## Effective Heat Transfer Pathways of Thermally Conductive Networks Formed by One-Dimensional Carbon Materials with Different Sizes

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 Table S1. Summary of the detailed preparation conditions and thermal conductivity values of carbonbased films prepared in this study.

Sample	FWCNT content (wt%)	MPCF content (wt%)	Ag content (mg)	Sonication time (h)	Heat treatment (1000 °C)	Thickness (µm)	Bulk density (kg/m³)	Thermal conductivity (W/mK)
1	100	-	-	0.5	Х	248	210	1.65
2	100	-	-	2	Х	228	286	2.70
3	100	-	-	4	Х	135	316	4.02
4	100	-	-	8	Х	138	360	4.71
5	80	20 (200 µm)	-	0.5	Х	236	220	2.30
6	60	40 (200 µm)	-	05	Х	182	280	3.29
7	40	60 (200 µm)	-	0.5	Х	166	360	4.91
8	20	80 (200 µm)	-	0.5	Х	149	350	4.63
9	10	90 (200 µm)	-	0.5	Х	173	300	4.22
10	5	95 (200 μm)	-	0.5	Х	179	290	3.60
11	100	-	-	4	О	145	305	4.80
12	100	-	-	0.5	0	250	200	2.02
13	80	20 (200 µm)	-	0.5	0	229	213	2.71
14	60	40 (200 µm)	-	0.5	0	190	272	4.02
15	40	60 (200 µm)	-	0.5	0	161	327	5.41
16	20	80 (200 µm)	-	0.5	О	150	298	4.84
17	10	90 (200 µm)	-	0.5	0	158	289	4.25
18	5	95 (200 μm)	-	0.5	О	134	322	3.65
19	40	60 (6 mm)	-	0.5	Х	185	274	10.7
20	40	60 (6 mm)	5	0.5	Х	197	234	14.9
21	40	60 (6 mm)	10	0.5	X	188	333	21.0
22	40	60 (6 mm)	15	0.5	Х	200	310	23.7
23	40	60 (6 mm)	20	0.5	Х	270	316	25.1
24	40	60 (6 mm)	25	0.5	Х	249	343	25.8



Figure S1. Schematic of the thermal conductivity measurement system using the modified laser flash technique.



**Figure S2.** HR-SEM images of the FWCNT-MPCF hybrid films with different MPCF (length: 200  $\mu$ m) contents: (a) and (b) 20 wt%, (c) and (d) 60 wt%, and (e) and (f) 90 wt%. (a), (c), and (e) are low-magnification images, while (b), (d), and (f) are high-magnification images.



Figure S3. TGA curve of Ag nanoparticles under air atmosphere to 350 °C (heating rate of 10°C min<sup>-1</sup>).



**Figure S4.** Measurement of the Ag nanoparticle sizes using HR-SEM image of the FWCNT-MPCF-Ag hybrid film incorporated with Ag content of 20 mg (MPCF length: 6 mm; MPCF content: 60 wt%; ultrasonication for 0.5 h).