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Article Characteristics of the Bright Band Based on Quasi-Vertical Profiles of Polarimetric Observations from an S-Band Weather Radar Network

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Abstract: Bright band (BB) characteristics obtained via dual-polarization weather radars elucidate thermodynamic and microphysical processes within precipitation systems. This study identified BB using morphological features from quasi-vertical profiles (QVPs) of polarimetric observations, and their geometric, thermodynamic, and polarimetric characteristics were statistically examined using nine operational S-band weather radars in South Korea. For comparable analysis among weather radars in the network, the calibration biases in reflectivity (Z_H) and differential reflectivity (Z_{DR}) were corrected based on self-consistency. The cross-correlation coefficient (ρ_{HV}) bias in the weak echo regions was corrected using the signal-to-noise ratio (SNR). First, we analyzed the heights of BBPEAK derived from the Z_H as a function of season and compared the heights of BBPEAK derived from the Z_H , Z_{DR} , and ρ_{HV} . The heights of BB_{PEAK} were highest in the summer season when the surface temperature was high. However, they showed distinct differences depending on the location (e.g., latitude) within the radar network, even in the same season. The height where the size of melting particles was at a maximum (BB_{PEAK} from the Z_H) was above that where the oblateness of these particles maximized (BBPEAK from ZDR). The height at which the inhomogeneity of hydometeors was at maximum (BB_{PEAK} from the ρ_{HV}) was also below that of BB_{PEAK} from the Z_H. Second, BB thickness and relative position of BB_{PEAK} were investigated to characterize the geometric structure of the BBs. The BB thickness increased as the Z_H at BB_{BOTTOM} increased, which indicated that large snowflakes melt more slowly than small snowflakes. The geometrical structure of the BBs was asymmetric, since the melting particles spent more time forming the thin shell of meltwater around them, and they rapidly collapsed to form a raindrop at the final stage of melting. Third, the heights of BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} were compared with the zero-isotherm heights. The dry-temperature zero-isotherm heights were between BB_{TOP} and BB_{BOTTOM}, while the wet-bulb temperature zero-isotherm heights were close to the height of BBPEAK. Finally, we examined the polarimetric observations to understand the involved microphysical processes. The correlation among Z_H at BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} was high (>0.94), and the Z_{DR} at BB_{BOTTOM} was high when the BB's intensity was strong. This proved that the size and concentration of snowflakes above the BB influence the size and concentration of raindrops below the BB. There was no depression in the ρ_{HV} for a weak BB. Finally, the mean profile of the Z_H and Z_{DR} depended on the Z_H at BB_{BOTTOM}. In conclusion, the growth process of snowflakes above the BB controls polarimetric observations of BB.

Keywords: quasi-vertical profile; S-band dual-polarization radar; bright band; melting layer; microphysical process

1. Introduction

When falling snowflakes pass through the zero-isotherm layers into the warmer air, they melt and collapse to form raindrops, causing an increase in radar reflectivity (known as the bright band, hereafter BB). The reflectivity (Z_H) increases owing to the increase in the dielectric constant. Afterwards, the Z_H decreases upon the formation of raindrops, owing to the decrease in the size and number concentration of snowflakes caused by the increase in fall velocity [1,2]. The overestimation in Z_H causes a significant error in radar rainfall estimates under the BB region. The identification of BB and correction of related errors are necessary for accurate estimations of precipitation [3–5]. The study of the vertical structure of the precipitation system associated with the melting layer and its characteristic analysis using remote sensing instruments is essential to understand cloud physics and rain microphysics. Weather radar can provide crucial information on melting layers with high spatiotemporal resolution. Therefore, detection and characterization of the BB using weather radar is one of the primary keys for understanding the microphysical processes related to the vertical structure of precipitation.

Most single-polarimetric techniques have identified the BB (i.e., peak, top, and bottom) based on a geometric feature from the vertical profile of $Z_{\rm H}$ (VPR) [1,6–10]. The gradient of VPR has been commonly used to define the boundary of BB. Klaassen [11] and White et al. [12] used the change in radial velocity when snowflakes turn into raindrops as they pass through the melting layer to identify the BB. Dual-polarization radar can provide information on the size, shape, and phase of hydrometeors, resulting in improved BB detection [13–17]. Ryzhkov and Zrnić [13] showed that polarimetric signatures pronounce the presence of BB. Brandes and Ikeda [14] identified BB by matching observed and modelled profiles of polarimetric observations. Giangrande et al. [16] proposed thresholds for $Z_{\rm H}$, the differential reflectivity ($Z_{\rm DR}$), and the cross-correlation coefficient ($\rho_{\rm HV}$) to detect top and bottom boundaries of BB in an operational environment. Boodoo et al. [18] modified the technique developed by Giangrande et al. [16] for a C-band radar in southern Ontario, Canada. The top of the BB effectively matched the 0 °C wet-bulb temperature layer. Illingworth and Thompson [19] showed that the linear depolarization ratio (LDR) was valuable for identifying BB and correcting an increase in $Z_{\rm H}$ due to BB. Hall et al. (2015) developed a fuzzy logic-based BB detection technique using $Z_{\rm H}$, $Z_{\rm DR}$, $\rho_{\rm HV}$, and LDR.

Fabry and Zawadzki [1] analyzed the vertical structure of BB revealed by X-band vertically pointing radar and wind profiler. The intensity of BB depends on variations in the refractive index, shape, and density of hydrometeors. Zawadzki [20] developed a BB model that showed that dense particles reduce the difference in Z_H at the peak height of the BB and in the rain region. Wolfensberger et al. [21] analyzed the characteristics of BB using the range-height indicator (RHI) scan mode at various climatic regions (i.e., South of France; Swiss Alps and plateau; and Iowa, USA). The distribution of polarimetric observations within the BB was similar regardless of the season and climatic regions. They also showed that the thickness of BB is highly related to the presence of rimed particles, the fall velocity of the hydrometeors, and BB intensity.

Recently, quasi-vertical profiles (QVPs) of polarimetric observations (described in more detail in Section 3) were used to investigate the vertical structure and microphysical processes of the precipitation system [22–25]. Kumjian et al. [22] first used QVP to detect refreezing signals of precipitation during winter storms. According to Ryzhkov et al. [24], QVP is a useful tool for the examination of microphysical processes resulting in precipitation on the surface and aids in the determination of the growth process of snowflakes. Kumjian and Lombardo [23] analyzed the microphysical and dynamic characteristics of winter snowstorms. They found that an increase in differential reflectivity (Z_{DR}) represented the initial stage of planar crystal growth, and an increase in the specific differential phase (K_{DP}) indicated the high number concentrations of planar crystals. The supersaturation caused by the ascent boosts the depositional growth and raises the potential of an increase in K_{DP} . Trömel et al. [26] showed the potential of ground precipitation nowcasting by identifying microphysical processes of stratiform snowfall storms. The K_{DP} increase in the dendritic growth layer (DGL, between -10 and -20 °C) exhibited a very high correlation with rainfall on the ground after half an hour. Griffin et al. [27] detected

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BB and analyzed the microphysical processes associated with BB and DGL for stratiform precipitation in winter. Using the QVPs of polarimetric observations, they identified a weak BB (Z_H of < 20 dBZ) whose detection failed when using the vertical profile of Z_H only. They also compared polarimetric observations above, within, and below the BB using QVPs for the first time at the S band.

In this study, we identified BB using the QVPs of polarimetric observations obtained from nine S-band dual-polarization radars operated by the Korea Meteorological Administration (KMA). For the analysis of BB characteristics, geometric features (including heights of the BB peak, top, and bottom at QVPs) were analyzed statistically, and then compared to the height of the 0 °C isotherm. Finally, the characteristics of polarimetric observations at the top, peak, and bottom of the BB were examined to determine the microphysical processes related to the BB.

2. Materials and Methods

2.1. Materials and Data

The KMA has operated a nationwide weather radar network composed of 10 S-band weather radars since 2008 and sequentially replaced all radars of the network with S-band dual-polarization radars during the period from 2014 to 2019. Figure 1 shows the deployment of the KMA S-band dual-polarization weather radar. The replacement began with the BRI radar at the northwestern island in 2014 and ended with the GNG radar at the northeastern coast in November 2019. We used a total of nine weather radars, except for the GNG radar, to analyze the characteristics of the BB from March to November 2019. Table 1 shows the volumetric scan strategies of the weather radar in the KMA network. All strategies consisted of nine elevation angles, including a wind profiling mode of 15° and were repeated every 5 min. Notably, several radars (i.e., KWK, MYN, and PSN) installed at a relatively high altitude (>600 m mean sea level (MSL)) employed a negative (-) elevation as the lowest elevation angle. The elevation angles for the lowest scan were determined based on a radar beam blockage simulation for standard beam propagation using the digital elevation model with a horizontal resolution of 1 arc second. The radar transmits a long pulse with a width of 2 µs at low elevation angles (less than 3°) to enhance the detectability of weak low-level echoes, such as winter snowstorms, whereas a short pulse of 1 µs pulse width is used at higher elevation angles (>3°) to increase the Nyquist velocity using high pulse repetition frequency (PRF). This configuration of the pulse length is based on the sensitivity test by Lee et al. [28]. They found that a longer pulse length (i.e., $2 \mu s$) improved radar sensitivity and increased the spatial extent of the precipitation echo for radar reflectivity and all dual-polarimetric observations. The azimuthal and radial resolutions were 1.0° and 250 m, regardless of the elevation angle. The BB was identified using QVPs of polarimetric observations at the highest elevation angle of 15.0°.

To analyze the thermodynamic characteristics of BB, three-dimensional dry-bulb temperature (T), dew point temperature (T_d) and wet-bulb temperature (T_w) data from three-dimensional atmospheric fields (T, T_d, and pressure) were generated by multi-quadric interpolation using observational data and very short-range data assimilation and prediction systems (VDAPS) [29] were used every 5 min. The horizontal resolution of three-dimensional atmospheric field data was 4 km, and the vertical resolution was 100 m at altitudes of 0–2 km and 200 m at altitudes of 2–10 km. The three-dimensional data consisted of $60 \times 257 \times 257$ (10 km × 1024 km × 1024 km) grids. The temperature data was interpolated to the same vertical resolution of the QVPs (20 m).



Figure 1. Deployment of the Korea Meteorological Administration (KMA) S-band dual-polarization weather radar network. The 10 circles indicate the 240 km radius coverage of the radar.

Radar	r Elevation Angle (°)								
GDK	-0.40	0.01	0.31	0.80	1.41	2.50	4.20	7.11	15.01
BRI	0.10	0.42	0.81	1.41	2.20	3.41	5.10	7.61	15.01
KWK	-0.19	0.00	0.30	0.81	1.50	2.60	4.40	7.30	15.01
MYN	-0.80	-0.39	0.01	0.41	0.91	1.91	3.60	7.00	15.01
KSN	0.00	0.30	0.70	1.30	2.10	3.21	5.00	7.61	15.01
PSN	-0.09	0.20	0.60	1.10	1.81	3.00	4.71	7.40	15.01
JNI	-0.09	0.20	0.60	1.10	1.81	3.00	4.71	7.42	15.02
SSP	0.20	0.50	1.01	1.60	2.41	3.50	5.20	7.60	15.00
GSN	0.20	0.50	1.01	1.60	2.41	3.50	5.20	7.60	15.01

Table 1. Scan strategy of KMA operational S-band dual-polarization radars.

2.2. Methodology

2.2.1. Construction of the QVPs

The QVPs were obtained by azimuthal averaging individual polarimetric observations at each range gate and for the highest elevation angle (15°). According to Ryzhkov et al. [24], the QVP at an elevation angle between 10 and 20° can reduce horizontal inhomogeneity. The QVP provides a stable vertical structure of the precipitation system for the BB identification, where Z_H and Z_{DR} increase and ρ_{HV} decreases.

Two kinds of corrections were required for all KMA radars before constructing the QVPs of polarimetric observations as follows: (1) the calibration biases in the power-based polarimetric measurements (i.e., Z_H and Z_{DR}) and (2) the correction of ρ_{HV} in the low SNR area. First, the calibration biases in Z_H and Z_{DR} lead to an unsuitable identification of the BB, and the different calibration biases among radars within the network resulted in a misunderstanding of the spatial and temporal statistics of BB. In this study, the Z_H bias was corrected based on the self-consistency principle between Z_H and differential phase (Φ_{DP}) [30,31]. The Z_{DR} bias was calibrated by comparing the empirical relationship between Z_H and Z_{DR} obtained from the drop size distribution of a two-dimensional video disdrometer

(2DVD) to the Z_{H} - Z_{DR} distribution of polarimetric measurements. Kwon et al. [31] described these two procedures in detail.

The noise caused by a radar receiver, waveguide, and antenna affects the quality of the polarimetric observations, even if the radar is properly calibrated [32]. The ρ_{HV} is biased in the low signal-to-noise ratio (SNR) areas. Meteorological echoes with a ρ_{HV} less than 0.98 are observed due to the bias related to the noise. The ρ_{HV} was corrected using the SNR as follows:

$$\rho_{\rm HV} = \rho_{\rm HV}^{(m)} \, (1 + 1/{\rm snr}) \tag{1}$$

where $\rho_{HV}^{(m)}$ and ρ_{HV} are the measured and corrected ρ_{HV} , respectively. The snr (=10^{0.1SNR(dB)}) is the SNR in linear units.

Radar observations included non-meteorological echoes. The regions with $\rho_{HV} < 0.7$, or with SNR < 10 dB, were removed to avoid contamination by non-meteorological echoes. The QVPs of polarimetric observations were constructed by obtaining the azimuthal average of Z_H , Z_{DR} , and ρ_{HV} . As the radar beam broadens, the QVP resolution is reduced at high altitudes. In this study, QVPs were converted to high resolution by interpolating them to a vertical resolution of 20 m. The QVPs of Z_H , Z_{DR} , and ρ_{HV} were used to analyze the characteristics of polarimetric observations at the top, peak, and bottom of the BB.

2.2.2. Detection of the Bright Band (BB)

Most BB detection algorithms apply the first and second derivatives of Z_H (dZ/dh and d²Z/dh²). However, local variations of Z_H can make the detection of the boundary of the BB challenging. A sharp curvature of Z_H is required for the detection of the top and bottom of the BB. The coordinate rotation method developed by Rico-Ramire and Cluckie [9] was used to detect the boundaries of the BB. This method is simple and has the advantage of reliably detecting the BB signature, The Z_H and Z_{DR} increase due to the increase in the hydrometeor dielectric constants and densities, and the ρ_{HV} decreases due to the diversity of the hydrometeor shapes, orientations, and densities. Before applying the coordinate rotation method, the ρ_{HV} was normalized to a value ranging between 0 and 100, and then converted to a new variable (new $\rho_{HV} = 100 - 100^* \rho_{HV}$), which increased in the BB as a result of this conversion.

The procedures for BB detection using the QVPs of the Z_{H} , Z_{DR} , and new ρ_{HV} were divided into the following two steps: (1) detection of the peak of the BB (BB_{PEAK}) and (2) detection of the top and bottom of the BB (BBTOP and BBBOTTOM) using the coordinate rotation method. BBPEAK was identified by calculating the first derivative of polarimetric observations. The first derivative was calculated from the difference in the polarimetric observations at a height of 60 m above and below a given height. BB_{PEAK} was obtained from the maximum polarimetric observations (Z_H, Z_{DR}, and new ρ_{HV}) within a height of 400 m above and below the height at which the first gradient was at maximum. The Z_H , Z_{DR} , and new ρ_{HV} at BB_{PEAK} should be greater than 0.0 dBZ, 0.0 dB, and 2 (=0.98), respectively. In this study, we briefly describe the coordinate rotation method. Figure 2 shows a diagram of the procedures for detecting BB_{TOP} and BB_{BOTTOM} from the QVP of the Z_{H} . First, the QVP was separated by the upper and lower parts of BBPEAK relative to the line connecting BBPEAK and Z'lower, upper. The original coordinate was rotated 90° in the clockwise (counterclockwise) direction to obtain the new coordinate with $h'_{upper}-Z'_{upper}$ ($h'_{lower}-Z'_{lower}$). Then, the height of 1200 m (800 m) above (below) BB_{PEAK} was selected to set the rotation angle \varnothing . The coordinate was again rotated \varnothing degrees in the clockwise (counterclockwise) direction, and h''_{upper} (h''_{lower}) and Z''_{upper} (Z''_{lower}) are the *x*-axis and *y*-axis in the final coordinate. The maximum value in the final coordinate was defined as BB_{TOP} (BB_{BOTTOM}).

Figure 3 shows the time series of the QVPs of the Z_H (top), Z_{DR} (middle), and ρ_{HV} (bottom), and the heights of BB_{TOP} (blue), BB_{PEAK} (black), and BB_{BOTTOM} (red) at an elevation angle of 15° for the BRI radar from 000 KST of 6 September 2019 to 1800 KST of 7 September 2019. In Figure 3a,c,e, the black solid line indicates BB height and the black dotted lines indicate T with a 5 °C interval (ranging from -30 to 20 °C). BB_{PEAK} is located at the Z_H maxima, Z_{DR} maxima, and ρ_{HV} minima. BB_{TOP} and BB_{BOTTOM} are within a height of 500 m above and below BB_{PEAK}. In Figure 3b,d,f, the solid and dashed lines indicate the heights where T is 0 °C and T_w is 0 °C, respectively. The height of BB_{TOP} is closer to the zero-isotherm layer (T = 0 °C) than that of BB_{PEAK} and BB_{BOTTOM}.



Figure 2. Quasi-vertical profile (QVP) of the Z_H and the parameters defined for rotating coordinates. (a) Original coordinate; (b) New coordinate after 90° rotation; (c) Final coordinate after \emptyset degree rotation. The thin lines indicate the top, peak, and bottom of the bright band (BB) derived from the QVP of the Z_H .



Figure 3. Time series of quasi-vertical profiles (QVPs) of the (**a**) $Z_{\rm H}$, (**c**) $Z_{\rm DR}$, and (**e**) $\rho_{\rm HV}$ and the height of the top (blue), peak (black), and bottom (red) of the BB from the (**b**) $Z_{\rm H}$, (**d**) $Z_{\rm DR}$, and (**f**) $\rho_{\rm HV}$ at elevation angles of 15.0° of the BRI radar from 0000 KST of 6 September 2019 to 1800 KST of 7 September 2019. The solid and dashed lines indicate the heights where T is 0 °C and T_w is 0 °C, respectively.

2.2.3. Variables for Characterizing the BB

The definitions of the feature parameters used to characterize the BB are presented in Table 2. These parameters are related to the geometric, thermodynamic, and polarimetric properties of the BB. The heights of the BB (BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM}) obtained by each polarimetric observation are H(Z_H Top), H(Z_H Peak), H(Z_H Bottom), H(Z_{DR} Top), H(Z_{DR} Peak), H(Z_{DR} Bottom), H(ρ_{HV} Top), H(ρ_{HV} Peak), and H(ρ_{HV} Bottom). H(T = 0 °C), H(T_d = 0 °C), and H(T_w = 0 °C) are the heights where T, T_d, and T_w are 0 °C. Z_H Top, Z_H Peak, Z_H Bottom, Z_{DR} Top, Z_{DR} Peak, Z_{DR} Bottom, ρ_{HV} Top, ρ_{HV} Peak, and ρ_{HV} Bottom, which are the polarimetric observations at the heights of BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} were defined to analyze polarimetric characteristics in the BB.

Feature Parameters	Definition
H(Z _H Top)	Height of BB_{TOP} identified by QVP of Z_H
H(Z _H Peak)	Height of BB _{PEAK} identified by QVP of Z _H
H(Z _H Bottom)	Height of BB_{BOTOM} identified by QVP of Z_H
H(Z _{DR} Top)	Height of BB _{TOP} identified by QVP of Z _{DR}
H(Z _{DR} Peak)	Height of BB_{PEAK} identified by QVP of Z_{DR}
H(Z _{DR} Bottom)	Height of BB_{BOTTOM} identified by QVP of Z_{DR}
H(ρ _{HV} Top)	Height of BB _{TOP} identified by QVP of ρ_{HV}
H(ρ _{HV} Peak)	Height of BB_{PEAK} identified by QVP of ρ_{HV}
$H(\rho_{HV} Bottom)$	Height of BB_{BOTTOM} identified by QVP of ρ_{HV}
$H(T = 0 \circ C)$	Height where T is 0°
$H(T_d = 0 \circ C)$	Height where T _d is 0°
$H(T_w = 0 \circ C)$	Height where T _w is 0°
Z _H Top	Z_{H} value at $H(Z_{H}$ Top)
Z _H Peak	Z_H value at H(Z_H Peak) (i.e., Maximum Z_H in BB)
Z _H Bottom	Z_H value at H(Z_H Bottom)
Z _{DR} Top	Z_{DR} value at H(Z_{DR} Top)
Z _{DR} Peak	Z_{DR} value at H(Z_{DR} Peak) (i.e., Maximum Z_{DR} in BB)
Z _{DR} Bottom	Z_{DR} value at H(Z_{DR} Bottom)
$ ho_{HV}$ Top	ρ_{HV} value at H(ρ_{HV} Top)
ρ_{HV} Peak	ρ_{HV} value at H(ρ_{HV} Peak) (i.e., Minimum ρ_{HV} in BB)
ρ_{HV} Bottom	ρ_{HV} value at H(ρ_{HV} Bottom)

Table 2. Definitions of feature parameters for characterizing the BB.

3. Results and Discussion

3.1. Characterization of the BB

3.1.1. Height of the BB

The monthly average $H(Z_H \text{ Peak})$ is shown in Figure 4 and Table 3. The cold (warm) color indicates that the radar is located at higher (lower) latitude. All $H(Z_H \text{ Peak})$ values in the warm season were higher than those in the cold season. The $H(Z_H \text{ Peak})$, which ranged from 4.14 to 4.71 km, on average, during the summer, showed an annual variation with a peak in July or August. The mean $H(Z_H \text{ Peak})$ in March, April, and November was less than 3.0 km, and that in September was greater than 4.0 km. The differences in $H(Z_H \text{ Peak})$ among radars during the cold seasons were greater than those during warm seasons. Overall, the $H(Z_H \text{ Peak})$ from radars at higher latitudes was lower than that from radar at lower latitudes. The $H(Z_H \text{ Peak})$ at the GSN and SSP radars, which are located at relatively low latitudes, reached 4 km in May, whereas those at the KWK, MYN, KSN, PSN, and JNI radars exceeded 4 km in June. The $H(Z_H \text{ Peak})$ at the BRI and GDK radars, which are located at relatively high altitudes, exceeded 4 km in July.



Figure 4. Monthly variation in mean height for BB_{PEAK} identified using the Z_H from March to November from the individual radar across the KMA weather radar network. The blue to red color indicates radar located from higher to lower latitudes.

Radar	MAR	APR	MAY	JUN	JUL	AUG	SEP	OCT	NOV
GDK	2.58	1.79	-	3.54	4.56	4.83	4.35	3.45	2.44
BRI	1.96	1.85	4.20	3.57	4.37	4.15	4.36	2.59	1.80
KWK	2.53	2.24	-	4.12	4.46	4.74	4.29	3.71	2.25
MYN	3.10	2.99	3.21	4.54	4.75	4.77	4.29	3.35	3.14
KSN	2.17	3.33	3.35	4.55	4.86	5.00	4.44	4.09	2.87
PSN	2.28	2.81	3.58	4.36	4.81	4.85	4.55	3.70	-
JNI	2.73	2.94	3.94	4.39	4.58	4.68	4.51	4.25	3.15
SSP	1.83	3.59	4.04	4.11	4.81	4.70	4.52	3.92	2.68
GSN	1.93	3.20	4.09	4.06	4.84	4.66	4.61	4.14	2.68
Mean	2.35	2.75	3.77	4.14	4.67	4.71	4.43	3.69	2.62

Table 3. Monthly mean height of BB_{PEAK} at each radar sorted in ascending order according to latitude.

Figure 5 shows the two-dimensional frequency distribution between $H(Z_{DR} \text{ Peak})$ and $H(Z_H \text{ Peak})$ and between H(ρ_{HV} Peak) and H(Z_H Peak). H(Z_H Peak) was 70 m and 100 m higher than H(Z_{DR} Peak) and H(ρ_{HV} Peak), respectively. The Z_H depends on the size, refractive index, and number concentration of hydrometeors in the melting layer. When the snowflakes enter the 0 °C isotherm layer, they start to melt at the tips of the crystal branches (mainly at the bottom side). Small snowflakes melt faster than large snowflakes, which boosts the aggregation and coalescence due to the difference in fall velocity. The Z_H increase below the 0 °C isotherm layer is due to the increase in the particle size (aggregation) or number density (no aggregation). The maximum of the Z_H results from melting particles covered by meltwater with a large size and a high dielectric constant. The fall velocity increases as large particles turn into raindrops below Z_H Peak. This process reduces the Z_H due to a decrease in the number concentration. In the BB, the Z_{DR} increases due to the oblate shape of the melting particles. The oblateness of the particles is maximized below Z_H Peak (where their size is at maximum). The decrease in the Z_{DR} below the BB is due to the break-up of large melted snowflakes, since the Z_{DR} is not related to the number concentration. The ρ_{HV} begins to decrease when the snowflakes and raindrops mix to a sufficient degree; therefore, it occurs at a relatively lower altitude than where the Z_H starts to increase via melting [16,21]. In other words, the Z_H depends on the change in size and number concentration of melting snowflakes, whereas the Z_{DR} and ρ_{HV} are subject to the non-spherical shape of melting snowflakes. The mean height difference between BB_{PEAK} from the Z_H and ρ_{HV} was 100 m in this study, which is consistent with the heights of 90, 96, and 121 m obtained in previous studies [21,33,34]. BB detection based on the ρ_{HV} can cause the underestimation of the height of the BB, as mentioned by Wolfensberger et al. [21]. According to Trömel et al. [26], the height of the maximum Z_H was very close to that of the maximum backscatter differential phase (δ) and was higher than that of the minimum ρ_{HV} . Trömel et al. [26] suggested that differences between heights should be analyzed in various climatic conditions to determine whether the aforementioned phenomenon is caused by differences in microphysical processes.



Figure 5. Two-dimensional frequency distribution (**a**) between $H(Z_{DR} \text{ Peak})$ and $H(Z_H \text{ Peak})$ and (**b**) between $H(\rho_{HV} \text{ Peak})$ and $H(Z_H \text{ Peak})$.

Figure 6 shows the difference between $H(Z_H \text{ Peak})$ and $H(Z_{DR} \text{ Peak})$ (black line), and that between $H(Z_H \text{ Peak})$ and $H(\rho_{HV} \text{ Peak})$ (red line) as a function of Z_H Bottom. The black (red) dotted line indicates no difference (the mean difference in heights shown in Figure 5). $H(Z_{DR} \text{ Peak})$ was almost identical to $H(Z_H \text{ Peak})$ in the range of 10 to 15 dBZ, whereas it was lower than 290 m than $H(Z_H \text{ Peak})$ in the range of 35 to 40 dBZ. However, $H(\rho_{HV} \text{ Peak})$ differed from $H(Z_H \text{ Peak})$ by more than 60 m (200 m) in the range of 10 to 15 dBZ (35 to 40 dBZ). In summary, according to Figures 5 and 6, $H(Z_H \text{ Peak})$, $H(Z_{DR} \text{ Peak})$, and $H(\rho_{HV} \text{ Peak})$ did not match. The difference in heights of BB_{PEAK} increased with increasing Z_H Bottom. The larger size and higher number concentration of melting snowflakes result in more significant differences in the height of BB_{PEAK} based on polarimetric observations.



Figure 6. Box plots of the mean differences between $H(Z_H \text{ Peak})$ and $H(Z_{DR} \text{ Peak})$ (**a**), and between $H(Z_H \text{ Peak})$ and $H(\rho_{HV} \text{ Peak})$ (**b**) as a function of Z_H Bottom. The black (red) dotted line indicates no difference (the mean height difference).

3.1.2. Geometric Structure of the BB

The heights of BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} were analyzed to characterize the vertical structure of the BB. Figure 7 shows the frequency distributions among the heights of BB_{TOP}, BB_{BOTTOM}, and BB_{PEAK} for Z_H, Z_{DR}, and ρ_{HV} , respectively. BB_{TOP} was 430–460 m higher than BB_{PEAK}, and BB_{BOTTOM} was 340 m lower than BB_{PEAK} on average, indicating that the structure of the BB was asymmetric. Physically, the melting particles spend more time covering the thin shell of meltwater around them, while they

rapidly collapse to form a raindrop at the final stage of melting. The difference between the heights of BB_{TOP} and BB_{BOTTOM} is considered to be the BB thickness, and the relative position (r) is considered to be the difference between the heights of BB_{PEAK} and BB_{BOTTOM} to the BB thickness as expressed below:



$r = (H(BB_{PEAK}) - H(BB_{BOTTOM}))/BB \text{ thickness}$ (2)

Figure 7. Two-dimensional frequency distributions. (a) Between $H(Z_H \text{ Top})$ and $H(Z_H \text{ Peak})$; (b) Between $H(Z_{DR} \text{ Top})$ and $H(Z_{DR} \text{ Peak})$; (c) Between $H(\rho_{HV} \text{ Top})$ and $H(\rho_{HV} \text{ Peak})$; (d) Between $H(Z_H \text{ Bottom})$ and $H(Z_H \text{ Peak})$; (e) Between $H(Z_{DR} \text{ Bottom})$ and $H(Z_{DR} \text{ Peak})$; and (f) between $H(\rho_{HV} \text{ Bottom})$ and $H(\rho_{HV} \text{ Peak})$; and (f) between $H(\rho_{HV} \text{ Bottom})$ and $H(\rho_{HV} \text{ Peak})$;

Figure 8 shows box plots of the BB's thickness (left) and r (right) according to Z_H Bottom at intervals of 5 dB. For the Z_H and Z_{DR} , the thicknesses of the BB increased with increasing Z_H Bottom. The weak Z_H in the BB represents non-aggregated snowflakes that are small in size. On the one hand, small snowflakes melt quickly and result in a thin BB. On the other hand, heavily aggregated snowflakes cause a thick and strong BB due to the fact that they need more time to completely melt than small particles. Interestingly, the BB thickness slowly increased until 20 dBZ, and rapidly increased above 20 dBZ, as shown in [34]. The BB thickness estimated using the Z_H and Z_{DR} exceeded 980 m and 870 m in the 35–40 dBZ range of Z_H Bottom. The BB thickness estimated using ρ_{HV} was 800 m in the 10–15 dBZ range of Z_H Bottom and 875 m in the 35–40 dBZ range of Z_H Bottom. The ρ_{HV} related to the diversity of hydrometeors had a relatively constant thickness regardless of Z_H and ρ_{HV} regardless of Z_H Bottom, and BB_{PEAK} was closer to BB_{BOTTOM} than BB_{TOP}. The r of the Z_{DR} decreased from 0.5 to 0.4 as Z_H Bottom increased from the range of 10–15 dBZ to 35–40 dBZ. The non-symmetric structure of the Z_{DR} resulted from a rapid decrease in the Z_{DR} , due to the break-up of large melted particles at the final state of melting process [34].



Figure 8. Box plots of the thickness of the BB (**left**) and relative position of BB_{PEAK} (**right**) as a function of Z_H BB_{BOTTOM}. The dashed line indicates the symmetric structure of the BB.

3.1.3. Thermodynamic Characteristic of the BB

The seasonal variability of the height of the BB depends on the ground temperature. To further analyze the thermodynamic characteristics of the BB, we compared H (T = 0 °C), H (T_w = 0 °C), H(Z_H Top), and H(Z_H Peak) (Figures 9 and 10). H(T = 0 °C) appears between H(Z_H Top) and H(Z_H Bottom), and H(T_w = 0°C) is close to H(Z_H Peak). H(Z_H Top) (H(Z_H Peak)) presented at 300 m (130 m) above (below) H(T = 0°C) on average with a standard deviation of 320 m (300 m). As compared with the NWP in [10], H(Z_H Peak) appeared at 100 m below H(T = 0°C), on average, with a standard deviation of 386 m. As observed by Zhang et al. [10], the top height of the BB exceeded the 0 °C altitude owing to the beam spreading effect. H(T_w = 0 °C) was located 470 m below H(Z_H Top) and 30 m below H(Z_H Peak), and H(T_w = 0 °C) was closer to H(Z_H Peak) than H(T = 0 °C). As mentioned in Zhang et. al. [10], the BB height detected from radars can be used to improve T for the numerical weather prediction (NWP).

The distributions of T, T_d, and T_w at BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} are shown in Figure 11, and Table 4 summarizes their mean and standard deviations. BB_{TOP} and BB_{PEAK} corresponded to temperatures ranging from -1.96 to -1.03 °C and 0.73 to 1.16 °C, respectively. The average T at BB_{BOTTOM} ranged from 2.41 to 2.84 °C. The average T_d at BB_{TOP}, BB_{PEAK}, and BB_{BOTTOM} ranged from -2.90 to -2.60 °C, from -0.89 to -0.49 °C, and from 0.64 to 1.03 °C. T_d refers to a longer tail on the left side of the distribution, with a standard deviation exceeding 3.00 °C. The average T_w at BB_{TOP} (BB_{PEAK} and BB_{BOTTOM}) was -2.03 to -1.73 °C (-0.04 to 0.37 °C and 1.53 to 1.93 °C).



Figure 9. Two-dimensional frequency distributions between (**a**) $H(Z_H \text{ Top})$ and $H(T = 0 \circ C)$ and between (**b**) $H(Z_H \text{ Top})$ and $H(T_w = 0 \circ C)$.



Figure 10. Two-dimensional frequency distributions between (**a**) $H(Z_H \text{ Peak})$ and $H(T = 0 \circ C)$ and between (**b**) $H(Z_H \text{ Peak})$ and $H(T_w = 0 \circ C)$.

Table 4. Mean and standard deviation (STD) of temperature (T), dew point temperature (T_d), and wet-bulb temperature (T_w) at the top, peak, and bottom of the BB.

	T at H(Z _H Bottom/Peak/Top)			H(Z _H	T _d at H(Z _H Bottom/Peak/Top)			T _w at H(Z _H Bottom/Peak/Top)		
MEAN	2.41	0.73	-1.33	0.64	-0.89	-2.90	1.53	-0.04	-2.03	
STD	1.55	1.32	1.39	3.34	3.24	3.36	1.71	1.52	1.58	
	T at				T _d at			T _w at		
	H(Z _{DR} Bottom/Peak/Top)			H(Z _{DR}	H(Z _{DR} Bottom/Peak/Top)			H(Z _{DR} Bottom/Peak/Top)		
MEAN	2.71	1.04	-1.96	0.92	-0.61	-2.63	1.82	0.25	-1.76	
STD	1.63	1.47	1.42	3.39	3.31	3.38	1.79	1.65	1.60	
		T at			T _d at			T _w at		
	$H(\rho_{HV} Bottom/Peak/Top)$			$H(\rho_{HV})$	H(ρ _{HV} Bottom/Peak/Top)			H(ρ _{HV} Bottom/Peak/Top)		
MEAN	2.84	1.16	-1.03	1.03	-0.49	-2.60	1.93	0.37	-1.73	
STD	1.65	1.44	1.51	3.39	3.28	3.40	1.79	1.60	1.69	





Figure 11. Normalized frequency distribution of (a,d,g) T, (b,e,h) T_d, and (c,f,i) T_w at top (blue), peak (black), and bottom (red) of bright band from QVPs of (a-c) Z_H, (d-f) Z_{DR}, and (g-i) ρ_{HV} .

3.2. Polarimetric Observation of the BB

The distributions of polarimetric observations at BB_{TOP} (blue), BB_{PEAK} (black), and BB_{BOTTOM} (red) are shown in Figure 12. Z_H Peak mainly ranged between 10 and 45 dBZ, and the average Z_H Peak was 27.2 dBZ. The average Z_H Top (Z_H Bottom) was 21.2 dBZ (17.5 dBZ). The Z_H , when the ice particles completely melted, was lower than that when they began to melt. Z_{DR} Peak was distributed between 0.0 and 3.0 dB with an average of 1.28 dB. The average values of Z_{DR} Top and Z_{DR} Bottom were almost similar (0.26 and 0.24 dB). The melting snowflakes were observed to be more oblate than snowflakes and raindrops. ρ_{HV} Peak was distributed between the range of 0.86 and 0.97 and was 0.92 on average. The average ρ_{HV} Top and ρ_{HV} Bottom, which are the threshold values commonly used for BB detection, were identical (0.97).



Figure 12. Normalized frequency distribution of (**a**) Z_{H} , (**b**) Z_{DR} , and (**c**) ρ_{HV} at top (blue), peak (black), and bottom (red) of the BB.

The results were compared with those obtained under various climatic conditions. In [21,26], the authors used X-band radar and [27] used S-band radar to analyze the BB. [21] detected the BB using RHI data from Davos (Swiss Alps), Ardeche (South of France), Iowa (Midwestern USA), and Payerne (Swiss Plateau). Ref. [26] constructed the QVPs from a radar located in Born (Germany), while [27] constructed theirs from the WSR-88D radar in the USA. Their BB detection technique was very similar to that of [21,26], and [27] applied a technique based on the ρ_{HV} . According to [27], QVP allows for more accurate quantification of polarimetric observations than RHI data. Therefore, the results of this study were comparable to those of previous studies. The distribution of Z_H Peak, Z_{DR} Peak, and ρ_{HV} Peak in Figure 12 were very similar to those in previous study. The average of Z_H Peak (27.2 dBZ) was slightly lower than that in the Payerne region (29.0 dBZ), higher than that in the Iowa region (25.46 dBZ), and higher than that obtained by [27] (25.42 dBZ). The average Z_{DR} Peak (1.28 dB) was slightly different from that in the Ardeche region (1.29 dB) and that obtained by [27] (1.13 dB). The ρ_{HV} Peak (0.92) was higher than those obtained in Davos and Iowa (0.82), but very consistent with those obtained in the Born region (0.93) and [27] (0.94).

Figure 13 shows scatterplots between Z_H Peak and Z_H Top/Z_H Bottom, Z_{DR} Peak and Z_{DR} Top/Z_{DR} Bottom, and ρ_{HV} Peak and ρ_{HV} Top/ ρ_{HV} Bottom. The color of the diamond symbol indicates the $Z_{\rm H}$ Peak. According to [27], a high $Z_{\rm H}$ in the BB represented large snowflakes enlarged via aggregation, and a low $Z_{\rm H}$ mainly represented pristine ice crystals. In addition, a high number of snowflake concentrations increased the number of raindrops after passing the BB. It is apparent from Figure 13a that the mean difference between Z_H Top and Z_H Peak was 9.68, with a standard deviation of 2.88 dB, and the mean difference between Z_H Peak and Z_H Bottom was 6.00 dB with a standard deviation of 2.49 dB. Large snowflakes result in an intense BB, which leads to overestimation of rainfall at the surface. Z_{DR} Top and Z_{DR} Peak showed a correlation of 0.58 and a mean difference of -1.04 dB, while Z_{DR} Peak and Z_{DR} Bottom showed a correlation of 0.33. Large snowflakes with high Z_{H} Bottom turn into large raindrops with high Z_{DR} Bottom. Large snowflakes grown by aggregation (represented by high Z_H Peak) turn into large raindrops (high Z_{DR} Bottom). In other words, the size of raindrops is related to the growth process of snowflakes above the BB. The difference between ρ_{HV} Peak and ρ_{HV} Top (between ρ_{HV} Peak and ρ_{HV} Bottom) increased even more as Z_H Peak increased. This results from the inhomogeneity of the hydrometeors' shape, orientation, and size within the BB since large snowflakes melt more slowly than small snowflakes. In addition, ρ_{HV} Peak, ρ_{HV} Top, and ρ_{HV} Bottom with low Z_H Bottom were similar (close to the 1:1 line). This mean that the ρ_{HV} shows no distinctive signature for a weak BB.

Figure 14 represents the mean profiles of the (a) Z_H and (b) Z_{DR} at the Z_H Bottom classes with 5 dBZ intervals. H(Z_H Peak) and H(Z_{DR} Peak) are reference heights. The maximum Z_H and Z_{DR} were located at 0.0 km. The difference in the Z_H above the BB and Z_H Peak was greater than the difference in the Z_H below the BB and Z_H Peak. The intensity of the BB depended on Z_H Bottom, and the Z_H below the BB was almost constant at every class. The size and concentration of snowflakes determined the Z_H structure of the BB and the rainfall intensity below the BB. The Z_{DR} decreased above the BB as the snowflake particles smoothen when they start to melt. Large snowflakes (high Z_H Bottom class) with a high axis ratio have a low Z_{DR} above the BB. The Z_{DR} within the BB with a high Z_H Bottom class. The slow the BB was larger at the high Z_H Bottom class. The shape and orientation of snowflakes determined the Z_{DR} below the BB was larger at the high Z_H Bottom class.



Figure 13. Scatter plots of (**a**) Z_H Top and Z_H Peak, (**b**) Z_{DR} Top and Z_{DR} Peak, (**c**) ρ_{HV} Top and ρ_{HV} Peak, (**d**) Z_H Bottom and Z_H Peak, (**e**) Z_{DR} Bottom and Z_{DR} Peak, and (**f**) ρ_{HV} Bottom and ρ_{HV} Peak. Colors indicate the Z_H Peak with 3 dBZ intervals.



Figure 14. Mean profile of the (**a**) Z_H and (**b**) Z_{DR} with respect to the height relative to BB_{PEAK} at the Z_H Bottom classes with 5 dBZ intervals.

4. Conclusions

In this study, we investigated the characteristics of BB in South Korea using QVPs from an operational S-band dual-polarization weather radar network. The BB was automatically identified based on the morphological features from the QVPs of polarimetric observations (Z_H , Z_{DR} , and ρ_{HV}) using the coordinate rotation technique proposed by [9], and their geometric, thermodynamic, and polarimetric characteristics were statistically examined. The polarimetric observations were corrected before constructing the QVPs for comparable analysis among weather radars in the network. First, the system calibration bias in power-related polarimetric observations (Z_H and Z_{DR}) was corrected based on the self-consistency principle between power- and phase-based measurements. Second, the ρ_{HV} was biased at low SNR due to noise effects. The precipitation echoes yielded a value that was equal to or greater than 0.98. Unfortunately, an abnormal ρ_{HV} was observed in meteorological echoes at a low SNR. The ρ_{HV} in low SNR areas was corrected using the SNR. Quality control was performed using the ρ_{HV} and SNR to minimize non-meteorological echoes, and then the Z_{H} , Z_{DR} , and ρ_{HV} were averaged in the azimuth direction to generate QVPs of polarimetric observations. The ρ_{HV} was converted to a new variable to apply the same procedure for the detection of the BB. In this study, the peak of the BB (BB_{PEAK}) was defined as the maximum value by calculating the first gradient. The top and bottom of the BB (BB_{TOP} and BB_{BOTTOM}) were identified via application of the coordinate rotation method developed by [9].

We analyzed the monthly mean height of BB_{PEAK} for all radars in the KMA network. The heights of BB_{PEAK} showed a seasonal variation in all radars (e.g., the highest occurred in the summer). The maximum height of BB_{PEAK} derived from the Z_H was 5 km, and the average heights varied within the range from 4.14 to 4.71 km in summer. However, they showed distinct differences depending on the location (e.g., latitude) and the altitude of the radar within the radar network, even in the same season. The heights of BB_{PEAK} differed among the polarimetric observations. The height where melting particles had the most oblate shapes (BB_{PEAK} derived from Z_{DR}) were below that where their size was at maximum (BB_{PEAK} derived from ρ_{HV}) below BB_{PEAK} derived from Z_H. The height difference of BB_{PEAK} between the Z_H and Z_{DR}, and that between Z_H and ρ_{HV} increased with increasing Z_H Bottom. The difference in heights of Z_H Peak and ρ_{HV} Peak was similar to that in previous studies under various climatic conditions.

The relative position (r) of BB_{PEAK} (defined as the height difference between BB_{PEAK} and BB_{BOTTOM} to the BB thickness) and the BB thickness were calculated to analyze the geometric characteristics of the BB. The difference in heights between BB_{PEAK} and BB_{TOP} (BB_{BOTTOM}) was 430–460 m (350 m). The BB thickness represented by the Z_H and Z_{DR} tended to increase with increasing Z_H Bottom. The r was less than 0.5 for all variables, and BB_{PEAK} was close to BB_{BOTTOM}. The r for the QVP of Z_{DR} was close to 0.5 if Z_H Bottom was low, and the r decreased to 0.4 if Z_H Bottom was high. We confirmed from these results that the structure of the BB was asymmetrical and depended on Z_H Bottom.

The thermodynamic characteristics were analyzed by comparing the BB heights and zero isothermal layers of dry-bulb, dew point, and wet-bulb temperatures. The zero-isotherm layer of the dry-bulb temperature was located between BB_{TOP} and BB_{BOTTOM} and was closer to the zero-isotherm layer of the welt-bulb temperature. BB_{TOP} was located above the zero temperature (-1.96 to -1.03 °C), and BB_{PEAK} was located below the zero temperature (0.73 to 1.16 °C).

The microphysical process associated with the BB was investigated by analyzing the polarimetric observations in the BB. The polarimetric observations at BB_{PEAK} were compared with those in previous studies. The distribution of polarimetric observations was very similar, although previous studies utilized different frequencies, radar scan strategies, and BB detection techniques. The Z_H at BB_{PEAK} averaged 27.2 dB, with a difference of 9.68 (6.00) dB from that at BB_{TOP} (BB_{BOTTOM}). The Z_{DR} at BB_{PEAK} was 1.28 dB, which was higher than the Z_{DR} at BB_{TOP} (0.26 dB) and BB_{BOTTOM} (0.24 dB). The ρ_{HV} at BB_{PEAK} was 0.92, whereas that at BB_{TOP} and BB_{BOTTOM} was 0.97, which is the threshold traditionally used for the detection of the BB. The relation between polarimetric observations at BB_{PEAK}, BB_{TOP}, and BB_{BOTTOM} represented the microphysical properties of the BB. The Z_H at BB_{PEAK}, BB_{TOP}, and BB_{BOTTOM} was highly

correlated. This means that large snowflakes turn into large raindrops. It was also confirmed that the Z_{DR} at BB_{BOTTOM} and BB_{PEAK} showed a positive relation with a high Z_H at BB_{PEAK}. The mean profiles of Z_H and Z_{DR} also depended on the size and concentration of the snowflakes above the BB.

In conclusion, the characteristics of BB from the QVPs of polarimetric observations were investigated in this study. The three-dimensional detection of BB and its intensity correction remain a challenge. Especially, this is more difficult in the cold season because the vertical structure of BB cannot be fully identified when they occur near the surface. The polarimetric observations above, within, and below the BB revealed in this study provide the characteristics of the BB related to microphysical processes. The results contribute by promoting an understanding of polarimetric signatures within BB and ultimately improve the performance of BB correction techniques. Furthermore, the NWP can represent the microphysical processes within BB, and the zero isothermal layer identified from radar observations can be used for NWP data assimilation.

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