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Review

The Vehicle Routing Problem: State-of-the-Art Classification and Review

Shi-Yi Tan and Wei-Chang Yeh *

Department of Industrial Engineering and Engineering Management, Integration and Collaboration Laboratory, National Tsing Hua University, Hsinchu 30013, Taiwan; s108034871@m108.nthu.edu.tw

* Correspondence: wcyeh@ie.nthu.edu.tw

Abstract: Transportation planning has been established as a key topic in the literature and social production practices. An increasing number of researchers are studying vehicle routing problems (VRPs) and their variants considering real-life applications and scenarios. Furthermore, with the rapid growth in the processing speed and memory capacity of computers, various algorithms can be used to solve increasingly complex instances of VRPs. In this study, we analyzed recent literature published between 2019 and August of 2021 using a taxonomic framework. We reviewed recent research according to models and solutions, and divided models into three categories of customerrelated, vehicle-related, and depot-related models. We classified solution algorithms into exact, heuristic, and meta-heuristic algorithms. The main contribution of our study is a classification table that is available online as Appendix. This classification table should enable future researchers to find relevant literature easily and provide readers with recent trends and solution methodologies in the field of VRPs and some well-known variants.

Keywords: vehicle routing problem; taxonomy; literature review; exact methods; heuristics; meta-heuristics

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1. Introduction

Problems related to the distribution of goods between warehouses and customers are generally considered as vehicle routing problems (VRPs). The VRP was first proposed by Dantzig and Ramser [1] in 1959 to model how a fleet of homogeneous trucks could serve the demand for oil from a number of gas stations from a central hub with a minimum travel distance. Five years later, Clarke and Wright [2] added more practical restrictions to VRPs in which the delivery of goods to each customer must occur within a set of bounds. This type of problem model became known as the VRP with time windows (VRPTW), which is one of the most widely studied topics in the field of operations research [3].

However, current VRP models differ significantly from those introduced by Dantzig and Ramser [1] and Clarke and Wright [2], because they aim to incorporate real-world complexities. Because VRPs are some of the most critical challenges faced by logistics companies, an increasing amount of research is focusing on VRPs. Several surveys and taxonomies for VRPs can be found in [3–6] ((Eksioglu et al. (2009); Braekers et al. (2016); Elshaer and Awad (2020); Konstantakopoulos et al. (2020)) and in many other books or book chapters [7–10] ((Cordeau et al. (2007); Golden et al. (2008); Toth and Vigo (2014)); Nalepa (2019)).

Solving VRPs is computationally expensive and categorized as NP-hard [11], because real-world problems involve complex constraints such as time windows, time-dependent travel times (reflecting traffic congestion), multiple depots, and heterogeneous fleets.

These features introduce significant complexity and have dramatically evolved the VRP research landscape.

The processing speed and memory capacity of computers has grown rapidly, enabling the processing of increasingly complex instances of VRPs and widespread application of logistics distribution scenarios. The number of VRP solution methods introduced in the academic literature has grown rapidly over the past few decades. According to Eksioglu et al. [4], the VRP represents an evolving field of operations research that has been growing exponentially at a rate of 6% per year, which makes it difficult to keep track of developments in the field and obtain a clear overview of which variants and solution methods are relatively novel.

The VRP family can be considered as two combinatorial senses: (1) the number of possible solutions, which grow exponentially with computer science and algorithm design; and (2) the number of conceivable problem variants, which also grow exponentially with a variety of problem attributes [12]. This survey classifies the academic literature on VRPs from the perspective of solution methodologies, as well as the detailed characteristics of VRPs. Because we base our classification on the taxonomy presented in [4], we restrict our analysis to articles published between 2019 and August of 2021. Therefore, we do not intend to provide an exhaustive overview of VRP literature. To the best of our knowledge, this article provides the first structured classification of recent VRP literature based on solution and problem attributes.

The main contribution of our paper is a classification table that is available online as Appendix. This classification table should enable future researchers to find relevant literature easily by eliminating or selecting characteristics in the taxonomy, leaving only articles tailored to their interests. The main objective of this work is to provide readers with recent trends and solution methodologies in the field of VRPs and some well-known variants. This survey is expected to help future researchers identify a problem domain and promising topics for research.

Section 2 defines the scope of this survey and Section 3 introduces the VRP and its variants. A comprehensive survey of state-of-the-art strategies currently used for solving VRPs is presented in Section 4. Section 5 summarizes our observations and conclusions.

2. Scope of the Survey

We analyzed recent literature published between 2019 and August of 2021 using a taxonomic framework. Classification is followed by a survey that uses the taxonomy to evaluate trends in the field and identify which articles contribute to these trends. We restricted the reviewed literature to the following features: only relevant articles published in English-language journals were considered, meaning books, conference proceedings, and dissertations were excluded.

To extract the most relevant literature and keep the number of articles manageable, the following search strategy was applied. First, only articles containing "vehicle routing" as title words or keywords were selected. Second, the search was limited to articles that were extended by highly cited articles published in any ranked journal (Google Scholar top 20), excluding review papers. For papers published in 2021, which are too recent to have cite ranking, we selected the top five pages from Google Scholar, each of which had 10 cited articles, as well as two review papers written by Moghdani et al. [13] and Asghari and Al-e (2021). Third, the abstracts of selected articles were read to determine their relevance to the subject.

This search strategy resulted in a final set of 88 articles. Although this selection is not exhaustive, it contains the majority of recent articles on VRPs and can be considered as representative of the field.

3. VRP and Its Variants

3.1. VRP

In addition to the classical VRP, several variants have also been studied. Capacitated VRP (CVRP), VRPTW, VRP with heterogeneous fleets (HFVRP), time-dependent VRP (TDVRP), and multi-depot VRP (MDVRP) are some of these variants. The classical VRP can be described as follows. Let G = (V, A) be a graph, where $V = \{v_0, v_1, v_2, ..., v_N\}$, where $\{v_1, v_2, ..., v_N\}$ is the node set representing customers to be served and v_0 is the depot. Each customer is characterized by a demand D_i . A = $\{(v_i, v_j): v_i, v_j \in V\}$ is the arc set (subscript indicates sequence) linking nodes i and j with a distance d_{ij} . Let $M_m = \{m_1, m_2, m_3, ..., m_m\}$ denote the vehicle set, where each vehicle has a maximum load capacity cap_m , meaning the total load of vehicle m cannot exceed the maximum load capacity cap_m . To reflect a real distribution scenario accurately, different features are considered according to the settings of heterogeneous models. The goal of the VRP is to derive optimal vehicle routes such that each customer is visited exactly once by one vehicle and each vehicle starts and ends its route at the depot. The following assumptions are adopted:

- 1. The depot has a demand equal to zero.
- 2. Each customer location is serviced by only one vehicle.
- 3. Each customer's demand is indivisible.
- 4. Each vehicle shall not exceed its maximum load capacity cap_m .
- 5. Each vehicle starts and ends its route at the depot.
- Customer demand, distribution distances between customers, and delivery costs are known.

The notations used for problem definition are summarized as Tables 1–3.

Table 1. Sets and indices of VRP.

V	Node set, where v_0 is the depot and $\{v_1, v_2,, v_N\}$ are customers
i,j	Subscripts of the customer nodes, $i, j = 1, 2, N$
A	$A = \{(v_i, v_j): v_i, v_j \in V\}$ is arcs set linking nodes i and j
M_m	The set of vehicles with <i>m</i> types

Table 2. Parameters of VRP.

D_i	Demand of customer i
d_{ij}	Distance between nodes i and j
veh_m	Maximum available number of each vehicle type
cap_m	Maximum load capacity of vehicle type m
fc_m	Fixed cost of vehicle type <i>m</i>
vc_m	Variable cost of vehicle type <i>m</i>
$Dm_{ij,m}$	Amount carried using vehicle type m from i to j

Table 3. Decision variable of VRP.

 $X_{ij,m}$ Value of one if vehicle type m travels from node i to j. Otherwise, value of zero

Traditional logistics models focus on minimizing the total cost of a network. This is where the concept of the VRP is best applied. We follow this concept and add the fixed cost fc_m of a vehicle, which represents rent cost or operating costs, to the total cost to minimize the total number of vehicles. We also include the variable cost vc_m of delivery using each type of vehicle to optimize vehicle scheduling. Additional constraints appear in the target calculation in the form of penalty functions to enforce vehicle limit constraints. The objective of minimizing the total cost is defined as follows:

Appl. Sci. 2021, 11, 10295 4 of 32

Minimize
$$\sum_{m=1}^{M} \sum_{i=0}^{N} \sum_{j=0}^{N} X_{ij,m} f c_m + \sum_{m=1}^{M} \sum_{i=0}^{N} \sum_{j=0}^{N} d_{ij} D m_{ij,m} v c_m$$
 (1)

subject to the following constraints:

Routing:

$$\sum_{i=1}^{N} X_{i0.m} = 1 \ \forall \ m \in M_m \tag{2}$$

$$\sum_{m=1}^{M} \sum_{i=1}^{N} \sum_{j=1}^{N} X_{ij,m} = 1 \,\forall \, (i,j) \in A \,\forall \, m \in M_m$$
 (3)

$$\sum_{m=1}^{M} \sum_{i=1}^{N} X_{ip,m} = \sum_{m=1}^{M} \sum_{i=1}^{N} X_{pi,m} \quad \forall \ p \in V$$
 (4)

Demand and capacities:

$$\sum_{i=1}^{N} \sum_{j=1}^{N} X_{ij,m} D_{j} = D m_{ij,m} \forall (i,j) \in A \forall m \in M_{m}$$
 (5)

$$\sum_{i=1}^{N} Dm_{0i,m} \le cap_m \,\forall \, m \in \mathcal{M}_m \tag{6}$$

$$\sum_{m=1}^{M} X_{ij,m} \le veh_m \ \forall \ m \in \mathcal{M}_m \tag{7}$$

The objective function in Equation (1) is the total cost, which includes the fixed cost and variable cost. Constraint (2) states that each vehicle should return to the depot, where the subscript is zero. Constraint (3) ensures that each node can only be visited once in a route. Constraint (4) states that, if a vehicle arrives at a node, it must leave that node, thereby ensuring route continuity. Constraints (5) and (6) impose restrictions on the amounts of demand and capacity. Constraint (7) defines the maximum number of available vehicles veh_m .

3.2. VRP Variants

Practical requirements and new challenges require extensive definitions and formulations of the VRP. For example, distance, driver working hours, time windows, traffic conditions, and so on can all arise in real-world VRPs and enrich the definition and applications of VRPs. This chapter provides an overview of recent research on different models for vehicle routing. The main goal of this chapter is to present an overview of vehicle routing and scheduling areas while discussing several real-world applications.

Some features of VRPs are summarized in Table 4 based on the research by Eksioglu et al. [4]. Other variants have also been studied beyond the classical VRP. These variants include the influence of time factors, time windows of customers, maximum operating time of vehicles, differing delivery times caused by varying traffic conditions, varying characteristics of vehicles, varying capacities, varying speeds, and new types of electric vehicles. By referring to the taxonomy of [4], we divided models into three main categories: customer-related, vehicle-related, and depot-related models, which is the most important issue to represent the difference in real delivery problems. These categories have representative model features that are sorted in the tables below according to the year as shown in Tables 5–7.

Table 4. Taxonomy of VRP literature (adapted from [4]).

1. Type of Study	3.4. Number of Points of Origin
1.1. theory	3.4.1 single origin
1.2. applied methods	3.4.2 multiple origins
1.2.1 exact methods	3.5. number of points of loading/unloading facilities (depot)
1.2.2 heuristics	3.5.1 single depot
1.2.3 simulation	3.5.2 multiple depots
1.2.4 real-time solution methods	3.6. time window type
1.3. implementation documented	3.6.1 restriction on customers
1.4. survey, review of meta-research	3.6.2 restriction on roads
2. scenario characteristics	3.6.3 restriction on depot/hubs
2.1. number of stops on rout	3.6.4 restriction on drivers/vehicle
2.1.1 known (deterministic)	3.7. number of vehicles
2.1.2 partially known, partially probabilistic	3.7.1 exactly <i>n</i> vehicles
2.2. load splitting constraint	3.7.2 up to <i>n</i> vehicles
2.2.1 splitting allowed	3.7.3 restriction on drivers/vehicle
2.2.2 splitting not allowed	3.8. capacity consideration
2.3. customer service demand quantity	3.8.1 limited capacity
2.3.1 deterministic	3.8.2 unlimited capacity
2.3.2 stochastic	3.9. vehicle homogeneity (capacity)
2.3.3 unknown	3.9.1 similar vehicles
2.4. request times of new customers	3.9.2 load-specific vehicles
2.4.1 deterministic	3.9.3 heterogeneous vehicles
2.4.2 stochastic	3.9.4 customer-specific vehicles
2.4.3 unknown	3.10. travel time
2.5. on-site service/waiting times	3.10.1 deterministic
2.5.1 deterministic	3.10.2 function dependent
2.5.2 time dependent	3.10.3 stochastic
2.5.3 vehicle type dependent	3.10.4 unknown
2.5.4 stochastic	3.11. transportation cost
2.5.5 unknown	3.11.1 travel time dependent
2.6. time window structure	3.11.2 distance dependent
2.6.1 soft time windows	3.11.3 vehicle dependent
2.6.2 strict time windows	3.11.4 operation dependent
2.6.3 mixture of both	3.11.5 function of lateness
2.7. time horizon	3.11.6 implied hazard/risk related
2.7.1 single period	4. information characteristics
2.7.2 multiple periods	4.1. evolution of information
2.8. backhauls	4.1.1 static
2.8.1. nodes request simultaneous pickups and deliveries	4.1.2 partially dynamic
2.8.2. nodes request either linehaul or backhaul service,	4.2 quality of information
but not both	4.2 quanty of information
2.9. node/arc covering constraints	4.2.1 known (deterministic)
2.9.1 precedence and coupling constraints	4.2.2 stochastic
	4.2.2 Stochastic
2.9.2 subset covering constraints	4.2.3 forecasted
2.9.2 subset covering constraints 2.9.3 recourse allowed	
	4.2.3 forecasted
2.9.3 recourse allowed	4.2.3 forecasted 4.2.4 unknown (real-time)

3.1.2 undirected network	4.4. processing of information
3.2 locations of addresses (customers)	4.4.1 centralized
3.2.1 customers on nodes	4.4.2 decentralized
3.2.2 arc routing instances	5. data characteristics
3.3 geographical locations of customers	5.1 data used
3.3.1 urban (scattered with a pattern)	5.1.1 real-world data
3.3.2 rural (randomly scattered)	5.1.2 synthetic data
3.3.3 mixed	5.1.3 both real and synthetic data
	5.2 no data used

Table 5. Model categories of VRPs published in 2021.

No.	Authors	Model Features			
No.	Autnors	Customer-Related Aspects	Vehicle-Related Aspects	Depot-Related Aspects	
4	(Mojtahedi, Fathollahi-Fard,	1	1		
1	Tavakkoli-Moghaddam, & Newton [14])	time windows	heterogeneous vehicles	single depot	
2	(Nguyen, Dang, & Tran [15])	classical	truck and drone	single depot	
3	(Basso, Kulcsár, & Sanchez-Diaz [16])	classical	electric vehicles	single depot	
4	(Pan, Zhang, & Lim [17])	time windows	homogeneous vehicles	loading at the depot simultaneously	
5	(Keskin, Çatay, & Laporte [18])	time window	electric vehicles	time window	
6	(Wang, Liu, & Wang [19])	time window	heterogeneous vehicles	single depot	
7	(Behnke, Kirschstein, & Bierwirth [20])	time window	heterogeneous vehicles	single depot	
8	(Anderluh, Nolz, Hemmelmayr, & Crainic [21])	"grey zone" customers	vehicle synchronization	single depot	
9	(Dewi & Utama [22])	classical	green vehicle	single depot	
10	(Martins, Hirsch, & Juan [23])	classical	homogeneous vehicles	single depot	
11	(Gmira, Gendreau, Lodi, & Potvin [24])	time windows	travel speeds are associated with road segments in the road network	single depot	
12	(Archetti, Guerriero, & Macrina [25])	static and online customers	heterogeneous vehicles	single depot	
13	(Abdirad, Krishnan, & Gupta [26])	time windows, dynamic, demands from customers at different locations that arrive in the system at different times	heterogeneous vehicles	single depot	
14	(Latorre-Biel, Ferone, Juan, & Faulin [27])	customer demands are not only stochastic, but also correlated	heterogeneous vehicles	single depot	
15	(Srivastava, Singh, & Mallipeddi [28])	soft time windows	heterogeneous vehicles	single depot	
16	(Altabeeb, Mohsen, Abualigah, & Ghallab [29])	time windows	heterogeneous vehicles	single depot	
17	(Sadati & Çatay [30])	classical	homogenous vehicles	multiple depots	
18	(İLHAN [31])	classical	homogenous vehicles	single depot	
19	(Euchi & Sadok [32])	classical	homogenous vehicles	single depot	
20	(Florio, Hartl, Minner, & Salazar- González [33])	time window, stochastic	homogenous vehicles	single depot	
21	(Chaabane, Montecinos, Ouhimmou, & Khabou [34])	time window	end-of-life vehicles	single depot	
22	(Park, Son, Koo, & Jeong [35])	time windows	heterogeneous vehicles	single depot	

23	(Chen, Demir, & Huang [36])	time windows	after the emergence of delivery assistants, each van can be equipped with several delivery robots while performing last-mile parcel delivery tasks in populated areas	single depot
24	(Abdullahi, Reyes-Rubiano, Ouelhadj, Faulin, & Juan [37])	time windows	green vehicle	single depot
25	(Pan, Zhang, & Lim [38])	time windows, time- dependent	heterogeneous vehicles	single depot
26	(Lee [39])	time window	electric vehicles	single depot
27	(Li, Wang, Chen, & Bai [40])	time windows	with satellite bi- synchronization	single depot
28	(Fan, Zhang, Tian, Lv, & Fan [41])	time windows	green vehicle	multiple depots
29	(Quirion-Blais & Chen [42])	time windows	heterogeneous vehicles	single depot
30	(Mühlbauer & Fontaine [43])	classical	cross-docking from vans to cargo bicycles at so-called satellites	single depot
31	(Lin, Ghaddar, & Nathwani [44])	time windows	electric vehicle	single depot
32	(Wang, Xu, & Wang [45])	time windows	heterogeneous vehicles	multi-depot
33	(Mendes, Lush, Wanner, Martins, Sarubbi, & Deb [46])	passengers are transported from their origin to their destination sharing the same vehicle	heterogeneous vehicles	single depot
34	(Aerts, Cornelissens, & Sörensen [47])	classical	heterogeneous vehicles	single depot
35	(Niu, Wen, Cao, & Xiao [48])	stochastic demand time window	heterogeneous vehicles	single depot
36	(Jia, Mei, & Zhang [49])	classical	homogeneous electric vehicle	single depot
37	(Sitek, Wikarek, Rutczyńska- Wdowiak, Bocewicz, & Banaszak [50])	time windows	homogenous vehicles	single depot
38	(Niu, Cao, Gao, Xiao, Song, & Zhang [51])	time windows, stochastic demands	heterogeneous vehicles	single depot
39	(Casazza, Ceselli, & Wolfler Calvo [52])	time windows	heterogeneous vehicles	single depot
40	(Grabenschweiger, Doerner, Hartl, & Savelsbergh [53])	classical	heterogeneous vehicles	single depot
41	(Afsar, Afsar, & Palacios [54])	accept the service if the zone prices are below individual thresholds	homogenous vehicles	single depot
42	(Olgun, Koç, & Altıparmak [55])	classical	green vehicle	vehicles departing from a certain depot must return to the same depot
43	(Stellingwerf, Groeneveld, Laporte, Kanellopoulos, Bloemhof, & Behdani [56])	time and temperature dependent	heterogeneous vehicles	single depot
44	(Wang, Liao, Li, Yan, & Chen. [57])	time window	heterogeneous vehicles	single depot
45	(Zhang, Li, Sun, & Hou [58])	the probability that customers are served before their (uncertain) deadlines must be higher than a predetermined target	heterogeneous vehicles	single depot

46	(Haixiang, Fang, Wenwen, & Mingyun [59])	an unknown number of customer requests that dynamically appear during route execution	heterogeneous vehicles	single depot
47	(Dalmeijer & Desaulniers [60])	time window	heterogeneous vehicles	single depot
48	(Guo, Huang, & Huang [61])	time window	heterogeneous vehicles	single depot

Table 6. Model categories of VRPs published in 2020.

No.	Authors	Model Features				
140.	Authors	Customer-Related Aspects	Vehicle-Related Aspects	Depot-Related Aspects		
1	(Pasha, Dulebenets, Kavoosi, Abioye, Wang, & Guo [62])	time window	two vehicles are expected to serve one customer each, while one vehicle is expected to serve two customers after visiting the required supplier and manufacturer nodes	after completing the service for the last customer, each vehicle returns to the dummy depot, travel costs from each customer location to the dummy depot are assumed to be zero		
2	(Abbasi, Rafiee, Khosravi, Jolfaei, Menon, & Koushyar [63])	classical	homogenous vehicles	single depot		
3	(Kitjacharoenchai, Min, & Lee [64])	classical	drone truck	multiple drones are not allowed to be launched or retrieved at the same node at any given time		
4	(Raeesi & Zografos [65])	time windows	electric commercial vehicles (ECVs), battery- swapping vans (BSVs)	ECVs and BSVs in the fleet to operate routes that start and finish at the depot		
5	(Zhang, Chen, Zhang, & Zhuang [66])	time windows	electric vehicle	single depot		
6	(Song, Li, Han, Han, Liu, & Sun [67])	time windows, adopt a rating method to determine customer satisfaction	vehicles with different energy consumption indexes are considered	single depot		
7	(Giallanza & Puma [68])	classical	green vehicle with a defined capacity	single depot		
8	(Zhang, Chen, Zhang, Wang, Yang, & Cai [69])	classical	homogenous vehicles	shared carriers and depots (multiple depots)		
9	(Brandão [70])	classical	homogenous vehicles	multiple depots, vehicles do not return to the depot after delivering goods to customers		
10	(Eshtehadi, Demir, & Huang [71])	time windows	multi-compartment vehicles	single depot		
11	(Zhen, Ma, Wang, Xiao, & Zhang [72])	time windows and release dates	multi-trip vehicle	multiple depots		
12	(Kancharla & Ramadurai [73])	classical	electric vehicle	allow multiple visits to a charging station without duplicating nodes		
13	(Molina, Salmeron, Eguia et al. [74])	time windows	heterogeneous vehicle	single depot		
14	(Mao, Shi, Zhou, & Zhang [75])	time windows	homogeneous electric vehicles	single depot		
15	(Lu, Chen, Hao, & He [76])	time windows	homogeneous fleet of k electric vehicles	single depot		

Appl. Sci. 2021, 11, 10295 9 of 32

16	(Fachini & Armentano [77])	time windows	heterogeneous fixed fleet	single depot
17	(Shi, Zhou, Ye, & Zhao [78])	time windows	classical	single depot
18	(Trachanatzi, Rigakis, Marinaki, & Marinakis [79])	classical	homogenous vehicles	single depot
19	(Li, Wang, Chen, & Bai [80])	time windows	mobile satellites	single depot
20	(Sethanan & Jamrus [81])	classical	heterogeneous fixed fleet	single depot

Table 7. Model categories of VRPs published in 2019.

No.	Authoro	Model Features			
No.	Authors -	Customer-Related Aspects	Vehicle-Related Aspects	Depot-Related Aspects	
1	(Wang & Sheu [82])	arc-based	with drones	single depot	
2	(Pelletier, Jabali, & Laporte [83])	classical	electric freight vehicles	single depot	
3	(Schermer, Moeini, & Wendt [84])	classical	homogenous vehicles	single depot	
4	(Bruglieri, Mancini, Pezzella, & Pisacane [85])	classical	green vehicle	single depot	
5	(Li, Soleimani, & Zohal [86])	classical	green vehicle	multiple depots	
6	(Basso, Kulcsár, Egardt, Lindroth, & Sanchez-Diaz [87])	classical	electric commercial vehicles	single depot	
7	(Breunig, Baldacci, Hartl, & Vidal [88])	classical	electric two-echelon vehicle	single depot	
8	(Zhen, Li, Laporte, & Wang [89])	classical	unmanned aerial vehicles	single depot	
9	(Stavropoulou, Repoussis, & Tarantilis [90])	classical	consistent vehicle	single depot	
10	(Keskin, Laporte, & Çatay [91])	time windows	electric vehicle	single depot	
11	(Huang, Blazquez, Huang, Paredes- Belmar, & Latorre-Nuñez [92])	classical	feed vehicle	single depot	
12	(Arnold & Sörensen [93])	classical	homogenous vehicles	single depot	
13	(Long et al. [94])	classical	prize-collecting vehicle	single depot	
14	(Sacramento, Pisinger, & Ropke [95])	classical	unmanned aerial vehicles	single depot	
15	(Schermer, Moeini, & Wendt [96])	classical	homogenous vehicles	single depot	
16	(Zhao, Luo, & Han [97])	time window	homogenous vehicles	single depot	
17	(Froger, Mendoza, Jabali, & Laporte [98])	classical	electric vehicle	single depot	
18	(Yu, Wang, Wang, & Huang [99])	time window	homogenous vehicles	single depot	
19	(Marinakis, Marinaki, & Migdalas [100])	time window	homogenous vehicles	single depot	
20	(Altabeeb, Mohsen, & Ghallab [101])	classical	homogenous vehicles	single depot	

The objectives of VRPs can also be diversified according to different stakeholder requirements. The traditional objective of the standard VRP is to minimize a cost function, which is considered to be the total distance traveled by all vehicles. However, recent studies have focused on various negative externalities of transportation, including carbon emissions and duration. For an objective discussion, we classified single and multiple objectives according to the diversity of objectives and then listed the objectives used in different studies. The papers with the same numbers as those in Tables 2–4 are listed in Tables 8–10. Additionally, we discussed the test instances used in different studies.

 $\textbf{Table 8.}\ \textbf{Model objectives of VRPs published in 2021}.$

No.	Multi-Object	Single-Object	Dataset	Max Nodes	Other Settings
1	cost, green emissions		self-generation	72	
2		minimize the operational cost	self-generation	400	driving and flight times of trucks and drones are assumed to be deterministic
3		energy consumption	real data	map	
4			based on the TDVRPTW instances proposed in [102]	100	multiple trips per vehicle, time-dependent travel times
5		tune constant waiting times	100 customer EVRPTW-SP instances from [103]	108	stochastic waiting times at recharging stations
6	minimize costs, service waiting times, and number of vehicles in multiple service periods		VRPTW-SP instances from [103]	41	
7	•	reduce greenhouse gas (GHG) emissions	instances for emission-oriented vehicle routing on a multigraph (uni-halle.de)	100	different vehicle–load combinations
8	minimize cost consisting of total GHG emissions		adapted Solomon instances introduced in [104]	100	
9	time-related and distance-related variable costs		adapted Solomon instances introduced in [104]	100	
10		minimize the total duration of delivery routes (cost)	test instances proposed in [105]	150	
11		` *	exact branch-and-price (BP) method reported in [106]	200	
12		minimize the distribution cost	from the well-known Solomon VRPTW instances presented in [107] and described in [108]	200	
13		minimize transportation cost	self-generation	100	

1.4		stochastic and	instance A-n32-k5 (available from	21	
14		correlated customer demands	https://bit.ly/3eGxGx9 accessed on 31 August 2020)	31	
	minimize	customer demands	2020)		
	number of vehicles, total travel distance,				
15	makespan, total waiting time, and total delay time incurred by late arrivals		same testing datasets used in [109,110]	250	
16		minimize the total distance	02 instances from seven standard benchmarks in [111–114]	200	
17		minimize the total distance	GVRP instances generated in [115]	483	
18		minimize the total distance	benchmarks instances proposed in [111]	199	
19		minimize the total travel time of vehicles and drones	benchmarks instances from [95]	200	
20	VRPSD-PDC (reduce traveling costs and the number of required vehicles)		self-generation	60	optimal restocking
21		minimize the total cost	self-generation	20	
22		minimize the total distance	self-generation	20	
23		minimize the sum of route completion times	https://data.mendeley.com/datasets/kxfcwkw db9/draft?a=edb5ce79-b4c7-4121-93ca- 317e82328b1c accessed on 23 January 2020	200	delivery robots
24	minimize distance, economic dimension cost, and environmental dimension cost		five instances from [116]	43	
25		duration minimizing	test instances adopted from [102] and newly generated instances	100	
26	total travel and charging time		adapted Solomon instances	36	
27		minimize the total cost	test instances adopted from [116]	120	
28		reduce distribution costs	self-generation	144	time-varying road network

maximize the number of lengthy historical customer chains in the solution and minimize the total cost minimize the total distance minimize logistics operating costs operating costs and riding cost minimize total distance minimize the picking travel distance minimize total distance minimize total distance minimize the distance minimize the distance minimize the distance minimize total ravelidis and mumber of vehicles minimize total traveling distance minimize total distance minimize total traveling distance minimize total traveling distance minimize total distance minimize total traveling distance minimize total distance self-generation and number of vehicles minimize the distances travelled by vehicles and the penalties for delivering items (shipments) to allernative points minimize total customer dissatisfaction minimize the total customer dissatisfaction minimize the total cost and maximize the total cost and minimize the total profit minimize the total consumption costs maximal profit minimize the total consumption costs maximal profit minimize the total consumption costs minimize the total profit minimize the total consumption costs minimize the total profit minimize the total cons						
Self-generation 300	29	number of lengthy historical customer chains in the solution and minimize		random generated instances	105	
distance minimize logistics operating costs reduce operating and riding costs minimize the order picking travel distance minimize travel distance drivers, remuneration, and number of vehicles minimize the distances travelled by vehicles and the penalties for delivering items (shipments) to alternative points minimize total cost and customer dissatisfaction minimize total satisfaction and minimize total cost and minimize the total profit minimize the total cost and co	30			self-generation	300	
Teal data 180	31			self-generation	100	
Internation	32			real data	180	
minimize travel distance, drivers, remuneration, and number of vehicles minimize travel distance, drivers, remuneration, and number of vehicles minimize the distance stravelled by vehicles and the penalties for delivering items (shipments) to alternative points minimize total cost and customer dissatisfaction minimize the total cost and cost and customer dissatisfaction minimize the total cost and cost and cost and customer dissatisfaction minimize the total cost and cost and cost and customer dissatisfaction minimize the total cost and cost and cost and customer dissatisfaction minimize the total cost and cost and cost and customer dissatisfaction minimize the total cost and cost and cost and cost and customer dissatisfaction minimize the total cost and cost and cost and cost and customer dissatisfaction minimize the total cost available instance set from [120] 75 heterogeneous locker boxes minimize the total profit classical CVRP instances from [121] 50 minimize minimize deconsumption costs real data obtained from seven supermarket deals as a cost and consumption costs and cost and cost and customer dissatisfaction real data obtained from seven supermarket deals as a cost and cost and customer dissatisfaction are cost and customer dissatisfaction and the cost and customer deals are cost and customer dissatisfaction are cost and customer deals are cost and customer dissatisfaction are cost	33		reduce operating		250	
distance, drivers, remuneration, and number of vehicles Self-generation 200	34		picking travel		100	
minimize total traveling distance minimize the distances travelled by vehicles and the penalties for delivering items (shipments) to alternative points minimize total cost and customer dissatisfaction minimize the total cost minimize the total profit minimize the total cost available instances est from [120] minimize total profit minimize fuel consumption costs minimize fuel consumption costs minimize fuel consumption costs minimize fuel consumption costs minimize product decay, minimize total at a obtained from seven supermarket chains minimize the total generated randomly from [122] minimize product decay, minimize the total chains minimize the total classical CVRP instances supermarket chains minimize the total consumption costs minimize the total classical cover supermarket chains minimize the total consumption costs minimize the total classical cover supermarket chains minimize the total classical cover supermarket chains minimize the total classical cover supermarket chains	35	distance, drivers, remuneration, and number of		self-generation	200	
minimize the distances travelled by vehicles and the penalties for delivering items (shipments) to alternative points minimize total cost and customer dissatisfaction 39 minimize the total cost minimize the total profit 10 minimize the total cost and customer dissatisfaction 39 minimize the total cost minimize the total cost minimize the total cost maximize the total cost maximize the total profit 10 minimize the total cost maximize the total profit 110 minimize fuel consumption costs 120 minimize fuel classical CVRP instances from [121] for cost minimize fuel consumption costs 120 minimize fuel classical CVRP instances from [121] for cost minimize fuel consumption costs 120 minimize fuel classical CVRP instances from [120] for cost minimize fuel consumption costs 120 minimize fuel classical CVRP instances from [120] for cost minimize fuel consumption costs 120 minimize fuel classical CVRP instances from [120] for cost minimize fuel consumption costs	36			-	1000	
38cost and customer dissatisfactionself-generation12039minimize the total costtest instances adopted from [119]3040minimize the total costavailable instance set from [120]75heterogeneous locker boxes41maximize the total profitclassical CVRP instances from [121]5042minimize fuel consumption costsgenerated randomly from [122]199minimize product decay, product decay, chainsreal data obtained from seven supermarket chains80	37		minimize the distances travelled by vehicles and the penalties for delivering items (shipments) to	•	6	delivery and
minimize the total cost test instances adopted from [119] 30 40 minimize the total cost available instance set from [120] 75 heterogeneous locker boxes 41 maximize the total profit classical CVRP instances from [121] 50 42 minimize fuel consumption costs generated randomly from [122] 199 minimize product decay, real data obtained from seven supermarket chains	38	cost and customer	•	self-generation	120	
40 minimize the total cost available instance set from [120] 75 heterogeneous locker boxes 41 maximize the total profit classical CVRP instances from [121] 50 42 minimize fuel consumption costs generated randomly from [122] 199 minimize real data obtained from seven supermarket product decay, chains 80	39			test instances adopted from [119]	30	
profit classical CVRP instances from [121] 50 42 minimize fuel consumption costs generated randomly from [122] 199 minimize real data obtained from seven supermarket product decay, chains 80	40		minimize the total	available instance set from [120]	75	_
minimize 43 product decay, generated randomly from [122] 199 real data obtained from seven supermarket chains	41			classical CVRP instances from [121]	50	
real data obtained from seven supermarket 43 product decay, chains	42			generated randomly from [122]	199	
	43	product decay,			80	

	cost, and				
	maximum decay				
	minimize the				
	total route				
	distance and				
	total customer				
44	waiting time for		test instances adopted from [123]	30	
	the				
	improvement of				
	customer				
	satisfaction				
45		minimize the total	colf compartion		
45		cost	self-generation	-	
16		minimize the total	16	(0	
46		cost	self-generation	60	
		minimize the	instances for the TWAVRP introduced in [124]		
47			and extended in [125]; these instances are	50	
47		expected cost of distribution	available in the VRP repository VRP-REP	30	
		distribution	[126]		
	_		P-n-k" instances are from [111], "RY"		
48		minimize the total	instances are from the "RY ATT48" in [127],	150	
40		cost	and "Tai" instances are from [128] with the	150	
			number of nodes ranging from 75 to 150.		

Table 9. Model objectives of VRPs published in 2020.

No.	Multi-Object	Single-Object	Dataset	Max Nodes	Other Settings
1		minimize the total supply chain cost	self-generation	75	factory will be assembled at each customer location to meet existing demand
2		minimize the total cost	self-generation	-	
3		minimize the total truck arrival time of trucks at the depot	benchmarks from [111] (sets A, B, and P) and [112]	75	multiple drones are not allowed to be launched or retrieved at the same node at any given time, meaning the times of both trucks and drones at customer locations must be adjusted to be the same
4		minimize the total cost	VRPTW instances proposed in [129]	100	battery swapping service begins before or after customer service

5		minimize the total travel distances of all EVs	fuzzy optimization model for EVRPTW and recharging stations (figshare.com accessed on 25 June 2019) [66]	200	recharging stations studied in an uncertain environment
6		minimize the total cost	test instances adopted from [107]	100	cold chain logistic system
7	total costs and carbon emissions are minimized		test instances adopted from [130]	based on dataset	
8	operating quality, operating reliability, operating cost, operating time		test instances adopted from [131]	(depots) 30	
9		minimize the distance travelled	test instances adopted from [121,132–134]	288	
10		minimize fixed and variable vehicle costs	self-generation	200	each compartment requires energy to maintain the temperature for the total number of delivery crates inside a compartment
11		minimize the total traveling time of all vehicles	test instances adopted from [107]	200	
12		minimize the total time (travel times plus charging times)	test instances adopted from [135]	320	the number of such duplications is not known a priori and the size of the problem increases
13	maximize the total number of served customers and minimize the total travel cost		test instances adopted from [136,137]	based on dataset	limited number of resources
14		minimize the total cost	test instances adopted from [129]	100	
15		minimize the total cost	self-generation	200	
16		minimize fixed and variable vehicle costs	test instances adopted from [107,138–140]	100	
17		minimize the total cost	test instances adopted from [141]	based on dataset	
18		minimize the total cost	test instances adopted from [107]	200	
19		minimize the total cost	test instances adopted from [107]	100	one DC in which a homogeneous fleet of van–UAV

				combinations are available
20	minimize the total cost	test instances adopted from [138,142]	100	

Table 10. Model objectives of VRPs published in 2019.

No.	Multi-Object	Single-Object	Dataset	Max Nodes	Other Settings
1		minimize total cost	self-generation	13	1
2		minimize total cost	test instances adopted from [135]	320	2
3		minimize the makespan through constraints	test instances adopted from [143]	100	3
4		minimize the total travel distance	test instances adopted from [115,144]	100	4
5	revenue maximization, and travel time, emission, and cost minimization	,	self-generation	35	5
6	stage one: path minimization; stage two: route minimization for total energy consumption		self-generation	20	6
7	·	minimize total cost	sets two and three from [145], set five from [146], and set six from [147]; charging stations follow the guidelines from [129] (instances of the electric VRP with time windows and recharging stations) and [103]	200	7
8		minimize the total time required to complete monitoring tasks	self-generation	724	8
9		maximize the net acquired profit	from the traditional VRP instances in [112]	199	9
10		minimize total cost	VRPTW instances presented by Schneider et al. [129]	100	10
11		minimize total cost	self-generation	200	11
12		minimize the number of routes	instance set from [148], MDVRP experiments using the benchmark set from [134]	1000	12

13	minimize the total traveling cost, maximize the prizes collected by all vehicles		http://www.coin- or.org/SYMPHONY/branchandcut/VRP/data/i ndex.htm.old accessed on 14 June 2018	32	13
14		minimize the operational cost when visiting customers	self-generation	200	14
15		minimize the makespan	test instances adopted from [105]	50	15
16	minimize transportation and time cost		test instances adopted from [107]	100	16
17	minimize total driving and charging time		Montoya et al.'s [139] testbed (publicly available at http://vrp-rep.org accessed on 18 June 2018).	20	17
18		minimize carbon emission	test instances adopted from [107]	100	18
19		minimize the number of vehicles	test instances adopted from [107], includes 56 instances divided into six sets with 100 nodes; includes 300 instances of different sizes from [108]	1000	19
20		minimize the total distance travelled by vehicles	self-generation	80	20

As shown in the tables above, there are different main model objectives for different years. The results are summarized in Figure 1.

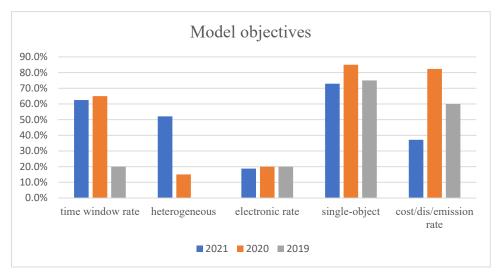


Figure 1. Different model objectives in different years.

One can see that the time window still occupies a large proportion of model objectives and is the mainstream of current research on the VRP and its variants. This trend is closely related to the concept of the "to C" distribution, where customers focus on

service satisfaction. There have been various extensions of the VRP, including the VRPTW and time-dependent problems such as those discussed in [17,24,41,75,89]. Additional research has focused on heterogeneous vehicle problems that are closely related to real-life vehicle applications. With the increasing focus on environmental protection, electric vehicle distribution has also gradually become a mainstream research topic. Relevant research can be found in [49,72,81,89,116]. Single-objective models still occupy a certain research space, where the objective value setting is still largely based on cost metrics (e.g., cost, distance, and $\it CO_2$ emission). However, unlike cost metrics in past research, the costs in the current single-objective problem research tend to be compound costs representing actual delivery costs.

4. Solutions for VRPs

Because real-world problems involve complex constraints, advanced algorithms are required to solve VRPs in complicated and constantly changing environments. The number of customers and vehicle types is increasing and the use of optimization algorithms is a key component of effective customer service and efficient operations. A large variety of VRP solution strategies have been presented in the literature. These strategies range from exact methods to heuristics and meta-heuristics. Exact methods provide optimal solutions, whereas heuristics and meta-heuristics generally yield near-optimal solutions. Exact methods are typically only suitable for small-scale problems (up to 200 customers). Because the VRP and its variants are known to have NP-hard complexity, solving larger instances optimally is very time-consuming. However, there are no bounds on problem size when solving problems using heuristics and meta-heuristics that can efficiently handle large numbers of constraints and still output near-optimal solutions. Figure 2 presents various approaches to solving the VRPs and was adapted from content in [6,149].

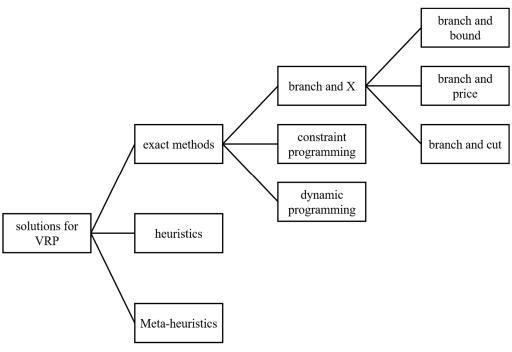


Figure 2. Solutions for VRPs.

Exact methods include a variety of approaches, mainly branch and X (X: cut, bound, price, and so on) approaches, as well as dynamic programming and column generation methods. In recent years, significant advances in the exact solution of VRPs have been

achieved. A major milestone was the branch-and-price algorithm proposed by Pecin et al. [150]. The branch-and-bound (BB) method was developed to explore solution spaces implicitly. Because the performance of BB algorithms depends on the quality of bounds obtained throughout a tree, BB algorithms can be combined with the generation of cutting planes, forming so-called branch-and-cut algorithms, or with column generation, resulting in BAP algorithms [151]. Branch and X remain the dominant VRP approaches [150,152]. While branch and X approaches treat VRPs as integer linear programming (ILP) or mixed ILP (MILP), dynamic programming breaks complex problems into a number of simpler sub-problems. Constraint programming is a model that interrelates different variables using constraints. When the search space is reduced, relatively simple problems can be solved by various search algorithms [149].

Approximate methods called heuristics are designed to solve specific problems. Heuristics focus on systematically finding an acceptable solution within a limited number of iterations. A heuristic yields solutions faster than an exact method. A meta-heuristic may be referred to as an intelligent strategy combining subordinate heuristics for exploration and exploitation.

For solution discussion, we classified exact methods, heuristic algorithms, and meta-heuristic algorithms in papers with the same numbers as those in Tables 11–13. The results are presented in the tables below.

Table 11. Solutions to VRPs published in 2021.

		Solution		_
No.	Exact Methods	Heuristic	Meta-Heuristic	Operating Environment
	Exact Methods	Algorithms	Algorithms	
1			Simulated	
			annealing (SA)	
		Slack induction		C++ compiled with GCC 9.3.0. Use CPLEX 12.10
2		through string and		to solve MILPs. All tests run on a desktop
		sweep removals		operating Xubuntu 20.04 with an AMD Ryzen
		<u> </u>		3700X @4.0 GHz CPU, 16 GB RAM.
3		Paths first, routes		/
		second		,
		Hybrid ALNS-		Java and the MIP model is solved by IBM ILOG
		variable		CPLEX 12.8.0 (IBM CPLEX, 2017). All
4		neighborhood		experiments run on an Ubuntu 18.04.3 LTS
		descent (VND)		server with an Intel(R) Xeon(R) Silver 4216 CPU
		algorithm		of 2.10 GHz
		Deterministic greedy	,	
		insertion,		
		probabilistic greedy		Coded in Java programming language and all
5		insertion,		experiments conducted on an Intel Core i7-8700
		probabilistic greedy		CPU 3.2 GHz processor with 16 GB RAM
		insertion with		
		confidence		
			Hybrid heuristic	
			algorithm with	
6			three-dimensional	/
			k-means	
			clustering	<u> </u>
7	1. Solve the shortest			C++ with Visual Studio 2017, single core of an
	path problem using			Intel i7-2600 CPU with 8 GB RAM

	a backward labelling			
	algorithm, 2. Use the			
	column generation			
	technique to set up a			
	fast heuristic and a			
	branch-and-price			
	(BAP) algorithm			
	(BIII) digoridani			C/C++ and tested under Linux Ubuntu 16.04
				LTS running on a virtual machine (using two
8		Large neighborhood		processors and 2 GB RAM) on a host Intel(R)
		search (LNS)		Core(TM) i5-3320 M CPU @2.60 GHz and 4 GB
				RAM
			HWOA algorithm	
			based on the	
9			whale	Linux Ubuntu 16.04 LTS running on a virtual
			optimization	machine
			algorithm	
		Agile optimization	uigorium.	
		(refers to the massive		p2 GB RAM with a host Intel(R) Core(TM) i5
10		parallelization of BR		CPU
		algorithms)		
		The initial solution is		
		generated by a		
		greedy insertion		
11		heuristic and the		2020 M CDU 02 (0 CU 1/1 4 CD D A M
11		neighborhood of the		3320 M CPU @2.60 GHz with 4 GB RAM
		current solution is		
		generated using		
		CROSS exchanges		
		Using an iterative		
		insertion algorithm		
		to construct an initial		Coded in Java, while the offline problem was
12		solution and re-		solved using Cplex 12.5. All experiments run on
		optimize using the 2-		an Intel(R) Core(TM) i7-16700HQ CPU with two
		O re-optimization		cores operating @2.60 GHz with 16 GB RAM.
		algorithm		
		Construction		
		algorithms: path		Al id id to be a list of the
		cheapest arc, savings,		Algorithm was implemented in Python.
13		and global cheapest		Experiments performed on a personal PC with
		arc are applied to the		an Intel® Core™ i7- 4790S CPU @3.20 GHz with
		construction phase of		four cores and 8 GB RAM
		a route		
14			Petri net predictor	
			Non-dominated	
1 -			sorting genetic	C language and Linux based. 2.50 GHz Intel
15			algorithm II	Core i7 CPU system with 8 GB RAM
			(NSGA-II)	
			Firefly algorithm	Coded in Java and executed on an Intel i5 CPU
16			(FA)	@3.2 GHz with 4 GB RAM on a 32-bit Windows
			(1 A)	7 OS

17		General variable neighborhood search method (GVNS) with		Intel Core i7-8700 @3.2 GHz and 32 GB RAM
		tabu search (TS)	0.4.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.	
			SA algorithm with	
18			a crossover	Intel Core i7 @2.40 GHz and 8 GB RAM
			operator	
			modified hybrid	
			genetic algorithm	Visual Studio C++ application, 64 bits (win64),
19			(nearest-neighbor	Intel® Core TM i5-2450M @ 2.5 GHz and 4 GB
1)			heuristic and	RAM
			modified savings	KAIVI
			heuristic)	
	marral DAD			Single thread of an Intel® CoreTM i7-4790 @3.60
20	novel BAP			GHz 32 GB RAM. Linear programs were solved
	algorithm			using IBM® CPLEX® version 12.6.1
		first phase focuses or	1	
		"routes' construction	l	
		using dealers"		
		characteristics,		Computational experiments were conducted on
		second phase of		a workstation with an Intel Core i7-2600 @3.4
		"routes' assignment"		GHz, 16 GB RAM, and Windows 7 Enterprise
21		assigns the most		2009 (64 bits). For VRP mathematical model
		interesting routes to		validation, the LINGO solver V.15. For heuristic
		internal carrier		development, Python 2.7.13 with CPXOPT was
		trucks, and the		used
		cheapest carrier		
		brokers get the		
		remaining dealers		
			genetic algorithm	,
22			(GA)	
			, ,	MS Windows with MATLAB R2020a (Math
		adaptive large		Works, 2020) on a laptop computer with an Intel
23		neighborhood search	1	i5-3610QM CPU @2.30 GHZ with 4 GB RAM.
		(ALNS) algorithm		The mathematical model was solved using the
		\		IBM CPLEX 12.10.0 solver (IBM, 2019)
		BRIG-LS generic		
		framework		
		combining a biased-		
24		randomized		Java application on an Intel QuadCore i5 CPU
		technique with an		@3.2 GHz with 4 GB RAM
		iterative greedy		
		technique		
		ALNS with TS		,
25		algorithm		1
2.	n i n	U		3.2 GHz Intel Xeon W CPU with 32 GB
26	BAP			of RAM
	CPLEX 12.4, a			
27	modified ALNS			/
	heuristic			

•••			hybrid GA with	MATLAB2018b on the Windows 10 OS, 4 GB
28			VNS	RAM, Intel(R) Core(TM) i7-7700 @3.60 GHz
29		Case base reasoning (CBR)		
30		Greedy insertion, repack insertion, regret insertion		C++11 compiled with GCC version 5.1.0. All runs were performed on a computer with 8 GB RAM and an Intel i5-6200 CPU @2.40 GHz
31			policy gradient algorithm	Macbook Pro (2018) running Mac OS 10.13.6 with 4 CPU processors @2.3 GHZ and 16 GB RAM. The RL model was realized using Tensorflow 2.2.0. The code was implemented in Python
32			hybrid GA with TS	1
33	cluster algorithm			/
34		Adapted Hausdorff- based batching heuristic		C++ Visual Studio 17. All experiments carried out on an Intel(R) Core i7-6820HQ CPU @2.7 GHz with 16 GB RAM
35		chromosome representation, decision tree		Python 3 on a machine with an Intel Core i5-8600K
36			Bi-level ant colony optimization (ACO) algorithm	C++ and executed on an Intel i7-6700 @3.40 GHz on the Arch Linux system
37		Construction heuristic (nearest neighbor)		Intel(R) Celeron(R) CPU 1005 M 2 @1.90 GHz, 8 GB RAM, Windows 10 64-bit
38			CLP and MP, CLP and GA	Python, Windows 10 with an AMD Rayzen7 1700x processor
39	check which integrality constraints are not satisfied and enforce them by exploring a search tree through branching rules			C++ using the SCIP framework version 4.0.0. LP sub-problems were solved using the simplex algorithm implemented in CPLEX 12.6 (CPLEX development team, 2011)
40		ALNS, iterative first- fit decreasing algorithm		C++ programming language. CPLEX 12.9 used for solving exact models (MIP). Multithreading deactivated. All programs run on an Intel Xeon Processor E5-2670 v2 (25 MB Cache, 2.50 GHz) with 3 GB RAM. The operating system was Linux
41	BAP			/
42		develop an HH-ILS algorithm based on ILS and VND heuristics, nearest neighborhood search heuristic for initial solution		Intel Core i7-4720HQ CPU @2.6 GHz computer with Windows 10 OS and 16 GB RAM. Metaheuristic was implemented in C++. Code compiled in Visual Studio Professional 16.7.1 with MSC compiler version 1927 with default settings. Commercial solver IBM ILOG CPLEX 10.2.0 with its default settings used as an optimizer to solve the MIP formulation

43	new two-index- based mathematical formulation			/
44			NSGA-II as a static optimizer when the environment does not change	16 GB RAM, Intel Core i7-10700 @2.9 GHz.
45	First is the difficulty of obtaining exact moment measures for the ambiguity set <i>Pi</i> and second is when the distribution function is continuous			/
46			improved differential evolution (DE) algorithm	MATLAB R2014a, Windows 7 (x32)
47		heuristic dynamic programming		Coded in C and C++, IntelXeon E3-1226 v3 @3.30 GHz and 16 GB RAM
48			MCWS-LS heuristic, S-ALNS algorithm with SA	

Table 12. Solutions to VRPs published in 2020.

		Solution		_
No.	Exact Methods	Heuristic Algorithms	Meta-Heuristic Algorithms	Operating Environment
1		Evolutionary algorithm		MATLAB (2016a), Intel(R) CoreTMi7- 7700K CPU and 32 GB RAM, Windows 10 OS
2			GA	Intel (R) Core i5-7600 @3.50 GHz with 8 GB RAM equipped with an NVIDIA GeForce GTX 1060 graphics card. This GPU has 1280 cores and its base and boost clocks are 1506 MHz and 1708 MHz, respectively, C++ CUDA 8.0 (V8.0.61)
3		DTRC, LNS		,
4	a	Dynamic programming Ilgorithm and integer program, ILNS algorithm		Intel CoreTM i5 @3.40 GHz CPU with 8 GB RAM. The branch-and-bound solver of CPLEXTM 12.9.0 was used as the exact solver and all other algorithms were coded in MATLAB. When necessary, CPLEXTM is called from MATLAB.
5		ALNS algorithm, VND algorithm		3.60 GHz AMD Ryzen 7 3700X CPU with 32 GB RAM, Windows 10 OS

6	Improved artificial fish swarm algorithm, push forward insertion heuristic (PFIH)		/
7	\ /	NSGA-II	/
8		Proposed EVNS algorithm	/
9	Nearest-neighbor heuristic, insertion heuristic		C language, desktop PC with an Intel Core i7-3820 CPU @3.6 GHz and 32 GB RAM
10	ALNS algorithm		
11		Particle swarm optimization (PSO), GA	Intel Core i7 @2.80 GHz, 8 GB RAM, model implemented in CPLEX (version 12.6.2) with C# (VS2015)
12	ALNS algorithm		Coded in GAMS 23.9 and solved using the Gurobi 7.5 solver hosted on the NEOS server. The server runs on an Intel XeonE5-2430 @2.2 GHz with 3 GB RAM. ALNS algorithm coded in Python and tested on a PC running a 3.6 GHz Intel Core-i7-7700 CPU with 16 GB RAM
13	VND tabu search algorithm with holding list		Algorithm coded in C++ and run on a 3.30 GHz Intel® Core(TM) i5-2400 CPU
14		improved ant colony optimization (ACO) algorithm	Coded in Visual C++ and implemented on an Intel Core i5 CPU @3 GHz with 8 GB RAM
15	IVNS algorithm, VND procedure		Coded in C++ and run on a Linux cluster system with an AMD Opteron 4184 CPU (2.8 GHz and 2 GB RAM) running Ubuntu 12.04. For the general CPLEX solver, the latest version of 12.6 was used
16		constructive heuristic based on LNS meta- heuristic	Programmed in C# and run on an Intel® Core $^{\text{TM}}$ i7-6500U CPU @2.5 GHz with 16 GB RAM
17	PFIH method, neighborhood search, tabu search		
18		FA based on coordinates	Gurobi 4.5.1 with Python 3.0 on an Intel(R) Core(TM) i7-7700HQ CPU @2.80GHz with 8 GB RAM.
19	ALNS algorithm		CPLEX 12.9, coded in C++. The code for the heuristic and exact method was executed on a Windows 8 computer configured with an Intel(R) Core(TM) 3.2 GHz CPU with 8 GB RAM
20		GA	MatLab on a 2.10 GHz PC, with 8 GBytes of RAM

Table 13. Solutions to VRPs published in 2019.

NT_	C =1C =	On a notion a Francisco manage
NO.	Solution	Operating Environment

	Exact Methods	Heuristic Algorithms	Meta-Heuristic Algorithms	_
1	BAP			C# on a computer with an Intel I7 CPU @2.69 GHz and 16 GB RAM. Gurobi 8.0.0 chosen as an MIP solver
2		LNS with cutting- plane method		C++, executed on a cluster of 27 machines, each with two Intel(R) Xeon(R) X5675 CPUs @3.07 GHz with 96 GB RAM running on Linux. Each machine had 12 cores and each instance was executed using a single thread
3		DASP		Intel® Xeon® Gold 6126 CPUs and 16 GB RAM, algorithms in Java SE 8 and Gurobi Optimizer 8.1.0 for solving MILPs
4	Path-based exact solution			Intel i7-5500U @2.4 GHz with 16 GB RAM, coded in Java
5			improved ACO algorithm	1
6		Bellman–Ford algorithm		1
7		LNS		Coded in Fortran 77 and run on a single thread of a 3.6 GHz Intel i7-4790 CPU with 32 GB RAM. Relies on CPLEX 12.5.1 for the resolution of linear programs and some integer subproblems. Metaheuristic was coded in Java (JRE 1.8.0-151), and run on a single thread of a 3.4 GHz Intel i7-3770 CPU
8			tabu search metaheuristic	IBM ILOG CPLEX Optimization Studio 12.6.1 (Visual Studio 2015, C#) on a DELL Precision 7600 workstation with two Xeon E5-2643 V3 CPUs (24 cores) @3.4 GHz with 128 GB RAM
9		Adaptive tabu search		C++ and all computational experiments were performed on a 3.30 GHz Intel Core i5 CPU on a single thread
10		ALNS algorithm		Intel Xeon E5 2.10 GHz CPU virtual machine with 16 GB RAM
11			ACO algorithm	JAVA computer language, executed using a computer with an Intel (R) Core (TM) i7 CPU @3.40 GHz and 4 GB RAM
12		Knowledge-guided local search		AMD Ryzen 3 1300X CPU @3.5 GHz on Windows 10
13		Genetic local search algorithm		C++ language and all 120 instances run independently five times on a PC with two Intel i7-7820 CPUs @2.9 GHz and 32 GB RAM on the Windows 10 OS (64-bit)
14		ALNS algorithm		Java, run on a Huawei XH620 V3 computer with an Intel Xeon 2660v3 CPU @2.60 GHz
15		Hybrid VNS/tabu search algorithm		Intel® Xeon® Gold 6126 cluster, where each node operated at 2.6 GHz with 16 GB RAM (hyperthreading disabled). Algorithms implemented in Java SE 8 and Gurobi Optimizer 8.1.0 used for solving MILPs (Gurobi Optimization, 2018).

Appl. Sci. 2021, 11, 10295 25 of 32

16			NSGA-II	MATLAB R2017a
		Exact heuristic		Gurobi 7.5.0, 12 GB RAM and on a cluster of 27
17				computers, each with 12 cores and two Intel(R)
		algorithm		Xeon X5675 @3.07 GHz CPUs
	Improved PAD			C# and CPLEX with a 3.10 GHz Intel Core TM
18	Improved BAP			i5-2400 CPU using the Microsoft Windows 7 OS
	algorithm			with 8 GB RAM
19			Multi-adaptive	Intel Core i5 2430M @2.40 GHz with 4 GB RAM
19			PSO algorithm	on the Windows 7 Home Premium 64-bit OS
			imamana d bashui d	Coded in Java and run on 12 computers with
20			improved hybrid	Intel i-5 @3.2 GHz CPUs and 4 GB RAM with 32-
			FA	bit Windows 7

As shown in the tables above. Heuristic algorithms and meta-heuristic algorithms are still the mainstream solution methods, although branch and X methods will continue to increase in popularity in 2021. As mentioned previously, with the rapid growth in the processing speed and memory capacity of computers (i.e., operating environments), more complex instances of the VRP can be solved.

5. Observations and Conclusions

Based on the practical importance of VRPs in real life, such problems have attracted significant research attention in recent years. Most work has been devoted to classical cost objectives such as total cost, total travel distance, and \mathcal{CO}_2 emission. Some studies have considered multiple objectives. In order to solve the problem of greenhouse gas emission, the discussion of trolley distribution has become a research trend. Time windows still account for a large proportion of modern papers and are mainstream in current research on the VRP and its variants. Time windows are closely related to the current mode of "to C" distribution, where customers focus on service satisfaction.

Regarding datasets, different studies make various adjustments to data and many use generated datasets in addition to real data, which makes it difficult to compare algorithms using a unified standard. There is still scope for significant further work in the field. Therefore, researchers should be motivated to develop publicly available datasets, and effective and efficient methods for dealing with VRPs. The gaps in the available literature mentioned above may motivate further work in these directions for researchers in this field.

For solving algorithms, with the development of the processing speed and memory capacity of computers, using the exact way such as branch and X to solve VRPs is rapid growth. However, heuristic algorithms and meta-heuristic algorithms are still the mainstream solution methods, such as SA [14], GA [35,41,45], NSG [28,47], SSO [153], and so on. It is hoped that more exact algorithms can be applied to solve VRPs in the future, and the number of nodes in the dataset that can be solved can be increased as much as possible.

Our research protocol was well defined because it aims at an efficient and thorough review of multiple VRP variants. The main goal of this study was to identify the trends of VRP variants and the algorithms applied to solve them. Additionally, papers that are considered to represent pioneering efforts from the research community were presented. The papers with the most citations were considered to be the most significant and they were discussed in detail in this review.

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Appl. Sci. 2021, 11, 10295 26 of 32

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Appendix A

Table A1. List of abbreviations for vehicle routing problems and its variants.

Abbreviations	Definition	Abbreviations	Definition
VRP	Vehicle routing problem	GVRP	Green VRP
VRPTW	VRP with time windows	HFVRP	VRP with
VKFIVV	VKF with time windows	ПГУКГ	heterogeneous fleets
CVRP	Capacitated VRP	MDVRP	Multi-depot VRP
EV	Electric vehicle	TDVRP	Time-dependent VRP
ECV	Electric commercial vehicle	TDVRPTW	Time-dependent VRP
ECV	Electric commerciai vernicie	IDVKFIW	with time widows
EVRP	Electric VRP	TWAVRP	Time window
EVKI	Electric VIXI	IWAVKI	assignment VRP
			VRP with stochastic
EVRPTW	Electric VRP with time widows	VRPSD-PDC	demands and
LVKIIVV		VICI 3D-1 DC	probabilistic duration
			constraints
	EVRPTW at most a single (S) recharge		
EVRPTW-SP	per route, and partial (P) battery	VRP-REP	VRP repository
-	recharges are possible		

Table A2. List of abbreviations for solution of VRP and its variants.

Abbreviations	Definition	Abbreviations	Definition
ACO	Ant colony antimization	HH-ILS	Hyper-heuristic algorithm based on
ACO	Ant colony optimization		ILS and VND heuristics
ALNS	Adaptive large neighborhood search	HWOA	Hybrid whale optimization algorithm
BAP/BP	Branch and price	ILNS	Iterated large neighborhood search
BB	Branch and bound	LNS	Large neighborhood search
		MCWS-LS	Modified Clarke-Wright saving
BC	Branch and cut		algorithm (MCWS), and solution
			improvement by local search (LS)
BRIG-LS	Biased-randomized iterated greedy with local search	MP	Mathematical programming
CDD	Case base reasoning	NSGA-II	Non-dominated sorting genetic
CBR			algorithm II
CLP	Constraint logic programming	PFIH	Push forward insertion heuristic
DE	Differential evolution algorithm	PSO	Particle swarm optimization
DTRC	Drone truck route construction	SA	Simulated annealing

Appl. Sci. 2021, 11, 10295 27 of 32

EVNS	Extended variable neighborhood search method	S-ALNS	Simulated annealing (SA), and adaptive large neighborhood search (ALNS)
FA	Firefly algorithm	SSO	Simplified swarm optimization
GA	Genetic algorithm	TS	Tabu search
GVNS	General variable neighborhood search method	VND	Variable neighborhood descent

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Appl. Sci. 2021, 11, 10295 31 of 32

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Appl. Sci. 2021, 11, 10295 32 of 32

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