

Supplementary Material

The film thickness ratio (λ) is used to estimate the lubrication regime under a specific lubrication system. In general, when $\lambda > 3$, the system is supposed to work in the hydrodynamic or elastohydrodynamic lubrication regime; when $3 \geq \lambda \geq 1$, the system works in the mixed lubrication regime; and when $\lambda < 1$, it is the boundary lubrication regime. The study is to investigate the tribological properties of PILs under a boundary lubrication regime, so the operating parameters in this research are well designed accordingly.

$$\lambda = \frac{h_{min}}{\sqrt{(R_1^2 + R_2^2)}}$$

In the formula up there, h_{min} is the minimum film thickness, and R_1 and R_2 are roughness of surfaces in contact. Regarding the elliptical contact, the following formulas that developed by Hamrock and Dowson have been used to calculate the minimum film thickness [1].

$$\frac{h_{min}}{R'} = 3.63U^{0.68}G^{0.49}W^{-0.073}(1 - e^{-0.68k})$$

$$U = \frac{\eta_0 u_0}{E'R'}$$

$$G = \alpha E'$$

$$W = \frac{F}{E'R'^2}$$

Among the parameters, R' is the effective radius, k is the ellipticity parameter, η_0 is the lubricant dynamic viscosity at atmospheric pressure and certain temperature, u_0 is the mean speed of the two contact surfaces, α is the pressure-viscosity coefficient at a certain temperature, and F is the normal load.

Table S1. Lubrication regime estimation for each lubricant at aluminum-steel contacts.

| Lubricant | $U \times 10^{-11}$ | G | W | k | $h_{\min} \times 10^{-9}$ | $\lambda \times 10^{-3}$ | Lubrication Regime |
|-----------------|---------------------|--------|-----------------------|-----|---------------------------|--------------------------|--------------------|
| BO | 1.47 | 1096.5 | 7.30×10^{-5} | 1 | 4.63 | 8.6 | Boundary |
| BOA | 1.49 | 1096.5 | 7.30×10^{-5} | 1 | 4.68 | 8.7 | Boundary |
| 1%Ets+BO | 1.56 | 1096.5 | 7.30×10^{-5} | 1 | 4.83 | 9.0 | Boundary |
| 1%Mts+BO | 1.55 | 1096.5 | 7.30×10^{-5} | 1 | 4.80 | 9.0 | Boundary |
| 1%Dts+BO | 1.54 | 1096.5 | 7.30×10^{-5} | 1 | 4.78 | 8.9 | Boundary |
| 1%Eds+BO | 1.70 | 1096.5 | 7.30×10^{-5} | 1 | 5.13 | 9.6 | Boundary |
| 1%Mds+BO | 1.69 | 1096.5 | 7.30×10^{-5} | 1 | 5.09 | 9.5 | Boundary |
| 1%Dds+BO | 1.92 | 1096.5 | 7.30×10^{-5} | 1 | 5.56 | 10.4 | Boundary |

1 Hamrock, B.J.; Dowson, D. Isothermal Elastohydrodynamic Lubrication of Point Contacts: Part III—Fully Flooded Results. *J. Lubr. Technol.* **1977**, *99*, 264–275. <https://doi.org/10.1115/1.3453074>.