



ANN-Based Pattern Recognition for Induction Motor Broken Rotor Bar Monitoring under Supply Frequency Regulation

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Abstract: The requisite of direct-on-line (DOL) starting for various applications in underground mines subjects the rotor bars of heavy-duty squirrel cage induction motors (SCIMs) to severe stresses, resulting in sustained fault in the rotor bars, unlike the applications where mostly reduced voltage starting is preferred. Furthermore, SCIMs working in underground mines are also affected by unforeseen frequency fluctuations. Hence, the paper proposes a discrete wavelet transform (DWT)based broken rotor bar detection scheme using the stator current analysis of SCIM when subjected to a frequency regulation ($\pm 4\%$ of 50 Hz supply) in steady-state, as prevalent in underground mines. In this regard, the level-seven detailed coefficient obtained by the DWT-based multi-resolution analysis of stator current corresponding to the healthy rotor is compared with that of the faulty rotor to extract the necessary features to identify the fault. Further implementation of the proposed scheme is done using artificial neural network (ANN)-based pattern recognition techniques, wherein both feed-forward backdrops and cascaded forward backdrop type ANNs have been used for fault pinpointing based on the feature extraction results obtained from DWT. The scheme is developed and analysed in MATLAB/Simulink using 5.5 kW, 415 V, 50 Hz SCIM, which is further validated using the LabVIEW-based real-time implementation.

Keywords: condition monitoring; discrete wavelet transforms; multi-resolution analysis; broken rotor bar; induction motor; frequency regulation



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1. Introduction

Pervasive applications, low cost, reasonably small size, ruggedness, and low maintenance requirement have made induction motor (IM) the mainstay of industrial prime movers. However, IMs are subjected to undesirable stresses, resulting in various faults, which may become catastrophic and severely hamper the production if not detected in incipient stages. Therefore, condition monitoring is indispensable for increasing machine availability, reducing consequential damage, and improving operational efficiency [1–3].

Of the various undesirable stresses that the IM is subjected to, a broken rotor bar is the most frequent fault that squirrel cage induction motors (SCIMs) encounter in underground coal mine scenarios. This is due to thermal, magnetic, residual, dynamic, mechanical, and environmental stresses arising from overload, supply unbalance, sparking, unbalanced magnetic pull, electromagnetic noise, vibration, manufacturing defects, unbalanced shaft torque, centrifugal forces, loose laminations, contamination, and abrasion [4–8]. Moreover, the rotor bars of heavy-duty SCIMs are stressed thermally and mechanically pertaining to the direct-on-line (DOL) start for various applications in underground coal mines, unlike their applications for serving other industrial needs, wherein mostly reduced voltage

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starting is preferred [9,10]. Hence, the detection of rotor bar cracks under a supply frequency regulation is exceptionally crucial for the machine's satisfactory working in the underground coal mines to minimise unwanted downtime.

Condition monitoring is primarily based on transient and steady-state analysis [11–25]. Traditional methods for monitoring the rotor health under steady-state conditions include the fast Fourier transform (FFT) based analysis of stator current [11], mechanical vibration [12], axial leakage flux [9], and rotor speed [13]. One of the significant drawbacks of these schemes [9,11–13] is their non-applicability to non-stationary signals since FFT is incapable of providing simultaneous time-frequency spectrum analysis [14]. Hence, [9,11–13] the fault detection process is miscarried under a frequency regulation, which is a widespread phenomenon in any practical application. Furthermore, another technique is short-time Fourier transform (STFT), which has been in relative use for possible monitoring of non-stationary current and vibration signals. However, STFT suffers from a major drawback in which it severely affects the resolution of the signal. This is due to the fact that the window length of the STFT remains constant throughout the time duration of the signal [14]. The discrete wavelet transform (DWT)-based techniques effectively analyse different spectrums under both the steady-state and start-up transient of an IM, thus establishing DWT-based techniques' suitability over the FFT- and STFT-based techniques for the rotor fault detection in SCIM [10].

Several cage fault detection techniques based on wavelet transform (WT) have been used recently [16-25]. The WT-based cage fault detection scheme of soft starter operated motors in the transient state is reported in [16], whereas [17] proposes a spectrum 'synth' technique for the detection of the cage and bearing faults in IM. Furthermore, the authors of [18] have analysed the motor start-up current using the wavelet approximation signal that isolates a characteristic component in the case of a broken rotor bar. Authors [19,20] also highlight outer cage fault detection schemes for double cage IM in the transient regime and the drawbacks associated with traditional techniques. All these WT-based methods [16,18–20] overcome the primary disadvantage of FFT, i.e., non-applicability in transient state. The rest of the literature [21-25] are situation-centric approaches. Such as the continuous WT-based rotor fault detection scheme [21], recursive wavelet packet technique, and directed acyclic graph support vector machines, which are employed to classify various IM faults [22]. The impact of axial cooling ducts, analysis of texture characteristics, feature extraction, and pattern classification using DWT-based techniques for the rotor fault detection in IM are discussed in [23-25]. These WT-based approaches discussed so far have not reported their applicability for non-stationary signals in a steady state.

Moreover, all these DWT-based approaches are complex and computation-intensive. Furthermore, many researchers have dedicated the artificial neural network (ANN) in the recent past towards the design of an effective fault detection algorithm [26–29]. The works done in [26,27] deploy convolutional neural networks with an inherent adaptive design for the fusion of feature extraction and classification phases of the fault detection into a single learning body. Furthermore, the authors of [28] concentrate on stator winding fault detection using a fuzzy detection system. Moreover, a comprehensive review of ANN-based techniques used to detect bearing damage and broken rotor bars is presented in [29]. Herein, vibration signals are used for feature extraction, followed by a hybrid feature reduction technique. It is evident from the recent research that while some of the works employ FFT for feature extraction, which makes it non-applicable in a transient state, the rest of the work uses the hybrid method on ANN, which is likely to make the computational process highly cumbersome. This, in turn, is likely to make the algorithm execution feature more sluggish.

Furthermore, the excessive use of instrumentation system based filter banks, spectrum analysers, and fuzzy logic approaches make the schemes used in the past highly computation intensive and cumbersome [11–25]. This is highly undesirable in certain hazardous work environments such as underground mines.

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Hence, the present work's objective is to propose a simple DWT-based SCIM cage fault detection scheme robust to supply the frequency regulation in underground coal mines. The multi-resolution analysis (MRA) of motor line current signal is employed in the proposed fault detection scheme for the feature extraction using stator current signatures. In this regard, the drawbacks of FFT-based analysis are also examined. The work shows that with the choice of proper mother wavelet and sampling frequency, it is possible to detect the rotor bar crack even by analysing the level-seven detailed coefficient (i.e., [d₇]) of DWT under a steady-state frequency regulation. Furthermore, a three-layer ANN of both feed-forward backdrop type and cascade forward backdrop type is examined using different algorithms to design an effective and fast ANN using pattern recognition and curve fitting. The proposed study is carried out in MATLAB/Simulink using 5.5 kW SCIM. The LabVIEW-based real-time implementation is also done as a validation of the proposed fault detection scheme. This proposed approach's execution requires a minimum instrumentation system compared to the schemes and algorithms used in the available and presented literature [11–25], which is highly desirable for the scheme's reliable working under dusty and hazardous mine environments.

2. Modelling of Rotor Bar Crack Fault

This section presents the rotor bar crack fault simulation for variable frequency fed SCIM using the winding function model.

2.1. Winding Function Theory-Based Modelling of SCIM

The winding function theory [30] considers that both stator and rotor consist of multiple inductive circuits coupled together, and the current in each circuit is assumed to be an independent variable. Figure 1a shows the current distribution in the rotor loops. The overall machine model can be represented as:

Stator voltage :
$$[V_S] = [R_S][I_s] + \frac{d}{dt}[\phi_s] \eqno(1)$$

$$\mbox{Rotor voltage}: \ [0] = [R_r][I_r] + \frac{d}{dt}[\phi_r] \eqno(2)$$

$$Stator\ flux:\ [\phi_S] = [L_s][I_s] + [L_{sr}][I_r] \eqno(3)$$

$$Rotor\ flux:\ [\phi_r] = [L_{sr}][I_s] + [L_r][I_r] \eqno(4)$$

Electromagnetic torque :
$$T_{em} = [I_s]^T \left[\frac{d}{d\theta_r} L_{sr} \right] [I_r]$$
 (5)

Elements of inductance matrices are :
$$L_{ij} = \left(\frac{\mu_0 lr}{g}\right) \oint_0^{2\pi} N_I(\theta_r,\phi) N_J(\theta_r,\phi) d\phi \quad \ (6)$$

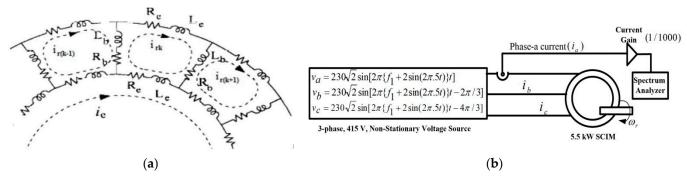


Figure 1. Simulation and modelling of SCIM: (a) Current distribution in rotor loops using the winding function theory, and (b) block diagram of MATLAB/Simulink model of variable frequency voltage fed SCIM.

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For sinusoidal distribution of stator windings, the winding functions for the three phases are given as:

$$N_{a}(\theta_{r},\phi) = \frac{N_{s}}{2p}\cos(p\phi) \tag{7} \label{eq:7}$$

$$N_{a}(\theta_{r}, \varphi) = \frac{N_{s}}{2p} \cos\left(p\varphi - \frac{2\pi}{3}\right) \tag{8}$$

$$N_{a}(\theta_{r}, \varphi) = \frac{N_{s}}{2p} \cos\left(p\varphi + \frac{2\pi}{3}\right)$$
 (9)

where the effective number of turns of the stator winding is $N_S = \frac{4}{\pi}NK_dK_pK_s$ and the actual number of turns of windings is $N_{S1} = pN_{tsp}N_{spp}$.

For the rotor, the winding function of each rotor loop can be written as:

$$N_{k}(\theta_{r}, \varphi) = \begin{cases} -\frac{\alpha_{r}}{2\pi}, & 0 < \varphi < \theta_{k} \\ 1 - \left(\frac{\alpha_{r}}{2\pi}\right), & \theta_{k} < \varphi < \theta_{k+1} \\ -\frac{\alpha_{r}}{2\pi}, & \theta_{k+1} < \varphi < \theta_{k} \end{cases}$$
(10)

Based on the above winding function theory, the final expressions of the inductances for stator and rotor circuits are given as:

$$L_{a} = L_{b} = L_{c} = \left(\frac{N_{s}}{2p}\right)^{2} \left(\frac{\pi\mu_{0Lr}}{g}\right) = L_{ms}$$

$$(11)$$

$$L_{ab} = L_{bc} = L_{ca} = -\left(\frac{N_s}{2p}\right)^2 \left(\frac{\pi\mu_{0Lr}}{2g}\right) = -\frac{L_{ms}}{2}$$
 (12)

$$L_{kk} = \left(\frac{\mu_0 Lr}{g}\right) \left(1 - \frac{\alpha_r}{2\pi}\right) \alpha_r \tag{13}$$

$$L_{k1....ki} = -2\pi \left(\frac{\mu_0 Lr}{g}\right) \alpha_r^2 \tag{14}$$

$$L_{ak} = L_m \cos(p(\theta_r + (k-1)\alpha_r + \delta))$$
 (15)

$$L_{bk} = L_{m} \cos \left(p(\theta_{r} + (k-1)\alpha_{r} + \delta) - \frac{2\pi}{3} \right)$$
 (16)

$$L_{bk} = L_m \cos \left(p(\theta_r + (k-1)\alpha_r + \delta) + \frac{2\pi}{3} \right)$$
 (17)

The fault detection analysis as carried out in the preceding sections is done using the winding function model of SCIM.

2.2. Modelling of SCIM Subjected to Frequency Regulation

In practice, the supply frequency varies within 49.2–50.3 Hz (i.e., roughly by $\pm 1.5\%$ from 50 Hz, as mentioned in the Central Electricity Authority 2010 amendment). In this work, $\pm 4\%$ (worst case) regulation in the nominal frequency is generated by a slowly varying sine wave of frequency 5 Hz and amplitude 2 V in each of the three phases to generate a non-stationary supply (Figure 1b).

This three-phase, 415 V, non-stationary voltage is fed to the 5.5 kW SCIM as designed in MATLAB/Simulink using the winding function theory. The winding function theory is used to design SCIM in the present work pertaining to the simpler nature of the winding function model compared to the other existing models such as the d-q model. This shall make the computation process less complex. The scaled-down (1/1000) phase-a current spectrum (ia), in accordance with the prospective ratings of the spectrum analyser, is used for the proposed cage fault detection scheme.

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2.3. Modelling of Rotor Bar Crack

An occurrence of a broken/cracked rotor bar causes variation in the rotor core's magnetic properties pertaining to the changes in the air-gap properties. This upsurge of the magnetic flux linkages in the rotor bar has affected part of the machine's definite loading. This additional flux induces eddy currents in the rotor slots [8,14]. Consequently, the machine flux becomes asymmetrical, resulting in an introduction of fault resistance in the rotor circuit, affecting the motor line current spectrum [5]. The incremental rotor resistance ($R_{\rm inc}$) with the number of cracked bars can be mathematically expressed as [31]:

$$R_{inc} = \frac{n_b}{\left(\frac{N}{3}\right) - n_b} \frac{(2N_1)^2}{\frac{N}{3}} R_b$$
 (18)

In practice, the contiguous number of cracked bars (n_b) is considerably small compared to the number of rotor bars (N). Hence, (1) can be approximated as [32,33]:

$$R_{\rm inc} = \frac{3n_b}{N} \frac{(2N_1)^2}{\frac{N}{3}} R_b \tag{19}$$

Since $n_b << N$ and the machine are not run in the underground mining setup, it is sent for maintenance as soon as even one damaged bar is detected, hence, (2) is quite applicable for the modelling of cracked rotor bars in the present work.

3. Simulation Results

The present section deals with the FFT, DWT, and ANN results obtained using the designed simulation model.

3.1. FFT-Based Analysis

The crack in the rotor bar is ultimately reflected as side-band frequencies around the principal slot harmonics in the stator current spectrum. These are given as [34]:

$$f_{lsb} = f_1(1-2s)Hz$$
 (20)

$$f_{usb} = f_1(1+2s)Hz$$
 (21)

Otherwise, the side-band frequencies (f_{sb}) around the higher-order slot harmonics can be obtained as [35]:

$$f_{sb} = f_1 \left\{ \frac{k}{p} (1 - s) \pm s \right\} Hz$$
, where, $\frac{k}{p} = 1, 2, ...$ (22)

MCSA using FFT is done on the phase-a current signal in MATLAB/Simulink in the following sub-sections [36].

3.1.1. Choice of Sampling Frequency

It is observed that the 6.25 kHz sampling frequency generates prominent side-bands (12) around the principal slot harmonics. Hence, initially, the 6.25 kHz sampling frequency is chosen for the FFT analysis of the phase current. However, it is presented later that the sampling frequency varying in the range of 6.1–6.35 kHz provides similar results.

3.1.2. Analysis of Stationary Current Signal Using FFT

Figure 2a shows a scaled-down phase current signal of $5.5 \,\mathrm{kW}$ SCIM with one bar cage fault under constant frequency (50 Hz) and full load torque (35 Nm). Figure 2b shows the corresponding FFT spectrum, which illustrates the presence of dominant fault side-bands (f_{lsb} and f_{usb} appearing at 45 and 54 Hz, respectively) with 3.49 and 3.65% amplitudes w.r.t fundamental (i.e., 50 Hz). According to (14), dominant fault side-band magnitudes A_{lsb}

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and A_{usb} must occur within 45–47 and 53–55 Hz, respectively, depending on the 3–5% variation in the machine slip. Therefore, MCSA using FFT produces precise and expected outcomes under a constant frequency operation.

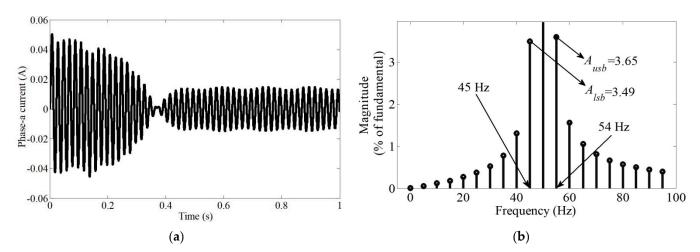


Figure 2. Analysis of rotor bar crack fault of a 5.5 kW SCIM (1 faulty bar) in stationary regime: (**a**) Phase-a current (i_a) with 50 Hz frequency, and (**b**) FFT spectrum of stationary i_a .

Similar tests have also been carried out with the motor, subjected to a stationary supply frequency, operating at 50% of rated load torque (i.e., 17.5 Nm), and the results obtained are similar to those obtained when the motor is running at a rated load torque.

3.1.3. Analysis of Non-Stationary Current Signal

In practice, the supply frequency does not remain constant. Moreover, it keeps varying by $\pm 1.5\%$ (approx.) around the fundamental frequency (50 Hz in the present case), resulting in a non-stationary current waveform. The Simulink model generates a typical scaled-down non-stationary phase-a current under a full load torque with $\pm 4\%$ frequency regulation (worst case) (Figure 1b) and is shown in Figure 3a.

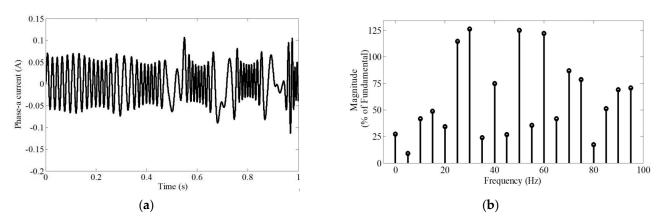


Figure 3. Analysis of rotor bar crack fault of a 5.5 kW SCIM (1 faulty bar) in non-stationary regime: (a) Phase-a current (i_a) with variable frequency, and (b) FFT spectrum of non-stationary i_a .

Figure 3b shows the corresponding FFT-based amplitude spectrum of the non-stationary phase current (Figure 3a) when fed to a SCIM under a cage fault operating at a rated load torque. Since no prevailing fault side-band amplitudes exist in Figure 3b as per (14) hence, the cage fault under such circumstances cannot be detected using the FFT analysis. This demands an alternative solution to detect the cage fault of SCIM under a frequency regulation in a steady state. The following sub-sections present the DWT-based MRA of motor line current spectrum. Moreover, similar tests have also been carried out with the motor, subjected to a

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non-stationary supply frequency, operating at 50% of rated load torque (i.e., 17.5 Nm), and the results obtained are similar to those obtained when the motor is running at the rated load torque.

3.2. DWT-Based MULTI-Resolution Analysis

The discrete wavelet transform (DWT)-based multi-resolution analysis (MRA) [37] decomposes a signal X[n] into several sub-bands known as detailed and approximated signals, with each corresponding to different frequency bands as [31]:

$$X[n] = \sum_{j} [a_n] \phi_j[n] + \sum_{n=1}^{L-1} \sum_{j} [d_n] \psi_{n,j}[n]$$
 (23)

where φ and ψ are the scaling function and mother wavelet, respectively, and n is the discrete sample number. In addition, $[a_n]$ and $[d_n]$ are the approximated and detailed coefficients, respectively that correspond to different frequency bands (in the present work) depending upon the scaling function and the mother wavelet defined as:

$$\varphi_i[n] = 2^{L/2} \varphi(2n - j) \text{ [i.e., scale of '2' which is shifted by 'j' samples]} \tag{24}$$

$$\Psi_{j}[n] = 2^{L/2} \Psi \left(2^{L} n - j \right) \left[\text{i.e., scale of '} 2^{L'}, \text{ also shifted by '} j' \text{ samples} \right]$$
 (25)

The MRA of the electrical signal can provide coincident information on the presence of a certain frequency component in the spectrum and the time of its occurrence. Therefore, the DWT-based MRA can be effectively used as an online condition monitoring tool.

3.2.1. Choice of Sampling Frequency for DWT Analysis

The frequency bands corresponding to the detailed and approximated signals at each level obtained using MRA are contingent upon the sampling frequency and the maximum number of decomposition levels. The corresponding frequency bands can be obtained as $[0,2^{-(L+1)}]$ and $[2^{-(n+1)}F_s,2^{-n}F_s]$, respectively [31].

Table 1 shows the numerical values of the frequency bands of the detailed and approximated signals for different sampling frequencies.

Table 1. Frequency	bands of [d _n]/	[a _n] for various sa	mpling	frequencies	[3.	IJ	•
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[4]/[-]	Sampling Frequency F _s (Hz)					
$[d_n]/[a_n]$	6100	6150	6200	6250	6300	6350
d_1	1525–3050	1537–3075	1550-3100	1562–3125	1575–3150	1588–3175
d_2	762-1525	769-1537	775-1550	781-1562	788-1575	794–1588
d_3	381-762	384-769	388-775	390-781	394-788	397-794
d_4	191-381	192-384	194-388	195-390	197-394	198-397
d_5	95-191	96-192	97-194	98-195	97-197	99-198
d_6	48-95	48-96	48-97	49-98	49-98	49-98
d_7	24-48	24-48	24-48	25-49	25-49	25-49
d_8	12-24	12-24	12-24	13-25	13-25	13-25
a ₈	0–12	0–12	0–12	0–13	0–13	0–13

As observed from Table 1, the desired side-band frequencies (i.e., 45–47 and 53–55 Hz as per (14)) in the line current spectrum for SCIM under cage fault lie in different detailed coefficients, i.e., $[d_7]$ and $[d_6]$ coefficients, respectively. This corresponds to the sampling frequencies in the range of 6100 to 6350 Hz. Isolation of fault frequency components in different detailed coefficients is highly desirable in contention with ambiguity-less fault detection. In practice, the sampling frequency may not remain fixed due to the sampler's variation of parameters. Hence, the analysis reveals that any sampling frequency within the specified range is suitable for the proposed fault detection scheme's satisfactory execution. However, in the present work, a 6250 Hz sampling frequency is used.

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3.2.2. Choice of Mother Wavelet and Number of Decomposition Levels

The choice of a suitable mother wavelet is a crucial aspect of the proposed DWT-based fault detection scheme. It is done by computing the correlation coefficients of a particular mother wavelet with the signal of interest [38]. It has been observed that the correlation coefficients as calculated for 'db41' with a stationary current signal and 'sym34' with a non-stationary current signal are 0.87 and 0.90, respectively, which are closest to unity in comparison to the other mother wavelets. Hence, 'db41' is used to analyse the stationary current signal, whereas 'sym34' is used to analyse the present work's non-stationary current signal.

Further, the number of maximum decomposition levels for the proposed scheme can be obtained as [39]:

$$L \ge \frac{\log\left(\frac{F_s}{f_1}\right)}{\log 2} + 1 \tag{26}$$

$$L = n_f + 2 \tag{27}$$

Based on (26) and (27), it is found that each of 'dB41' and 'sym34' with the 8th level of decomposition is sufficient to carry out MRA of both the stationary and non-stationary current signals, respectively.

3.2.3. Analysis of Stationary and Non-Stationary Current Signals by DWT for a Motor operating at Variable Load

Figure 4 shows the approximated and detailed coefficients for the 8th level decomposition of the phase-a current signal of stationary and non-stationary natures under both the healthy and faulty cases when the motor is operating at a rated load torque (i.e., 35 Nm). The analysis reveals that $[d_1]$ - $[d_5]$, $[d_8]$, and $[a_8]$ do not contain any substantial ripple in any case (Figure 4a–d), since the magnitudes of the other fault side-band frequencies around the other higher-order slot harmonics are progressively smaller and hence, are not reflected in $[d_1]$ - $[d_5]$, while $[d_8]$ and $[a_8]$ represent the low-frequency bands (less than the fundamental frequency).

Hence, these coefficients are not of great concern in the process of fault detection. On the contrary, the presence of significant undulations, as shown in Figure 4b,d, correspond to the frequency bands of 49–97 and 24–48 Hz, respectively, as per Table 1 under the faulty cage. Hence, it is established that the upper and lower side-band frequencies (54 and 45 Hz) around the principle slot harmonics (50 Hz) of line current spectrum lie in $[d_6]$ and $[d_7]$, respectively, during the cage fault. The amplitudes of variations in such cases are appreciably higher than those for the healthy cases, as shown in Figure 4a,c due to the presence of both the upper side-band and principal slot harmonics. Furthermore, Figure 4a,c shows the nonexistence of any variation of $[d_7]$, which indicates the absence of the lower side-band frequency around the principle slot harmonic under the healthy motor condition. In contrast, the variation as reflected in $[d_6]$ is similar (having lesser magnitude) to the faulty one (Figure 4b,d) owing to the presence of principal slot harmonics only.

Finally, there is a distinct difference in both the nature and amplitude of $[d_7]$ for the healthy and the faulty conditions of the SCIM (Figure 4). Therefore, the point-to-point standard deviation of $[d_7]$ is considered for the fault detection algorithm's edifice in the present work.

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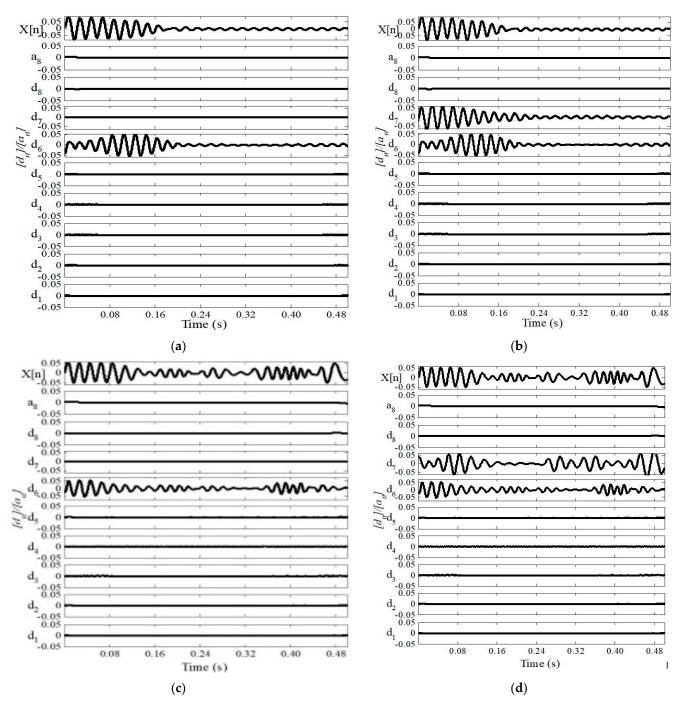


Figure 4. Approximated $[a_n]$ and detailed $[d_n]$ coefficients obtained by the DWT-based MRA of phase-a current of 5.5 kW SCIM running at a rated load torque: Under constant frequency operation: (a) In the absence of cage fault, (b) in the presence of cage fault, and under frequency regulation: (c) In the absence of cage fault, (d) in the presence of cage fault.

3.3. ANN-Based Analysis

It is evident from the results obtained in Section 3.2 that the instantaneous values of $[d_7]$ detailed coefficient are a good indicator of the broken/cracked rotor bar damage. Hence, the instantaneous values of the $[d_7]$ detailed coefficient are used for the training of the ANN. A three-layered ANN having 10 neurons in each layer is designed in the present work. Two types of ANN are designed and tested in the present work using cascaded forward backdrop and feed-forward backdrop-based designs, as shown in Figure 5a,b, respectively [14,27,29,31,40-45].

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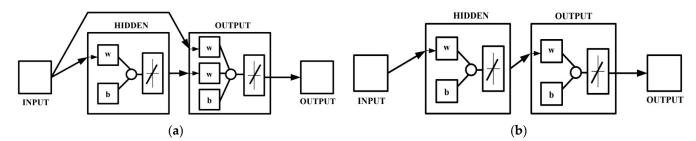


Figure 5. Artificial neural network design based on (a) cascaded forward backdrop and (b) feed-forward backdrop based design.

ANN training is done using four different algorithms: Bayesian Regulation, Polak-Ribiere Restarts, Gradient Descent with momentum and adaptive learning rate, and finally, Levenberg Marquardt algorithm. The pattern recognition technique is used to identify broken rotor bars using the value of coefficients of correlation (R) of curve fitting between the input and the target values. The main motive behind using the pattern recognition-based curve fitting technique is that it is one of the most trivial ways of identifying a curve pattern. Furthermore, the drastic difference in the nature of the curve corresponding to a faulty induction machine to that corresponding to a healthy induction machine makes the process of pattern recognition all the more effective. Moreover, the use of epochs to check the point of convergence is in direct contention with the fast detection of faults that is indispensible w.r.t. for the process of fault detection, as it helps minimise the damage of an induction machine due to prolonged subjection to a prospective fault. Figure 6 shows the pattern recognition-based curve fitting diagram for the different algorithms using the cascaded forward backdrop type of ANN.

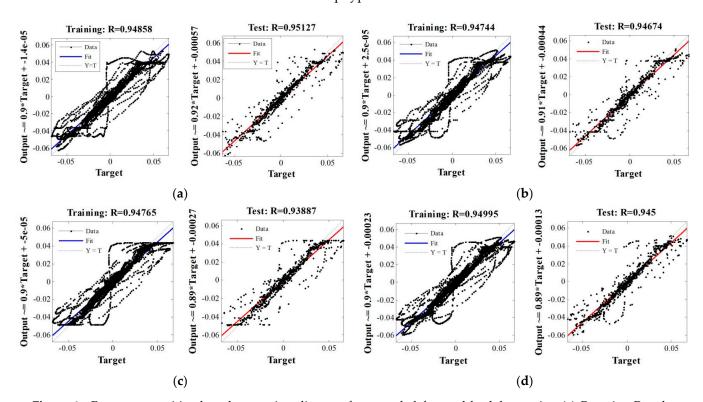


Figure 6. Pattern recognition-based regression diagram for cascaded forward backdrop using (a) Bayesian Regulation, (b) Polak-Ribiere Restarts, (c) Gradient Descent with momentum and adaptive learning rate, and (d) Levenberg-Marquardt Algorithm.

It is seen from Figure 6 that the maximum value of the coefficient of correlation is achieved for Bayesian Regulation. However, the choice of the apt algorithm for the

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proposed ANN cannot be made based solely on the value of the coefficient of correlation. Another critical factor in the selection of the algorithm is the epoch value of mean square error. The value of the mean square error for the different algorithms is shown in Figure 7. It is seen from Figure 7 that the mean square error reaches the minimum value at the earliest on Epoch 5 for the Lavenberg-Marquardt algorithm.

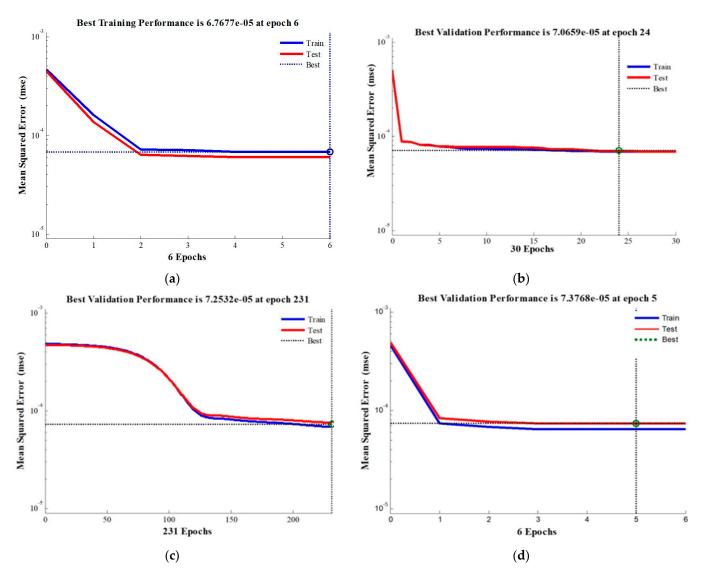


Figure 7. Mean square error diagram for cascaded forward backdrop using (a) Bayesian Regulation, (b) Polak-Ribiere Restarts, (c) Gradient Descent with momentum and adaptive learning rate, and (d) Levenberg-Marquardt Algorithm.

Based on the results obtained in Figures 6 and 7, it is inferred that both the Bayesian Regulation and Levenberg-Marquardt algorithm give highly satisfactory results in the present work. Furthermore, a similar test is done using the feed-forward backdrop type ANN, and the results are compiled in Figures 8 and 9 for the curve fitting diagram and mean square diagram, respectively.

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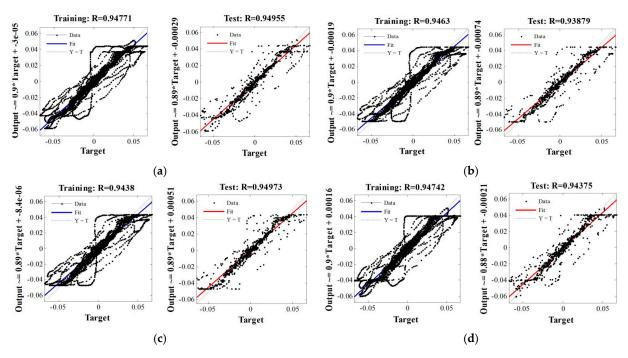


Figure 8. Pattern recognition based regression diagram for feed-forward backdrop using (**a**) Bayesian Regulation, (**b**) Polak-Ribiere Restarts, (**c**) Gradient Descent with momentum and adaptive learning rate, and (**d**) Levenberg-Marquardt Algorithm.

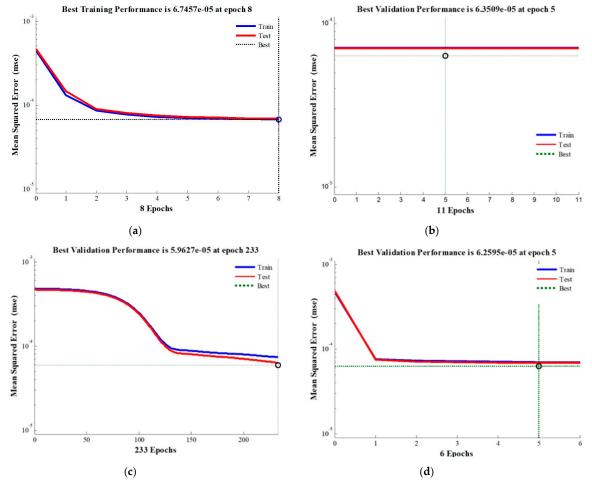


Figure 9. Mean square error diagram for feed-forward backdrop using (a) Bayesian Regulation, (b) Polak-Ribiere Restarts, (c) Gradient Descent with momentum and adaptive learning rate, and (d) Levenberg-Marquardt Algorithm.

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It is seen from Figures 8 and 9 that both Bayesian Regulation and Levenberg-Marquardt algorithm give highly satisfactory results both in terms of the values of coefficient of correlation and the mean square error values. The values of mean square errors and coefficient of correlation for the different algorithms are further tabulated in Table 2.

	Correlation Coefficient Value (R)		Mean Square Error Epoch Value	
-	Cascaded Forward Backdrop	Feed-Forward Backdrop	Cascaded Forward Backdrop	Feed-Forward Backdrop
Bayesian Regulation	0.95127	0.94955	6	8
Polak-Ribiere Restarts	0.945	0.95373	24	5
Gradient Descent with momentum and	0.94557	0.95264	231	233
adaptive learning rate	0.74337	0.73204	251	233
Levenberg-Marquardt	0.94935	0.94925	5	5

Table 2. Values of mean square errors and regression for the different algorithms.

It is clear from the values encapsulated in Table 2 that the best results in terms of coefficient of correlation, mean square error, and epoch value are obtained using the Levenberg-Marquardt algorithm. Moreover, it is also seen that the obtained values are better in the case of the cascaded forward backdrop type of ANN than compared to the feed-forward backdrop type of ANN. Hence, the cascaded forward backdrop type ANN with Levenberg-Marquardt algorithm is used in the present work for the detection of broken rotor bars using pattern recognition and curve fitting.

3.4. Modelling of DWT-Based Fault Detection Scheme

Figure 10 shows the scheme representative of both the simulation model and experimental setup for DWT- and ANN-based cage fault detection of SCIM.

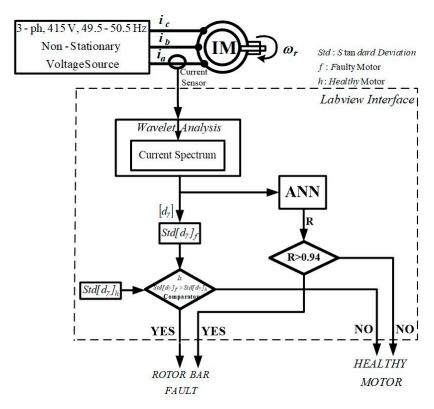


Figure 10. Scheme for DWT- and ANN-based cage fault detection of SCIM.

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A three-phase, 415 V, $50 \pm 1.5\%$ Hz non-stationary source is fed to the SCIM. The scaled-down (1/1000) current of phase-a (i_a) is used for MRA in the simulation study. In addition, 'dB34' is used for scrutinising stationary signals in the 'wavelet analysis' block. The point-to-point standard deviation of [d_7] obtained from the 'wavelet analysis' block is compared with the pre-fed values of the standard deviation of [d_7] obtained by analysing the healthy motor state in the 'comparator' block. The standard deviation of [d_7] obtained from the motor with a faulty cage running in real-time is consistently higher than that of the motor in a healthy state, which indicates the presence of a fault. Furthermore, the instantaneous values of the [d_7] detailed coefficient are fed to the 'ANN' block, wherein the cascaded forward backdrop-based design has been adopted, and the execution is done using the Levenberg-Marquardt algorithm. The value of the coefficient of correlation (R) obtained from the ANN block is fed to a comparator block which checks whether the value of R value is more than 0.94. A value greater than 0.94 indicates damaged rotor bars, whereas a lesser value indicates a healthy rotor bar. This is justified based on the values obtained in Table 2.

4. Real-Time Validation

This section details the real-time validation of the proposed cage fault detection scheme in the LabVIEW-based SCIM laboratory prototype.

4.1. LabVIEW-Based Laboratory Prototype

The LabVIEW-based laboratory prototype for cage fault detection of 5.5 kW, three-phase, 415 V, 4 pole SCIM (Appendix A) is shown in Figure 11. The motor line current is sensed in the sensing module using LEM current sensors (0–5 A). This line current is filtered, discretised, and further digitised using an A/D converter in the data acquisition card (11–30 V (dc), 30 W) for feeding into the LabVIEW interface. The real-time code corresponding to Figure 10 is generated in LabVIEW. The cage fault detection algorithm is implemented using the acquired data. A sampling frequency of 6.2 kHz and 'sym34' mother wavelet (since the supply frequency constantly regulates by $\pm 1.5\%$, making the current signal non-stationary) are used to implement the fault detection algorithm.

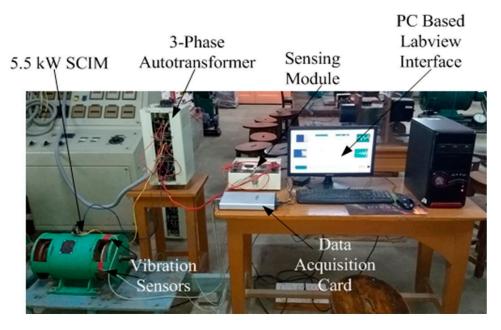


Figure 11. Experimental setup for the validation of the proposed fault detection scheme.

4.2. Results of Fault Detection

Figure 12 shows the experimental results obtained by the LabVIEW-based SCIM laboratory prototype to validate the simulation study. Moreover, the real-time signals

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are inherently non-stationary in nature due to the supply frequency regulation $\pm 1.5\%$ (approx.). Hence, the experimental validation for SCIM at the rated load torque (35 Nm) subjected to only the non-stationary signal at an operating sampling frequency of 6.2 kHz is presented.

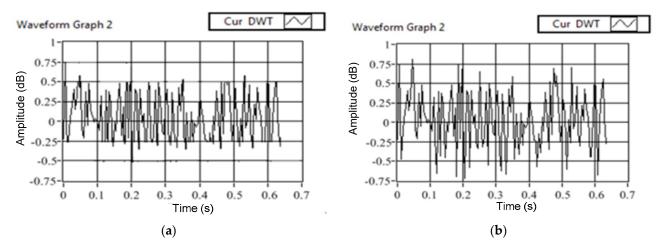


Figure 12. The $[d_7]$ coefficient for SCIMs operating at a rated load torque obtained using the LabVIEW-based laboratory prototype under (**a**) healthy state, and (**b**) faulty state.

Figure 12a shows the variation in the $[d_7]$ coefficient for SCIMs operating at a rated load torque under healthy conditions. The $[d_7]$ components in these cases show significantly lesser variations from the pre-fed values, a characteristic of the healthy machine. Furthermore, Figure 12b shows the $[d_7]$ coefficient for SCIMs operating at a rated load torque having broken rotor bars. It is evident that the deviation of the $[d_7]$ coefficient is much greater than those shown in Figure 12a.

Furthermore, Figure 13 shows the curve fitting-based pattern recognition diagram of ANN for the detection of broken rotor bars.

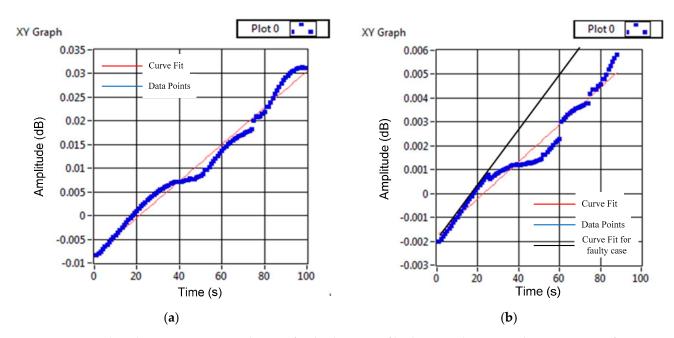


Figure 13. ANN-based pattern recognition diagram for the detection of broken rotor bars using the stator current for SCIM: (a) With broken rotor bars and (b) without broken rotor bars.

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The value of correlation coefficients for the SCIM in the faulty case is at 0.9536, and that for the healthy case is at 0.69, which further goes on to validate the proposed fault detection scheme (Figure 10).

5. Conclusions

The cage fault detection at an incipient juncture results in reducing the unwanted downtime of the drive system, especially in the underground mines. This paper proposes a two-tier approach using the DWT-based MRA of motor line current and ANN to detect the rotor bar crack for SCIMs operating under a supply frequency regulation, which is a common phenomenon in the Indian industrial scenario which leads to the presence of non-stationary signals as sources for the SCIM. The rigorous analysis in MATLAB/Simulink ensures that even the level-seven detailed coefficient [d₇] alone is sufficient to detect the rotor bar crack provided the analysing mother wavelet and working sampling frequency are selected accurately. In the present work, it is found that 'db41' is suitable for analysing the stationary current signal, whereas 'sym34' is the proper choice for the non-stationary current signal in the MRA. Furthermore, it is also observed that the use of cascaded forward backdrop type ANN using the Levenberg-Marquardt algorithm gives highly satisfactory results for the process of fault detection.

Moreover, pattern recognition and curve-fitting make the proposed scheme simplistic, robust, and less erroneous. The scheme is further validated by a real-time implementation on a LabVIEW-based 5.5 kW SCIM laboratory prototype. The proposed scheme is also robust to the $\pm 2\%$ (approx.) sampling frequency variation from the operating frequency. Implementing this proposed approach requires a minimum instrumentation system that is highly desirable for the scheme's reliable working under dusty and hazardous mine environments.

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Nomenclature

Description
Slip of the machine (%)
Supply frequency (Hz)
Number of pole pairs
Rotor speed (rad/s)
Rotor bar resistance (Ω), inductance (H)
Increase in rotor resistance (Ω)
End-ring resistance (Ω), inductance (H)
Turn number of one stator winding
Total number of rotor bars
Contiguous number of cracked bars
Higher-order slot harmonics
Stator voltage, rotor loop current matrices

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ID III 1	D () () () ()	
$[R_r][L_r]$	Rotor resistance, inductance matrices	
$\Phi_{\rm s}$, $\Phi_{\rm r}$	Total flux linkages of stator and rotor winding	
$\theta_{\mathbf{r}}$	Angular rotor position	
Φ	Particular point along the air-gap	
1	Effective length of the motor	
N_{tsp} , N_{spp}	Number of turns/slot/phase, number of slots/pole/phase	
$N_k (\theta_r, \varphi)$	Winding function of rotor windings	
L_a , L_b , L_c , L_{ab} , L_{bc} , L_{ca}	Elements of $[L_s]$	
$L_{k1} \dots L_{kk}$	Elements of $[L_r]$	
L_{ak} , L_{bk} , L_{ck}	Elements of $[L_{sr}]$	
$\theta_{\mathbf{k}}$	Angular position of bar 'k'	
A_{lsb} , A_{usb}	Lower, upper fault side-band amplitude (%)	
v_a, v_b, v_c	Voltages of phase-a, phase-b, phase-c (V)	
i_a , i_b , i_c	Currents of phase-a, phase-b, phase-c (A)	
F_s	Sampling frequency (Hz)	
t	Time (s)	
L	Number of decomposition levels	
n_f	Detailed coefficient containing 50 Hz	
f_{lsb} , f_{usb}	Lower, upper side-band frequency (Hz)	
$[I_s]$	Stator current vector	
$[R_s]$	Stator winding resistance matrix	
$[L_s]$	Stator winding inductance matrix	
$[L_{sr}]$	Stator to rotor mutual inductance matrix	
T_{em} , T_{L}	Electromagnetic, load torques (Nm)	
J	Rotor inertia (Kg-m ²)	
F	Coefficient of friction	
μ_0	Permeability of air	
r	Air-gap average radius (mm)	
N_s , N_{s1}	Effective, the actual number of turns of the stator winding	
g	Air-gap length (mm)	
$N_1 (\theta_r, \varphi), N_j (\theta_r, \varphi)$	Winding function of circuit <i>I</i> and <i>J</i>	
K_p, K_d, K_s	Pitch, distribution, skew factors	
N_a , N_b , N_c	Winding function of stator windings	
$\alpha_{\rm r}$	Angle between any two adjacent bars	
-	· ,	

Appendix A. Motor Parameters

Parameters	Ratings
Shaft power	5.5 kW
Rated voltage	415 V
Frequency	50 Hz
Synchronous speed	1500 rpm
Stator resistance/phase	1.83Ω
Stator inductance/phase	0.0074 H
Rotor resistance referred to stator/phase	1.26Ω
Rotor inductance referred to stator/phase	0.007 H
Mutual inductance	0.198 H
Number of stator slots	36
Number of rotor slots	28
Number of poles	4

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