | | 8.6650 | 22.7928 | 0* | 8.8078 | 0 |
| CO | | 6.4066 | 14.0291 | 0* | 6.5119 | 0 |
| CO2 | | 40.7766 | 33.7118 | 0* | 41.4823 | 0 |
| H2O | | 42.4500 | 23.1384 | 0* | 43.1858 | 0 |
| O2 | | 0 | 0 | 21* | 0 | 16.6227 |
| N2 | | 0 | 0 | 79* | 0 | 83.3773 |
| Molar Flow | | lbmol/h | lbmol/h | lbmol/h | lbmol/h | lbmol/h |
| Dodecane | | 0.9392 | 0.0094 | 0* | 0.0094 | 0 |
| CH4 | | 0.0001 | 4.3453 | 0* | 0.0001 | 0 |
| H2 | | 4.7824 | 15.6852 | 0* | 6.8266 | 0 |
| CO | | 3.5359 | 9.6543 | 0* | 5.0472 | 0 |
| CO2 | | 22.5055 | 23.1993 | 0* | 32.1516 | 0 |
| H2O | | 23.4291 | 15.9230 | 0* | 33.4720 | 0 |
| O2 | | 0 | 0 | 61.6931* | 0 | 46.2698 |
| N2 | | 0 | 0 | 232.084* | 0 | 232.084 |
| Properties | | | | | | |
| | | Units | | | | |
| Temperature | °F | 1148.86 | 1148.86 | 1202* | 1382 | 1510.38 |
| Pressure | psig | 29.3919 | 29.3919 | 31.6330* | 29.3919 | 29.3166* |
| Mole Fraction Vapor | % | 100 | 100 | 100 | 100 | 100 |
| Mole Fraction Light Liquid | % | 0 | 0 | 0 | 0 | 0 |
| Molecular Weight | lb/lbmol | 30.4608 | 24.4301 | 28.8503 | 28.0584 | 28.6759 |
| Mass Density | lb/ft ³ | 0.0777881 | 0.0623630 | 0.0748829 | 0.0625761 | 0.0596508 |
| Molar Flow | lbmol/h | 55.1921 | 68.8165 | 293.777 | 77.5070 | 278.353 |
| Mass Flow | lb/h | 1681.19 | 1681.19 | 8475.56 | 2174.72 | 7982.03 |
| Vapor Volumetric Flow | ft ³ /h | 21612.5 | 26958.2 | 113184 | 34753.2 | 133813 |
| Liquid Volumetric Flow | gpm | 2694.54 | 3361.02 | 14111.3 | 4332.87 | 16683.1 |
| Std Vapor Volumetric Flow | MMSCFD | 0.502668 | 0.626754 | 2.67561 | 0.705904 | 2.53514 |
| Std Liquid Volumetric Flow | sgpm | 4.21232 | 5.11225 | 19.5623 | 5.41508 | 18.6986 |
| Compressibility | | 1.00013 | 1.00052 | 1.00095 | 1.00023 | 1.00077 |
| Specific Gravity | | 1.05173 | 0.843508 | 0.996127 | 0.968783 | 0.990104 |
| Enthalpy | Btu/h | -5.867E+06 | -5.503E+06 | 2.424E+06 | -8.180E+06 | 2.970E+06 |
| Mass Enthalpy | Btu/lb | -3489.72 | -3273.06 | 286.019 | -3761.55 | 372.083 |
| Mass Cp | Btu/(lb*°F) | 0.420278 | 0.419152 | 0.270519 | 0.388689 | 0.279584 |
| Ideal Gas CpCv Ratio | | 1.18385 | 1.24080 | 1.34136 | 1.22282 | 1.32927 |
| Dynamic Viscosity | cP | 0.0357026 | 0.0359852 | 0.0390885 | 0.0409182 | 0.0432815 |
| Kinematic Viscosity | cSt | 28.6527 | 36.0227 | 32.5871 | 40.8214 | 45.2966 |
| Thermal Conductivity | Btu/(h*ft*°F) | 0.0454580 | 0.0619019 | 0.0366208 | 0.0531900 | 0.0418510 |
| Net Ideal Gas Heating Value | Btu/ft ³ | 190.321 | 165.986 | 0 | 46.0361 | 0 |
| Net Liquid Heating Value | Btu/lb | 2045.76 | 2351.91 | 0 | 279.959 | 0 |

| | | | | | | |
|-------------------------------|---------------------|---------|---------|---|---------|---|
| Gross Ideal Gas Heating Value | Btu/ft ³ | 227.158 | 195.533 | 0 | 72.2725 | 0 |
| Gross Liquid Heating Value | Btu/lb | 2504.77 | 2810.88 | 0 | 634.801 | 0 |
