



Optimal Hardware and Control Co-Design Applied to an Active Car Suspension Setup

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Abstract: For complex systems, it is not easy to obtain optimal designs for the hardware architecture and control configurations. Every design aspect influences the final performance, and often the interactions of the different components cannot be clearly determined in advance. In this work, a novel co-design optimization method was applied that allows the optimal placement and selection of actuators and sensors to be performed simultaneously with the determination of the control architecture and associated controller tuning parameters. This novel co-design method was applied to a state-space model of a downscaled active car suspension laboratory setup. This setup mimics a car driving over a specific road surface while active components in the suspension have to increase the driver's comfort by counteracting unwanted vibrations. The result of this co-design optimization methodology is a Pareto front that graphically represents the trade-off between the maximum performance and the total implementation cost; the co-design results were validated with measurements of the physical active car suspension setup. The obtained controller tuning parameters are compared herein with existing controller tuning methods to demonstrate that the co-design method is able to determine optimal controller tuning parameters.

Keywords: closed loop systems; evolutionary computation; control design; state-space methods



1. Introduction

Multi-domain engineering is becoming increasingly important in the development of modern products and machines. The design of such complex systems has therefore become a comprehensive design challenge. Conventionally, the different domains of system design are addressed sequentially and thus separately. First, a mechanical engineer makes decisions on the physical setup in accordance with properties regarding strength, inertia, weight, etc. In addition, a choice is made on the location of actuators and sensors and which parts of the system are correspondingly measured or controlled. Additionally, selection of the types of actuators and sensors is done. The mechanical engineer will try to make the correct choices of hardware components based on some assumptions regarding the performance to be achieved and the total implementation costs. After that, the control engineer designs a control configuration for the fixed hardware architecture. The application of different control architecture features can be considered, while corresponding controller tuning parameters must be determined. In contrast to the mechanical engineer, the control engineer uses different objectives, such as system stability, reference tracking properties, and disturbance rejection.

This sequential hardware architecture and control configuration design will cause problems when designing complex and interacting systems, resulting in sub-optimal system performance. First of all, in practice, the mechanical engineer and the control engineer



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almost completely ignore the tight interdependency between the hardware architecture and the control configuration on the overall performance. For example, choices made by the hardware engineer can already severely limit the design space of the control engineer. On the other hand, it is not always clear what the influence of specific design choices is on the final performance of the total system. Therefore, more and more attention is being paid to resource-efficient system design with a growing demand for systematic and comprehensive methods to obtain optimal co-designs of hardware architecture and control configurations [1].

This co-designing of hardware architecture and control configuration has only been applied to a limited extent. Examples of the co-designing of geometric properties and controller tuning parameters for a four-bar system (using a Genetic Algorithm), parallel robots (using a differential evolution), and machine tools (using a multilevel decomposition) can be found in [2–4], respectively. Similarly, co-designing of controller tuning through the use of a Linear Quadratic Regulator (LQR) method and the geometrical properties of a pendulum system, a satellite altitude control, and an angular motor controlling a mass position was detailed in [5–7], respectively. More recently, ref. [8] combined mechanical design properties and the PD controller tuning for an airborne wind energy system. Other controller tuning methods are also used in the co-designing of the controller tuning and mechanical design variables. For example, refs. [9,10] used the H_2/H_{∞} method to obtain the controller tuning parameters. PID values can also be directly optimized, as shown in [11] for a DC motor. In [12], an example is shown in which the co-design of mechanical design variables and controller parameters was performed for a hybrid power train system used in a hydraulic excavator.

The co-design examples mentioned so far succeed in the simultaneous optimization of separate hardware parts and controller tuning for fixed and rather modest feedback loops. In contrast, the author of this work recently proposed an optimization methodology to perform a thorough co-design of the hardware architecture and control configuration [13]. The proposed methodology can perform a hardware architecture and control configuration co-design in which more parts can be optimized at the same time, while considering more extensive and also changing controller architectures. By doing so, a larger design space is explored to obtain a system-level optimum. The optimization methodology does not assume a fixed control architecture, but instead, a trade-off can be made between different control architecture features, which has not been considered in current literature before. Furthermore, the optimization methodology enables the inclusion of non-linear constraints and (conflicting) objectives. These objectives will always be related to the trade-off between implementation cost and system performance, represented in a Pareto front. This profound level of co-design has not been applied in the current literature.

Earlier work by the author suggested using a Genetic Algorithm (GA) [14] to optimize the proposed problem because it is one of the few algorithms that can satisfy the applicable non-linear constraints and intended objectives [13]. These objectives can be freely programmed according to, for instance, tracking error, vibrations, energy consumption, or settling time requirements. Additionally, non-linear (mixed-integer) constraints on, for example, maximum actuator output or hardware cost can be taken into account. A disadvantage in applying a Genetic Algorithm is that a relatively long calculation time is required. Genetic algorithms have previously been implemented for many applications, for instance, to determine the optimal controller tuning parameters using a Linear Quadratic Regulator (LQR) [15], H_{∞} control [16], or proportional integral (PI) control [17]. Another field of application of Genetic Algorithms is the motion profile optimization for repetitive machines [18].

In this paper, the novel co-design methodology is applied to a state-space model of a downscaled active car suspension setup (see Figure 1). Over the past decades, active suspension control technologies became an extensive research topic; hence, these systems have a significant influence on the vehicle dynamics and the subjective driver comfort impression [19]. An example of previous work using a Genetic Algorithm (GA) to optimize

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feedback controller values via the Linear Quadratic Regulator (LQR) method for a quarter-car suspension can be found in [20]. Furthermore, refs. [16,21] used a Genetic Algorithm to optimize a robust H_{∞} controller for a vehicle suspension control. These optimizations were limited in the sense that only the controller tuning parameters were optimized. Additionally, mechanical design parameters and their influences on vehicle dynamics were optimized in [22,23]. More information on the theory and application of vehicle dynamics can be found in [24]. The laboratory setup that was used for this study mimicked the behavior of a car driving on a road surface while active suspension components ensure the driver's comfort. The test setup allowed examining a wide variety of hardware architectures and control configurations. It is important to emphasize that the primary goal of this setup was not to improve the current state-of-the-art in active car suspension systems but rather to validate the presented model-based co-design methodology with measurements on a physical setup.

The paper is organized as follows. Section 2 details the downscaled physical laboratory setup and the corresponding model description on which the co-design method was validated. Subsequently, Section 3 describes the application of the co-design methodology and its properties. The results of this model-based optimization and the validation measurements on the laboratory setup are presented in Section 4. Finally, conclusions are formulated in Section 5.

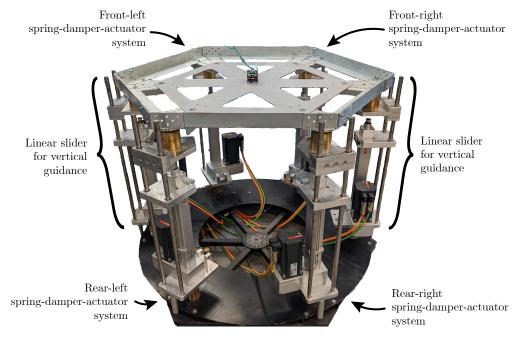


Figure 1. Picture of the physical full-car active suspension laboratory setup. The locations of the sliders and the spring-damper-actuator systems are indicated in accordance with the diagram in Figure 2. The linear slider systems for vertical guidance also had an actuator, but these were not connected to use the laboratory setup as in an active car suspension. The springs are not present in this picture, but were mounted to perform the mentioned tests.

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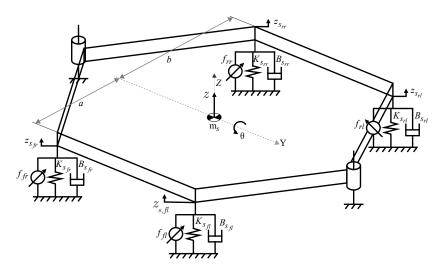


Figure 2. Full-car active suspension laboratory setup diagram.

2. Active Car Suspension Setup

2.1. Setup Properties

A full-car active suspension laboratory setup was built to emulate the behavior of the widely available theoretical full-car suspension model [25–28]. The physical laboratory setup is shown in Figure 1, with the corresponding laboratory setup model diagram shown in Figure 2. The setup consisted of a central, hexagonal platform with mass m_s supported in four places by a spring, a damper, and an actuator system in parallel. The spring-damper systems correspond to a classic car's suspension, while the actuators represented an active component to counteract the unwanted vibrations of the central platform. The lower sides of the vertical rods could not translate but could rotate around their attachment points through ball couplings. The upper sides of the vertical rods were also attached to the central platform using ball couplings. Linear sliders were provided on the two opposite sides of the central platform, allowing the central platform to translate along the z-axis with a heave height z and rotate around the y-axis with an angular pitch rotation θ . This makes it possible to emulate a car driving on a straight road.

The key parameters to represent a passenger car suspension model are not the same for every car, but typical values can be found in previous work [19,23,25,27,29]. The laboratory setup has a scaling factor of 1:2 compared to typical mid-size passenger car dimensions. Therefore, the appropriate scaling laws must be applied for some fundamental parameters (see Table 1) [30]. Although the laboratory setup parameters do not perfectly match the downsized values of a typical passenger car, they are close enough so that the laboratory setup will exhibit similar dynamic characteristics to a typical mid-size passenger car.

Table 1. Downscaling typical passenger car parameters to laboratory setup parameters with scaling factor 1:2.

	Downsized Value from a Typical Passenger Car	Lab Setup Parameter
Mass inertia (I_{yy}) [kgm ²]	$4000/2^5 = 125$	104.45
Suspension stiffness (K_s) [N/m]	23,000/2 = 11,500	13,000
Damping coefficient (B_s) [Ns/m]	$6000/2^2 = 1500$	1800
Dimension front-rear $(a + b)$ [m]	2.5/2 = 1.25	1
Body mass (m_s) [kg]	$1400/2^3 = 175$	58.26

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2.2. State-Space Model Identification

The system has four inputs, namely, the four actuator forces u_{fr} , u_{fl} , u_{rr} , and u_{rl} . The subscripts fr, fl, rr, and rl represent the wheel location, being front-right, front-left, rear-right, and rear-left, respectively. These system inputs are used for both the application of the road profile disturbances d_{fr} , d_{fl} , d_{rr} , and d_{rl} (see Section 2.3) and the control effort signals f_{fr} , f_{fl} , f_{rr} , and f_{rl} eliminating unwanted central platform vibrations. The applied feedback control has no information on the road disturbance signals. The model inputs are as follows:

$$\mathbf{u} = \begin{bmatrix} u_{fr} \\ u_{fl} \\ u_{rr} \\ u_{rl} \end{bmatrix}, \tag{1}$$

with $\mathbf{u} = \mathbf{f} + \mathbf{d}$. The model states \mathbf{x} are the horizontal position z, speed \dot{z} , acceleration \ddot{z} , and angle θ of the central platform:

$$\mathbf{x} = \begin{bmatrix} z \\ \dot{z} \\ \ddot{z} \\ \theta \end{bmatrix}, \tag{2}$$

while the same system properties are used for the model output y for the identification procedure:

$$\mathbf{y} = \begin{bmatrix} z \\ \dot{z} \\ \ddot{z} \\ \theta \end{bmatrix}. \tag{3}$$

As a result, the dimensions of the state-space system matrices are defined as **A** $[4 \times 4]$, **B** $[4 \times 4]$, **C** $[4 \times 4]$, and **D** $[4 \times 4]$. For the model identification, a multisine excitation with sample frequency $F_s = 1000$ Hz containing sine frequencies from 0.01 Hz to 490 Hz [31] is imposed on the system inputs, while the system response is measured. From the measured input and output signals, the model matrices values are identified using the prediction error minimization (PEM) method [32]. This model identification procedure is graphically displayed in Figure 3.

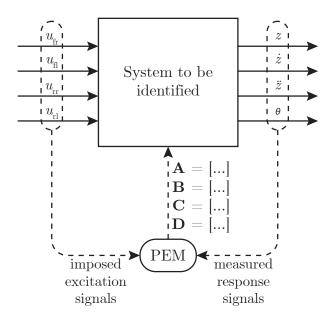


Figure 3. Graphical representation of the model identification procedure using a prediction error minimization (PEM) method to identify the system's state-space matrix values based on the imposed excitation signals and measured response signals.

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The resulting (rounded) matrix values are shown in Equations (4)–(7). Figure 4 depicts the Bode plot of the identification measurements using the multisine signal and the Bode plot of the identified PEM state-space model. It is important to emphasize that the model will not perfectly match the actual setup. For example, it is known in advance that the dampers have a non-linear character. This non-linear behavior (along with possibly other phenomena such as static friction) is not explicitly modeled in the identified Linear time-invariant (LTI) system.

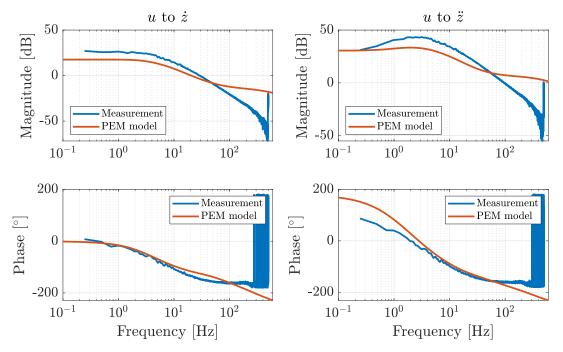


Figure 4. Comparison of the Bode plots of the identification measurements (blue) and the identified prediction error minimization (PEM) state-space system (red) from system inputs u to platform velocity \dot{z} (**left**) and system inputs u to platform acceleration \ddot{z} (**right**).

$$\mathbf{A} = \begin{bmatrix} -525.4 & -286.7 & 31.40 & 20948 \\ 2773 & 4221 & -462.6 & -262133 \\ 27543 & 41914 & -4603 & -2603136 \\ 47.85 & 24.79 & -2.672 & -1831 \end{bmatrix}$$
(4)

$$\mathbf{B} = \begin{bmatrix} -62.87 & 54.67 & 35.99 & -44.83 \\ 539.0 & -511.8 & -529.7 & 585.6 \\ 5704 & -5429 & -5352 & 5825 \\ 4.168 & -4.047 & -3.078 & 3.490 \end{bmatrix}$$
 (5)

$$\mathbf{C} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \tag{6}$$

2.3. Road Profile

Road profile disturbance signals were applied to the actuators with the intention of the central platform experiencing the same forces as if it was driving over a real road surface.

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A random road profile formulation was based on the ISO 8608 norm, with a "roughness factor" indicating how smooth the road surface is. This factor ranges from 1 to 8 for smooth asphalt layers to very rough cobblestone roads [33,34]. The road profile is defined as a displacement disturbance, while the laboratory setup only allows force disturbance inputs. That is why the road displacement z_r is converted to a force disturbance d for the active car suspension laboratory setup. This conversion is graphically represented in Figure 5.

Figure 6a shows an ISO 8606 road profile for a car traveling at 72 km/h for 20 s on a road profile of 400 m with a roughness factor 5. Figure 6b shows this displacement profile converted to an equivalent force profile, applicable to the laboratory setup. Based on a speed of 72 km/h and a distance between the front and rear wheel axles of 1 m, there will be a time delay of 0.05 s between the applied front and rear wheel force disturbances.

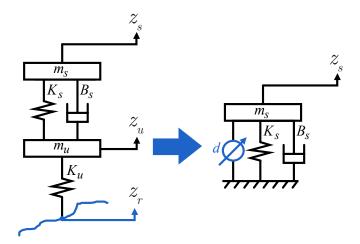


Figure 5. Graphical representation of the conversion from a road displacement z_r from a traditional quarter car model to a force disturbance d for the quarter-car suspension laboratory setup.

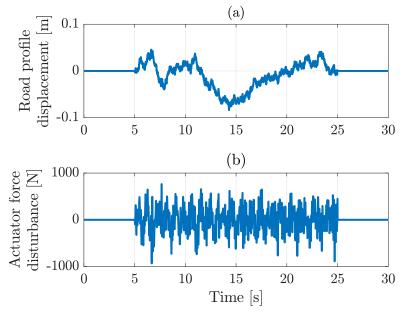


Figure 6. (a) ISO 8608 road displacement profile with roughness factor 5. (b) Corresponding actuator force disturbance.

3. Hardware and Control Co-Design

3.1. Objective Function

The objective of the active car suspension setup is to achieve the greatest comfort for the driver. According to the ISO 2631 norm, the driver's comfort is quantified as the

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perceived acceleration levels in the three principal axes [35]. The laboratory setup only allows translation along the vertical *z*-axis. That is why in this case, the control objective is to minimize the *z*-axis accelerations, maximizing the driver's comfort. A fitness value (FV) quantifies the performance according to the ISO 2631 norm by taking the rms of the acceleration along the *z*-axis:

$$FV = \sqrt{\frac{1}{N} \sum_{n=1}^{N} \ddot{z}^2},\tag{8}$$

with N the total number of samples, being $T_m/T_s = 30 \text{ s}/0.001 \text{ s} = 30,000.$

3.2. Design Parameters

The design parameters for this co-design optimization problem consist of two actuator selection integers, two sensor selection binaries, two control architecture binaries, and 12 controller tuning parameters.

The actuator selection integers $i_{act,f}$ and $i_{act,r}$ define which types of actuators are applied to the front wheels f and the rear wheels r, respectively. Table 2 provides an overview of the different actuator types, with each actuator type corresponding to an associated cost and maximum actuator output. The component cost was chosen arbitrarily and was different for each application. Therefore, this cost is not expressed in a currency but in percentage terms relative to the most expensive setup in which all possible parts were present.

Table 2. Possible actuator selection integer $i_{act,...}$ values with corresponding cost and maximum actuator output.

Actuator Selection Integer	Cost [%]	Maximum Actuator Output [Nm]
0	0	0
1	5.7	1
2	14.3	2
3	42.9	5

The design space for the feedback control architecture is shown in Figure 7. This design-space shows the attainable form of the feedback control when all capabilities regarding the control configuration optimization are active. The second and fourth row of the **C** and **D** matrices of the identified model are omitted for the co-design optimization procedure so that the model has the platform position z and acceleration \ddot{z} as outputs. PID controllers can be applied separately to the front and rear wheels for both the displacement and acceleration feedback control. The sensor selection binaries $b_{sen,z}$ and $b_{sen,\ddot{z}}$ define the presence or absence of a sensor on the central platform heave position z and acceleration \ddot{z} , respectively. The cost for a displacement feedback sensor and an acceleration feedback sensor is 1.4% and 4.3%, respectively. The control architecture binaries $b_{CL,z}$ and $b_{CL,\ddot{z}}$ define the presence or absence of the PID controllers for the displacement and acceleration feedback control, respectively. Both control loops have a cost of 2.1%. The PID controller values $K_{p,...}$, $T_{i,...}$, and $T_{d,...}$ are also design parameters, with the subscript referring to the corresponding controller. For example, $T_{d,\ddot{z},r}$ is the T_d value of the acceleration feedback PID controller connected to the rear actuators.

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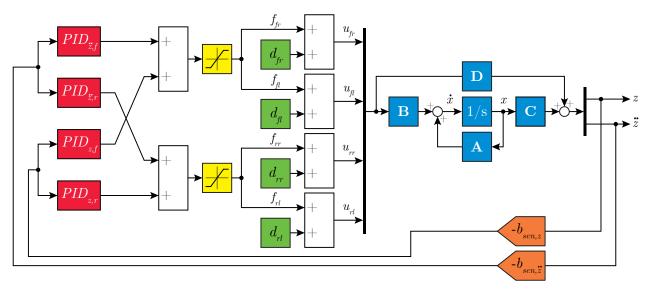


Figure 7. Design space for the feedback control architecture with the active car suspension model in blue, road profile force disturbance signals in green, actuator output saturation in yellow, PID controllers in red, and sensor feedback in orange.

3.3. Constraints

The number of possible actuator types determines the upper and lower bounds for the actuator selection integers, see Table 3. For the binary design parameters, the bounds are equal to zero and one. For the PID values, the most relaxed boundaries are determined based on system stability margins. For example, for determining the constraint on the upper bound of the acceleration feedback values $K_{p,\vec{z},f}$ and $K_{p,\vec{z},r}$, a phase margin ϕ_{PM} of 50° is suggested to obtain a sufficiently robust control [36]. The Bode plot of the system input u to the platform acceleration \ddot{z} identification measurements is shown in Figure 8. To obtain this phase margin ϕ_{PM} of 50° , a zero crossing of the magnitude plot must occur at a phase angle shift of $-180^\circ + \phi_{PM} = -180^\circ + 50^\circ = -130^\circ$. The phase plot shows that a phase angle shift of -130° occurs at $\omega_{PM50} = 19.5Hz$ (illustrated with a black vertical line in Figure 8). The gain at phase ω_{PM50} is 25.96 dB. Thus, the corresponding gain factor is $10^{-25.96/20} = 0.05$.

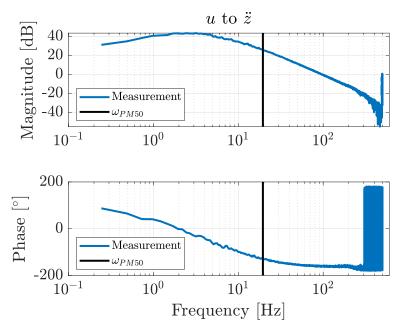


Figure 8. Bode plot of the identification measurements (blue) from system inputs u to platform acceleration \ddot{z} . A vertical black line indicates frequency ω_{PM50} at which the phase plot attained -130° .

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Table 3 provides an overview of the design parameters with corresponding lower bound (LB) and upper bound (UB) constraints. Next to the design parameter bounds, a maximum implementation cost can be implemented as a nonlinear constraint in which the optimization algorithm ensures that the sum of the different components does not exceed this maximum implementation cost. By subsequently performing this optimization for several different maximum implementation costs, the progression of the maximum achievable performance relative to the total implementation cost can be determined.

Table 3. Design parameters with their corresponding lower bound (LB) and upper bound (UB) constraints.

Design Parameter	LB	UB	Design Parameter	LB	UB
$i_{act,f}$	0	3	i _{act,r}	0	3
$b_{sen,z}$	0	1	$b_{sen,\ddot{z}}$	0	1
$b_{CL,z}$	0	1	$b_{CL,\ddot{z}}$	0	1
$K_{p,z,f}$	0	2	$K_{p,z,r}$	0	2
$T_{i,z,f}$	0	0.01	$T_{i,z,r}$	0	0.01
$T_{d,z,f}$	0	0.01	$T_{d,z,r}$	0	0.01
$K_{p,\ddot{z},f}$	0	0.05	$K_{p,\ddot{z},r}$	0	0.05
$T_{i,\ddot{z},f}$	0	0.01	$T_{i,\ddot{z},r}$	0	0.01
$T_{d,\ddot{z},f}^{J=J_{J}}$	0	0.01	$T_{d,\ddot{z},r}$	0	0.01

3.4. Genetic Algorithm Application

A Genetic Algorithm (GA) was deployed to optimize the 18 design parameters based on the non-linear objective function and according to the mixed-integer and non-linear constraints mentioned above. For this active car suspension application, the optimization was performed repeatedly with a changing constraint on the maximum cost varying from 0% to 100% in 14 equal steps. By allowing a higher maximum implementation cost in successive optimizations, more expensive and higher performing parts could be used. In this way, the different points of the Pareto front were determined. Table 4 depicts some of the key settings for the Genetic Algorithm.

Table 4. Genetic Algorithm settings.

Description	Value	Unit
Population size	200	individuals
Maximum calculation time	7200	seconds
Maximum number of generations	infinite	generations
Function tolerance	1^{-10}	_ /
Maximum stall generations	10	generations
Crossover fraction	40	%
Elite count	20	individuals

Increasing the population size enables the Genetic Algorithm to search more points in one generation. However, the larger the population size, the longer the genetic algorithm takes to compute each generation. A population size of 300–500 individuals is suggested for the type of co-design optimization problems described in this paper. Successive generations are calculated iteratively using three "reproduction functions": "elite selection", "crossover", and "mutation". "Elite count" indicates how many individuals go directly and unchanged to the next generation through elite selection. This value is usually around 10–20 for this type of optimization problem [37]. The rest of the GA children are determined via crossover and mutation. A crossover child is formed by randomly combining variables from two parent individuals. A mutation child is created by randomly making small changes in the variables of a parent individual. The "crossover fraction" value specifies the fraction of the remaining children determined via crossover (and not via mutation).

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For optimization problems with a discontinuous objective function, it is recommended to set the crossover fraction low [38]. In this way, a relatively large number of mutations occur when determining the children, resulting in a broad search space for subsequent generations, preventing the optimization algorithm from prematurely ending up in a local minimum. An appropriate "crossover fraction" value is 0.4 for co-design optimization problems described in this paper. Refer to [39] for more in-depth information on the technical operation of a Genetic Algorithm. The optimization took approximately 8 hours and 18 minutes on an Intel[®] Xeon[®] CPU @ 3.10 GHz with 64 GB of RAM.

4. Results and Measurements

4.1. Model-Based Pareto Optimizations

Table 5 shows the results for every Pareto point optimization. As more implementation costs are allowed, actuators with higher torque outputs can be applied, resulting in better fitness values, and thus, better system performances. Each point contains an optimized situation depending on the implementation cost. It will be up to the design engineer to make a final decision on which Pareto point is most appropriate for the specific application. None of the Pareto-optimized points contain a position feedback control. Thus, these results show that applying a position feedback control gives no added value to the intended objective. This is also why the last Pareto point does not have a cost of 100%. The resulting Pareto front is shown in blue in Figure 9 and provides a valuable understanding of the trade-off between the performance and the implementation cost.

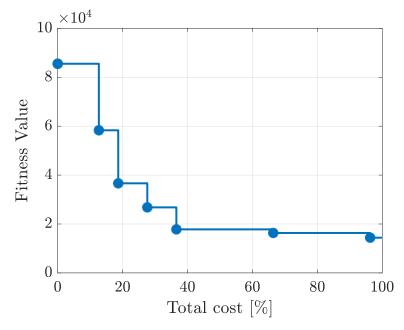


Figure 9. Pareto front representing the active car suspension model optimization results, showing the maximum achievable performance related to the implementation cost.

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Pareto Point	Cost [%]	Fitness Value []	$[i_{act,f},$ $i_{act,r}]$	$[b_{sen,z},\ b_{sen,\ddot{z}}]$	$[b_{CL,z},\ b_{CL,\ddot{z}}]$	$[K_{p,\bar{z},f},$ $T_{i,\bar{z},f},T_{d,\bar{z},f}]$	$[K_{p,\bar{z},r},$ $T_{i,\bar{z},r},T_{d,\bar{z},r}]$	$[K_{p,z,f}, \dots \\ T_{i,z,f}, T_{d,z,f}]$	$[K_{p,z,r},$ $T_{i,z,r}, T_{d,z,r}]$
0	0	85,526	[0, 0]	[0, 0]	[0, 0]	[0, 0, 0]	[0, 0, 0]	[0, 0, 0]	[0, 0, 0]
1	12.7	58,318	[0, 1]	[0, 1]	[0, 1]	[0, 0, 0]	[0.040, 0.006, 0.009]	[0, 0, 0]	[0, 0, 0]
2	18.7	36,633	[1, 1]	[0, 1]	[0, 1]	[0.042, 0.003, 0.008]	[0.048, 0.001, 0.009]	[0, 0, 0]	[0, 0, 0]
3	27.6	26,795	[1, 2]	[0, 1]	[0, 1]	[0.043, 0.005, 0.004]	[0.036, 0.007, 0.007]	[0, 0, 0]	[0, 0, 0]
4	36.6	17,800	[2, 2]	[0, 1]	[0, 1]	[0.049, 0.09, 0.003]	[0.049, 0.007, 0.008]	[0, 0, 0]	[0, 0, 0]
5	66.4	16,332	[3, 2]	[0, 1]	[0, 1]	[0.048, 0.009, 0.009]	[0.043, 0.004, 0.007]	[0, 0, 0]	[0, 0, 0]
6	96.3	14,404	[3, 3]	[0, 1]	[0, 1]	[0.05, 0, 0.01]	[0.05, 0.01, 0.01]	[0, 0, 0]	[0, 0, 0]

Table 5. Model-based Pareto front optimization results (rounded).

4.2. Validation Measurements

The results of the model-based Pareto optimizations were validated with measurements on the physical laboratory setup. For each hardware and control combination of Table 5, the system response to the same road disturbance signals was measured. Appendix A details the differences between the model-based calculated responses and the actual measured responses for each Pareto point, see Figures A1–A14 and Tables A1–A7. Figure 10 depicts the platform acceleration \ddot{z} measurements for every Pareto-optimized point configuration. The progression of the graphs clearly shows that the measured accelerations decrease as a higher maximum implementation cost is allowed. Figure 11 depicts the difference in platform accelerations \ddot{z} measurements between no active actuation and the optimized active actuation from Pareto point 6. The figure shows that the largest acceleration spike decreased from -566 to -63 mm/s², which is a reduction of 89%. This means that a significant increase in driver's comfort can be achieved using the optimized active car suspension, which is also represented in the corresponding fitness values.

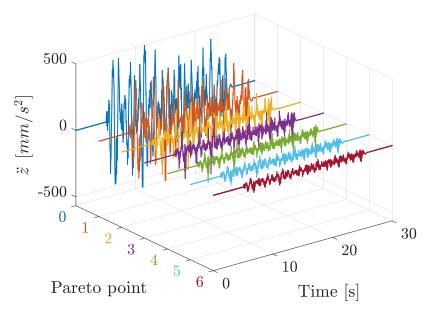


Figure 10. Measured platform acceleration \ddot{z} for every Pareto-optimized point configuration.

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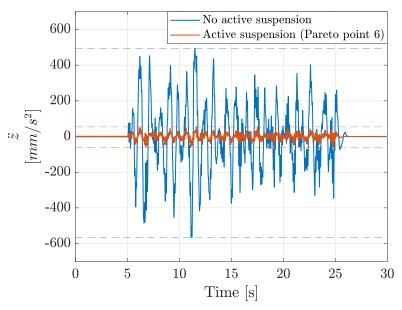


Figure 11. Comparison of the measured platform acceleration \ddot{z} for no active actuation (blue) and with optimized active actuation (red) from Pareto point 6 for the same road disturbance signals.

Figure 12 shows a comparison of the calculated and measured front and rear wheel actuator outputs u_f and u_r and platform acceleration signals \ddot{z} for a part of the time-domain response for Pareto point 6, demonstrating that the calculated and measured responses match well. Table 6 shows the fitness values for the validation measurements. These validation measurement results are depicted together with the model-based Pareto optimization results in Figure 13. The calculated and measured fitness values show better agreement as more co-design features are allowed and the implementation cost rises. Although the individual measured fitness values for configurations with smaller implementation costs do not match the model-based calculated fitness values, the overall trend is similar to that of the calculated fitness values. Therefore, conclusions on the hardware and control co-design based on the model-based optimization values will still be valid on the physical setup. The differences mentioned above can be attributed to modeling errors (e.g., friction or non-linear system behavior) and inherent measurement noise levels in the actual setup rather than limitations of the optimization algorithm.

Table 6. Fitness values for the model-based optimization results and the validation measurements.

Pareto Point	Cost [%]	Model-Based Optimization Fitness Value []	Validation Measurement Fitness Value []		
0	0	85,526	156,349		
1	12.7	58,318	100,677		
2	18.7	36,633	46,322		
3	27.6	26,795	33,926		
4	36.6	17,800	20,448		
5	66.4	16,332	17,489		
6	96.3	14,404	15,106		

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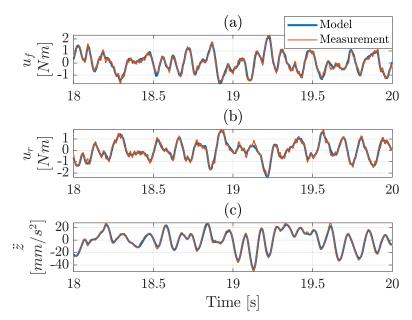


Figure 12. Comparison of the calculated (blue) and measured (red) time-domain responses for the front wheel actuator output u_f (**a**), rear wheel actuator output u_r (**b**), and platform acceleration \ddot{z} (**c**) for the validation measurement of Pareto point 6. The actuator outputs $u_{...}$ consist of the road disturbance signals $d_{...}$ and the control effort signals $f_{...}$.

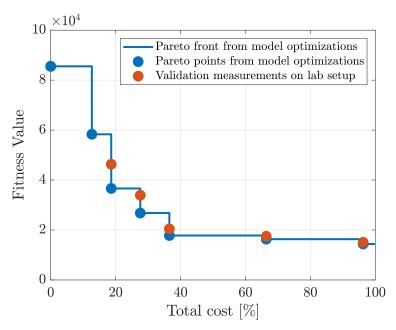


Figure 13. Comparison of the Pareto front results (blue) from the model-based co-design optimization methodology and the Pareto point validation measurements on the physical lab setup (red).

4.3. Comparison to Existing Controller Tuning Methods

The optimized controller values are compared here to existing controller tuning methods to validate the optimized acceleration controller tuning parameters as part of the control configuration optimization. First, the obtained controller tuning is compared to an LQR feedback design. In an LQR control design, relative weights are given to the state and input variables by adjusting the diagonal matrix Q and R values, respectively. Based on these values, a cost function minimization routine determines the values of the feedback matrices [15]. Thus, the LQR controller design comes down to adjusting the weights of the Q and R matrices according to the desired system behavior. However, for this application,

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a typical starting value of 1, applying the Bryson method [40], and manual adjustments of the Q and R diagonal matrices did not lead to a feasible solution. Thus, it was found that applying an LQR feedback control loop always leads to an unstable system, which is not the case with the controllers from the presented co-design methodology.

Furthermore, an existing controller tuning method was applied in which the P and PI controller values were determined based on the intended phase margins of the measured Bode plots [41]. This measured model is further denoted as G. The controller tuning method was applied to obtain P acceleration controllers with intended phase margins ϕ_{PM} equal to 30°, 60°, and 90°. Figure 14 shows the Bode plot of the identification measurements for G in which the frequencies $\omega_{P,PM30}$, $\omega_{P,PM60}$, and $\omega_{P,PM90}$ for phase margins of 30°, 60°, and 90°, shown with black vertical lines. The corresponding $K_{p,P,PM30}$, $K_{p,P,PM60}$, and $K_{p,P,PM90}$ values are obtained by compensating for the differences in the magnitude ratio at $\omega_{P,PM30}$, $\omega_{P,PM60}$, and $\omega_{P,PM90}$, respectively. Thereafter, each P controller was tested on the physical laboratory setup with different actuator types for a comparison with the obtained Pareto points from the co-design optimization methodology. Table 7 shows the results for the existing P controller tuning method and the corresponding validation measurements.

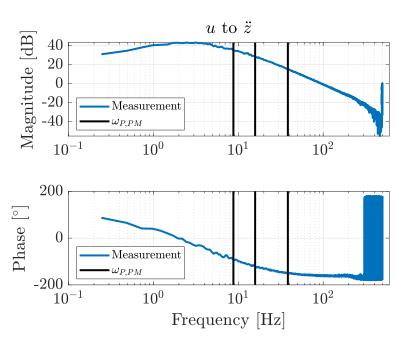


Figure 14. Bode plot of the identification measurements from system inputs u to platform acceleration \ddot{z} with frequencies ω_{PM30} , ω_{PM60} , and ω_{PM90} shown in vertical black lines to define the corresponding P controller values.

Table 7. Existing P controller tuning and validation measurement results for different phase margins. The fitness values for unstable system configurations are denoted by "/".

Phase Margin (ϕ_{PM})		30°			60°			90 °		
$\angle G(j\omega_{P,PM})$		-150°			−120°			−90°		
$\omega_{P,PM} [Hz]$	38.28				15.8			8.76		
$ G(j\omega_{P,PM}) [dB]$	15.2				28.38			35.16		
$K_{p,P,PM}$	$10^{-15.2/20} = 0.17$			10	$10^{-28.38/20} = 0.04$			$10^{-35.16/20} = 0.02$		
$[i_{act,f},i_{act,r}]$	[1,1]	[2,2]	[3,3]	[1,1]	[2,2]	[3,3]	[1,1]	[2,2]	[3,3]	
Cost [%]	18.7	36.6	96.3	18.7	36.6	96.3	18.7	36.6	96.3	
Fitness value (FV)	/	/	/	56,956	32,431	27,017	60,260	48,807	47,749	

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The same approach was used to obtain PI acceleration controllers with phase margins ϕ_{PM} of 30°, 60°, and 90° at corresponding frequencies $\omega_{PI,PM30}$, $\omega_{PI,PM60}$, and $\omega_{PI,PM90}$. A PI controller consists of a gain, a pole at the origin, and a zero [42]. The pole will cause a phase delay of -90° at the frequency $\omega_{PI,PM}$ at which the magnitude plot $|G(j\omega_{PI,PM})|$ crosses 0 dB. A zero causes a phase angle shift of $+90^{\circ}$ for infinitely high frequencies, but it is more realistic to design the controller requiring a phase shift of $+60^{\circ}$ at frequency $\omega_{PI,PM}$. With this knowledge, the frequency $\omega_{PI,PM}$ can be determined as:

$$\angle G(j\omega_{PI,PM}) - 90^{\circ} + 60^{\circ} = -180^{\circ} + \phi_{PM}.$$
 (9)

Figure 15 shows the Bode plot of the identification measurements in which the frequencies $\omega_{PI,PM30}$, $\omega_{PI,PM60}$, and $\omega_{PI,PM90}$ for phase margins ϕ_{PM} of 30°, 60°, and 90° are shown with black vertical lines.

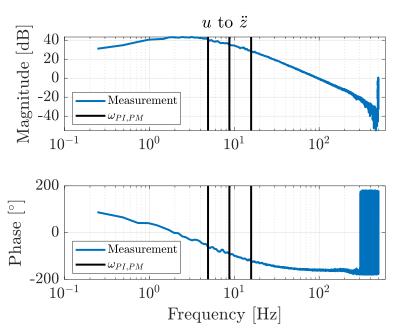


Figure 15. Bode plot of the identification measurements from system inputs u to platform acceleration \ddot{z} with frequencies ω_{PM30} , ω_{PM60} , and ω_{PM90} shown in vertical black lines to define the corresponding PI controller values.

Once frequency $\omega_{PI,PM}$ is defined, $T_{i,PI,PM}$ can be specified as:

$$\angle (1 + T_{i,PI,PM}s)|_{\omega = \omega_{PI,PM}} = 60^{\circ}, \tag{10}$$

from which the value of $T_{i,PI,PM}$ is found.

Finally, the value $K_{p,PI,PM}$ is determined so that the combined magnitude plot of the system and the PI controller intersects 0 dB at frequency $\omega_{PI,PM}$. The obtained PI acceleration controllers were also tested on the physical laboratory setup with different actuator types. Table 8 shows the results for the existing PI controller tuning method and the corresponding validation measurements.

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Phase Margin (ϕ_{PM})	Phase Margin (ϕ_{PM}) 30°						90°			
$\angle G(j\omega_{PI,PM})$		−120°		-90°			−60°			
$\omega_{PI,PM} [Hz]$	15.8				8.76			4.91		
$ G(j\omega_{PI,PM}) [dB]$	28.38			35.16			40.61			
$T_{i,PI,PM} \ K_{p,PI,PM}$		$tan(60^{\circ})/(15.8 \times 2\pi) = 0.017$ $10^{-30.6/20} = 0.030$			$tan(60^{\circ})/(8.76 \times 2\pi) = 0.032$ $10^{-39.17/20} = 0.011$			$tan(60^{\circ})/(4.91 \times 2\pi) = 0.056$ $10^{-45.35/20} = 0.054$		
$[i_{act,f}, i_{act,r}]$ $Cost [\%]$ Fitness value (FV)	[1,1] 18.7 57,396	[2,2] 36.6 35,146	[3,3] 96.3 30,643	[1,1] 18.7 61,144	[2,2] 36.6 51,611	[3,3] 96.3 51,049	[1,1] 18.7 64,982	[2,2] 36.6 59,839	[3,3] 96.3 59,761	

Table 8. Existing proportional integral (PI) controller tuning and validation measurement results for different phase margins.

The measured performances of these P and PI controller tuning methods are depicted as black circles in Figure 16. As shown in this figure, no classical controller tuning method achieved the performance obtained with the optimized values determined by the co-design methodology proposed in this paper.

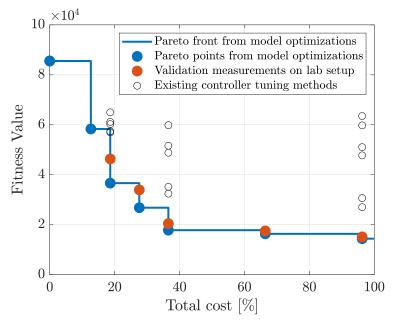


Figure 16. Comparison of the Pareto front results (blue) from the model-based co-design optimization methodology, Pareto point validation measurements of the physical laboratory setup (red), and measurements of existing controller tuning methods (black).

5. Conclusions

In this work, a novel co-design optimization methodology was applied to an active car suspension laboratory setup. Initially, the setup dynamics were identified by applying a prediction error minimization method to obtain a state-space system representation. Actuator force disturbance signals were determined to mimic a situation in which a car is driving over an actual road profile. The active components in the car suspension were used to reduce the central platform vibrations so that the driver's comfort was increased.

With the proposed co-design methodology, the optimal types and locations of actuators and sensors were determined simultaneously with the optimal control architecture and controller tuning parameters, exhibiting a profound level of co-design unprecedented in the current literature. This novel co-design methodology uses a Genetic Algorithm implementation, for which the results are presented in a Pareto front that graphically shows the interplay between the maximum achievable performance and the implementation

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cost. These results can be of great value to a design engineer in understanding how the maximum achievable performance varies as a function of the implementation cost.

The system configurations of the resulting Pareto points were validated with a physical laboratory setup. These validation measurements show that the obtained model-based trend in the Pareto front can also be observed in the corresponding measurements. The differences in the performances between the calculated and the measured situations can be attributed to the inherent measurement noise levels and modeling inaccuracies (e.g., friction or non-linear system behavior) rather than to errors in the co-design optimization methodology. Additionally, existing controller tuning methods were applied to the physical setup, and no existing method achieved the performance obtained with the proposed co-design methodology. This demonstrates that the presented co-design methodology is capable of determining the optimal controller tuning parameters.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A. Validation Measurements

Appendix A.1. Pareto Point 0 = No Active Car Suspension

Table A1. Model-based Pareto front optimization results for Pareto point 0 (rounded).

Pareto Point	Cost [%]	Fitness Value []	$[i_{act,f},$ $i_{act,r}]$	$[b_{sen,z},\ b_{sen,\ddot{z}}]$,	$[K_{p,\ddot{z},f},$ $T_{i,\ddot{z},f},T_{d,\ddot{z},f}]$			$[K_{p,z,r}, T_{i,z,r},T_{d,z,r}]$
0	0	85,526	[0, 0]	[0, 0]	[0, 0]	[0, 0, 0]	[0, 0, 0]	[0, 0, 0]	[0, 0, 0]

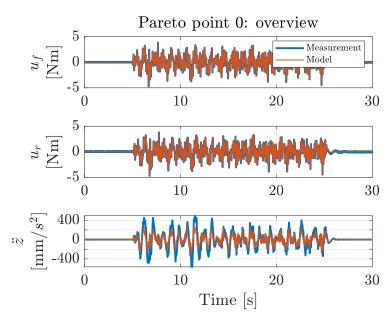


Figure A1. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 0.

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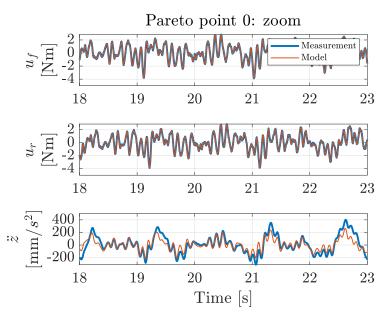


Figure A2. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 0.

Appendix A.2. Pareto Point 1

Table A2. Model-based Pareto front optimization results for Pareto point 1 (rounded).

Pareto Point		Fitness Value []	$[i_{act,f},$ $i_{act,r}]$			$[K_{p,\ddot{z},f}, T_{i,\ddot{z},f},T_{d,\ddot{z},f}]$	$[K_{p,z,r},$ $T_{i,z,r},T_{d,z,r}]$	$[K_{p,z,f}, \dots \\ T_{i,z,f}, T_{d,z,f}]$	
1	12.7	58,318	[0, 1]	[0, 1]	[0, 1]	[0, 0, 0]	[0.040, 0.006, 0.009]	[0, 0, 0]	[0, 0, 0]

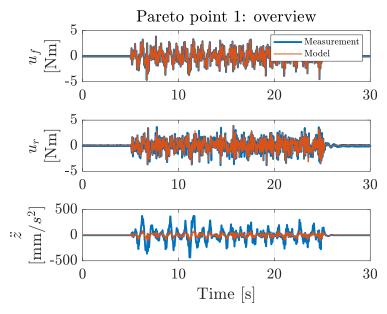


Figure A3. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 1.

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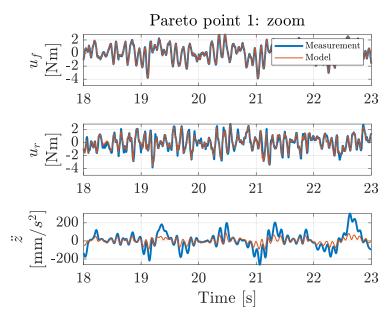


Figure A4. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 1.

Appendix A.3. Pareto Point 2

 Table A3. Model-based Pareto front optimization results for Pareto point 2 (rounded).

Pareto	Cost	Fitness	$[i_{act,f},$	$[b_{sen,z},$	$[b_{CL,z},$	$[K_{p,\ddot{z},f},$	$[K_{p,\ddot{z},r},$	$[K_{p,z,f},$	$[K_{p,z,r},$
Point	[%]	Value []	$i_{act,r}$]	$b_{sen,\ddot{z}}]$	$b_{CL,\ddot{z}}]$	$T_{i,\ddot{z},f},T_{d,\ddot{z},f}$	$T_{i,\ddot{z},r},T_{d,\ddot{z},r}$	$T_{i,z,f},T_{d,z,f}$	$T_{i,z,r},T_{d,z,r}$
2	18.7	36,633	[1, 1]	[0, 1]	[0, 1]	[0.042, 0.003, 0.008]	[0.048, 0.001, 0.009]	[0, 0, 0]	[0, 0, 0]

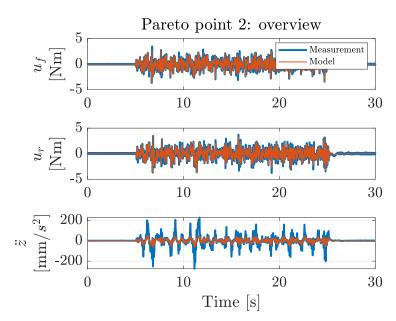


Figure A5. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 2.

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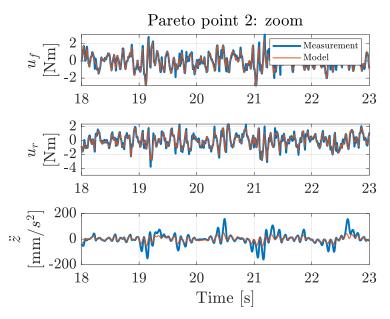


Figure A6. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 2.

Appendix A.4. Pareto Point 3

 Table A4. Model-based Pareto front optimization results for Pareto point 3 (rounded).

Pareto	Cost	Fitness	$[i_{act,f},$	$[b_{sen,z},$	$[b_{CL,z},$	$[K_{p,\ddot{z},f},$	$[K_{p,\ddot{z},r},$	$[K_{p,z,f},$	$[K_{p,z,r},$
Point	[%]	Value []	$i_{act,r}$]	$b_{sen,\ddot{z}}]$	$b_{CL,\ddot{z}}]$	$T_{i,\ddot{z},f},T_{d,\ddot{z},f}$	$T_{i,\ddot{z},r},T_{d,\ddot{z},r}$	$T_{i,z,f},T_{d,z,f}$	$T_{i,z,r},T_{d,z,r}$
3	27.6	26,795	[1, 2]	[0, 1]	[0, 1]	[0.043, 0.005, 0.004]	[0.036, 0.007, 0.007]	[0, 0, 0]	[0, 0, 0]

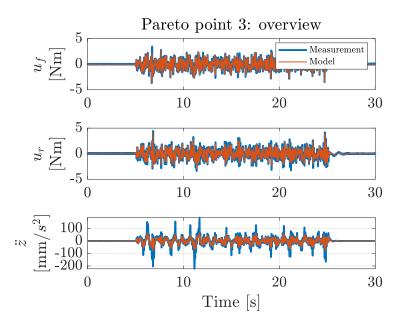


Figure A7. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 3.

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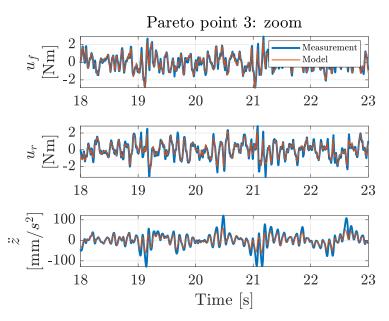


Figure A8. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 3.

Appendix A.5. Pareto Point 4

Table A5. Model-based Pareto front optimization results for Pareto point 4 (rounded).

				$\begin{bmatrix} b_{sen,z}, \\ b_{sen,\ddot{z}} \end{bmatrix}$			$[K_{p,\tilde{z},r},$ $T_{i,\tilde{z},r},T_{d,\tilde{z},r}]$	$[K_{p,z,f}, \dots \\ T_{i,z,f}, T_{d,z,f}]$	
4	36.6	17,800	[3, 2]	[0, 1]	[0, 1]	[0.049, 0.09, 0.003]	[0.049, 0.007, 0.008]	[0, 0, 0]	[0, 0, 0]

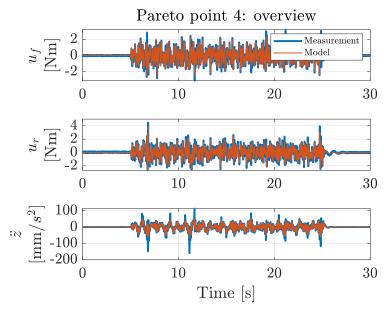


Figure A9. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 4.

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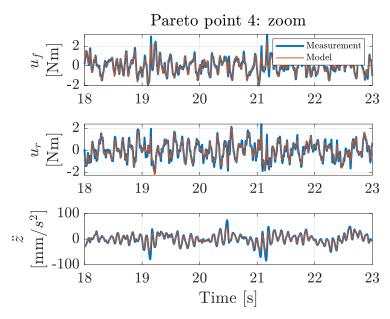


Figure A10. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 4.

Appendix A.6. Pareto Point 5

Table A6. Model-based Pareto front optimization results for Pareto point 5 (rounded).

				$[b_{sen,z},$			$[K_{p,\ddot{z},r},$	$[K_{p,z,f},$	
Point	[%]	Value []	$i_{act,r}]$	$b_{sen,\ddot{z}}]$	$b_{CL,\ddot{z}}]$	$T_{i,\ddot{z},f},T_{d,\ddot{z},f}$	$T_{i,\ddot{z},r},T_{d,\ddot{z},r}$	$T_{i,z,f},T_{d,z,f}$	$T_{i,z,r},T_{d,z,r}$
5	66.4	16,332	[2, 2]	[0, 1]	[0, 1]	[0.048, 0.009, 0.009]	[0.043, 0.004, 0.007]	[0, 0, 0]	[0, 0, 0]

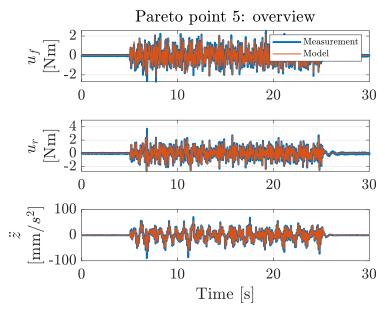


Figure A11. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 5.

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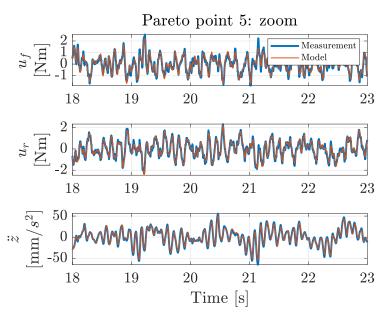


Figure A12. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 5.

Appendix A.7. Pareto Point 6

 Table A7. Model-based Pareto front optimization results for Pareto point 6 (rounded).

Pareto Point		Fitness Value []		$[b_{sen,z},\ b_{sen,\ddot{z}}]$		$[K_{p,\ddot{z},f},$ $T_{i,\ddot{z},f},T_{d,\ddot{z},f}]$	$[K_{p,\ddot{z},r},$ $T_{i,\ddot{z},r},T_{d,\ddot{z},r}]$	$[K_{p,z,f}, \dots \\ T_{i,z,f}, T_{d,z,f}]$	$[K_{p,z,r}, \dots \\ T_{i,z,r}, T_{d,z,r}]$
6	96.3	14,404	[3, 3]	[0, 1]	[0, 1]	[0.05, 0, 0.01]	[0.05, 0.01, 0.01]	[0, 0, 0]	[0, 0, 0]

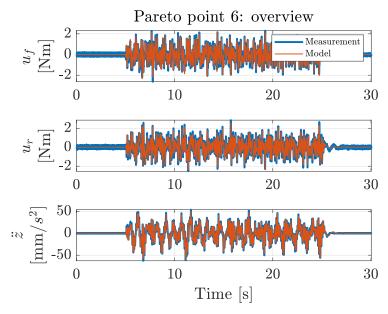


Figure A13. Overview of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 6.

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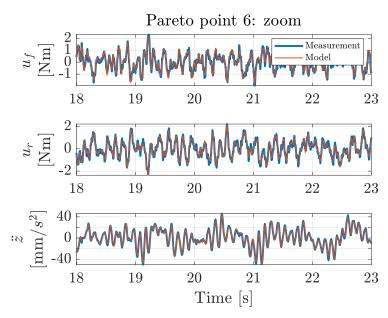


Figure A14. Zoom from 18 to 23 s of the front wheel actuator output u_f , rear wheel actuator output u_r , and platform acceleration \ddot{z} for the calculated model-based response (red) and the response measured in the physical setup (blue) for Pareto point 6.

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