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Towards the Search for Thallium Nuclear Schiff Moment in Polyatomic Molecules: Molecular Properties of Thallium Monocyanide (TICN)

A. V. Kudrin¹, A. Zaitsevskii^{1,2,*}, T. A. Isaev², D. E. Maison^{2,3} and L. V. Skripnikov^{2,3}

- ¹ Chemistry Department, M. Lomonosov Moscow State University, Moscow 119991, Russia
- ² NRC "Kurchatov Institute"—PNPI, Orlova Roscha, 1, Gatchina 188300, Russia
- ³ Physical Department, Saint-Petersburg State University, Ulianovskaya 1, Petrodvoretz 198504, Russia
- * Correspondence: zaitsevskii_av@pnpi.nrcki.ru

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Abstract: Molecular properties of the thallium monocyanide (TI·CN) system in its ground electronic state are studied using high-precision ab initio relativistic two-component pseudopotential replacing 60 inner-core electrons of Tl. A relativistic coupled-cluster method with single, double and perturbative triple amplitudes is employed to account for electronic correlations. Extrapolation of results to the complete basis set limit is used for all studied properties. The global potential energy minimum of TI·CN corresponds to the linear cyanide (TICN) isomer, while the non-rigid isocyanide-like (TINC) structure lies by approximately 11 kJ/mol higher in energy. The procedure of restoration of the wavefunction in the "core" region of Tl atom was applied to calculate the interaction of the Tl nuclear Schiff moment with electrons. The parameter *X* of the interaction of the Tl nuclear Schiff moment with electrons of the nuclear Schiff moment are discussed.

Keywords: molecular electronic structure; parity and time-reversal invariance violating interactions; Schiff moment; relativistic coupled cluster calculation

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1. Introduction

Linear triatomic molecules with heavy atoms have recently attracted great attention in connection with the prospects for searching for the effects not described in the framework of the Standard Model of elementary particles. Some triatomic molecules with open-shell ground electronic states have been proposed for the search for the nuclear spin-dependent effects, violating space parity ($\mathcal{NSD-PV}$ effects) and scalar electron-nucleon interaction violating both space parity and time reversibility $(\mathcal{P}, \mathcal{T}$ -odd effects) [1,2] and search for permanent electron electric dipole moment [3]. It turns out that linear triatomic molecules with Σ ground electronic state (like the proposed RaOH and YbOH), being excited to the first bending vibrational state, possess so-called *l*-doubling of spin-rotational levels, similar to Λ -doubling for spin-rotational levels for linear molecules with Π ground electronic state. The Λ -doubling can be, for example, used with great efficiency for suppressing of the different systematic effects in ultra-precise molecular spectroscopy (see e.g., Reference [4]). Recently, the search for the Schiff moment of the Tl nucleus has started using the TlF molecule [5] and the spin-rotational spectrum of this molecule was studied for both ground and several excited states [6]. In Reference [1] we have pointed to the molecule TICN as a prospective candidate for the search for $\mathcal{NSD-PV}$ and \mathcal{P}, \mathcal{T} -odd effects (note that the nuclear Schiff moment arises due to \mathcal{P}, \mathcal{T} -odd nuclear forces). Both experimental and theoretical information concerning the molecular structure and isomerism of TICN is scarce. Three

vibrational frequencies detected in the gas-phase experiment [7] were allegedly assigned to cyanide and isocyanide isomers. The DFT electronic structure calculations [7] using large-(68-electron-) core one-component pseudopotential of Tl and a very restricted basis set, confirmed the existence of linear TlCN, whereas the detected stationary point of the potential energy surface presumably associated with the isocyanide was a saddle-type point.

According to electronic structure calculations and experiments in the gas phase and in inert matrices, molecules consisting of a group 13 or group 1 metal atom M and the CN fragment, M·CN, which can be considered respectively as analogs and pseudo analogs of Tl·CN, can have linear or slightly bent isomers (the cyanide MCN and isocyanide MNC) and a T-shaped one usually denoted as M[CN]. In the first approximation, the relative stability of isomers is determined by the type of the M - CN bond. If this bond is essentially ionic, the T-shaped structure is normally the most stable one due to the optimal Coulomb attraction and the isomerization barriers are low [8]. This situation occurs in the Na·CN [9–11] and K·CN [10–13] molecules. In the latter case, the KNC isomer does not exist [11]. In contrast, when the bond has a significant covalent component, isocyanide structures are more stable, isomerization barriers are relatively large and the T-shaped isomers usually do not exist [14]. It seems natural to suppose the existence of linear TICN isomers similar to those of other cyanides of 13th groups elements.

In the present paper we report a study of ground-state properties and isomerism of Tl-CN by accurate relativistic electronic structure methods and for the first time calculate the parameter X of the interaction of the Tl nuclear Schiff moment [15] with electrons in linear triatomic molecule, TlCN.

2. Computational Methods

The electron subsystem of Tl-CN is described using the accurate shape-consistent two-component relativistic pseudopotential replacing 60 inner-core (1s-4f) electrons of the Tl atom [16]. The remaining external electrons of Tl and all the electrons of the light atoms are treated explicitly. The many-electron problem is solved using the relativistic coupled-cluster method with single, double and perturbative triple cluster amplitudes, RCCSD(T) [17] with the triple zeta (TZ) and quadruple zeta (QZ) quality basis sets. The TZ set includes aug-cc-pVTZ bases for C, N [18] and (9s 9p 8d 4f 1g)/[6s 7p 5d 4f 1g] one for Tl [19]; the QZ set consists of aug-cc-pVQZ for C, N [18] and (10s 11p 9d 5f 4g 1h)/[7s 8p 6d 5f 4g 1h] for Tl [19]. One-electron molecular spinors are constructed by solving the relativistic Kramers-restricted analog of the Hartree–Fock equations. Final energy estimates are obtained by the two-point extrapolation to the complete basis set limit (CBS) [20]. Note that the extrapolation efficiently supresses the basis set superposition errors [21]. A separate set of calculations is performed using the two-component relativistic density functional theory (RDFT) [22] with the hybrid exchange-correlation functional PBE0 [23] and the basis sets (11s 7p 2d)/[5s 4p 2d] for C, N [24] and uncontracted [8s 7p 7d 3f] for Tl [16].

We started with scanning the RCCSD(T) potential energy surface in a wide range of the internal coordinates *R* and θ (see Figure 1) in order to approximately locate the stationary points. At this stage, the C - N distance was frozen at r(CN) = 1.158 Å. Then the configurations and energies of all linear structure were refined using the Broyden-Fletcher-Goldfarb-Shanno's algoritm [25].

The vibrational frequencies for the TICN isomer (TI-C stretching ω_1 , bending ω_2 and C = N stretching ω_3) are evaluated within the harmonic approximation. Other molecular properties of this isomer are calculated for the equilibrium geometry obtained at the CBS limit. The dipole moment *D* is evaluated within the central finite-difference approximation, fitting the dependence of the total energy on the strength of the applied uniform electric field along the molecular axis in the range ± 0.00004 a.u.

The effective interaction of electrons with the Tl nuclear Schiff moment in the TlCN molecule is described by the following Hamiltonian [15,26]:

$$H_{\rm eff} = 6X\left(\vec{S},\vec{\lambda}\right),\tag{1}$$

where $\vec{S} = S\vec{I}/I$ is the Schiff moment of Tl, \vec{I} is Tl nuclear spin, $\vec{\lambda}$ is the unit vector along the internuclear axis *z* from Tl to C and *X* is the parameter given by:

$$X = \frac{2\pi}{3} \cdot \left. \frac{\partial \rho_{\psi}(\vec{r})}{\partial z} \right|_{\vec{r}=0},\tag{2}$$

where $\rho_{\psi}(\vec{r})$ is the electronic density at the point \vec{r} , where $\vec{r} = 0$ corresponds to the center of the Tl nucleus. To calculate this parameter determined by the behavior of the valence wave function inside the nucleus, we employed the two-step method described in detail in References [27–31]. At the first step, the valence and outer-core part of the molecular wave function is treated within the generalized relativistic pseudopotential method [32–34]. The inner-core electrons are excluded from the explicit treatment. The resulting valence (pseudo) wave functions are smoothed in the spatial inner core region of a heavy atom that leads to considerable computational savings [35,36]. The second step is the nonvariational restoration of the correct 4-component behavior of the valence wave function in the spatial core region of the heavy atom [27–31].

The calculations are carried out using the DIRAC17 [37], MRCC [38,39], and two-component relativistic DFT [22] codes.

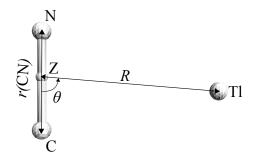


Figure 1. Internal coordinates *R*, r(CN), θ for the Thallium Monocyanide (TI·CN) system. Z is the center of mass of the CN fragment, $\theta = 0^{\circ}$ and $\theta = 180^{\circ}$ correspond to the linear TICN and TINC structures, respectively.

3. Results and Discussion

Molecular properties. The relative energies of stationary points for the Tl·CN potential energy surface are listed and compared with the corresponding values for the cyanides of group 13 and 1 elements in Table 1. At all levels of correlation treatment (RCCSD(T)/TZ,QZ,CBS, RDFT/PBE0) the global energy minimum corresponds to the linear TlCN isomer. The dependence of the ground-state energy on the bending angle in the region of isocyanide-like structures is extremely flat. The cross section of Tl·CN potential energy surface along the approximate isomerization path obtained at the RCCSD(T)/CBS level of theory is displayed in Figure 2.

Due to the non-rigidity of the TINC-like structure, the position of the local minimum is very sensitive to the level of correlation treatment; the harmonic approximation for the vibrations of this isomer is senseless.

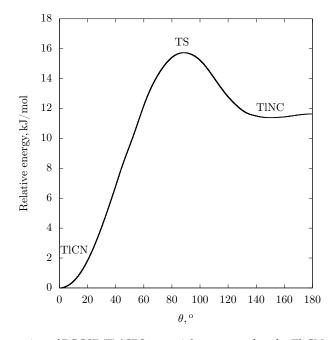


Figure 2. The cross section of RCCSD(T)/CBS potential energy surface for Tl·CN along the approximate isomerization path. TS: transition state. The energy is given with respect to the global minimum. The distance r(CN) = 1.16641 Å is frozen at the equilibrium value for the TlCN isomer.

Table 1. Relative energies (kJ/mol) of isomers and transition states (TS) for M·CN systems. PW: present work.

м	Method	C	MCN	TS	MNC		
IVI	Method	Source	MCN	15	Minimum	Linear	
	RCCSD(T)/TZ		0	16.4		9.0	
Tl	RCCSD(T)/QZ	PW	0	16.0	9.9	11.2	
11	RCCSD(T)/CBS	I VV	0	15.7	10.7	11.4	
	RDFT/PBE0		0		13.4	14.5	
Tl	DFT/BP89	[7]	0			6.2	
	CCSD	[40]	25.7	55.5		0	
Al	CCSD(T)	[40]	23.2			0	
	QCISD(T)	[41]	23.7			0	
Ca	DFT/BP89	[7]	5.5			0	
Ga	DFT/B3LYP	[42]	8.7			0	
In	DFT/BP89	[7]	1.4			0	
			MCN	TS	M[CN]	linear MNC	
Na	CCSD(T)	[11]	10.1	15.8	0	11.2	
Κ	CCSD(T)	[11]	18.3	19.3	0	13.0	_
Rb	CCSD(T)	[11]	18.3	18.8	0	12.5	

The situation with no minima corresponding to the linear isocyanide structure and low isomerization barriers is typical for systems with predominantly ionic bonds M–CN. At the same time, for strongly ionic alkali metal cyanides the most stable isomers are T-shaped. In contrast, light analogues of the thallium compounds, such as the Al·CN and Ga·CN, are stable in the isocyanide configurations and have no T-shaped isomers. Along the series Al–Ga–In–Tl, the relative stability of the isocyanide isomers decreases monotonically, so that the TlCN isomer is significantly more stable than the isocyanide. The isomerisation barriers decrease along the series, becoming for the Tl·CN comparable to those in Na·CN, K·CN and Rb·CN systems. The results of simple DFT modeling of the indium system (Table 1) indicate that the linear InNC should not exist; however, this disagrees with the microwave spectroscopy data [42]. Anyway, according to the infrared spectroscopy study [7] the linear or slightly bent InNC is slightly more abundant than the cyanide.

The calculated equilibrium geometries, harmonic vibrational frequencies and dipole moment for the TlCN isomer, along with the corresponding available experimental data for other analogue and pseudo analogue M·CN systems, are collected in Table 2. The TlCN harmonic vibrational frequencies were calculated for the most abundant isotopomer ($^{205}Tl^{12}C^{14}N$). In all cases, the dipole moment direction corresponds to the charge redistribution $M^{+\delta} \cdot (CN)^{-\delta}$.

Table 2. Molecular parameters of M·CN isomers for M belonging to groups 13 and 1. Internuclear distances in ångstroms, vibrational frequencies (ω) in cm⁻¹, dipole moments (*D*) in atomic units, r(MX) = r(MC) for cyanides and r(MN) for isocyanides. PW: present work.

Molecule	Source	r(MX)	r(CN)	ω_1	ω_2	ω ₃	D	
	RCCSD(T)/TZ, PW	2.344	1.173					
TICN	RCCSD(T)/QZ, PW	2.333	1.170					
	RCCSD(T)/CBS, PW	2.324	1.166	294	101	2163	2.41	
	RDFT/PBE0, PW	2.358	1.178	277	104	2149	2.39	
TICN	Exptl. [7]			207(2)		2126		
TlNC(?)	Exptl. [7]			307(?)		2048		
	CCSD(T) [40]	2.014	1.171	472	187	2479	3.49	
AlCN	Exptl. [41]			524	133	1975		
	Exptl. [7]			456		2144		
	CCSD(T) [40]	1.861	1.187	584	131	2290	3.14	
	Exptl. [42]	1.854	1.178	453	167			
AINC	Exptl. [43]	1.849	1.171					
	Exptl. [44]			549;557	100	2069		
	Exptl. [7]			532		2069		
GaCN	Exptl. [42]	2.062	1.158	304				
GaCN	Exptl. [7]					2138		
GaNC	Exptl. [42]	1.938	1.174		105			
Gane	Exptl. [7]			401		2046		
LONI	Exptl. [42]	2.262	1.146	302				
InCN	Exptl. [7]			333		2132		
InNC	Exptl. [42]	2.137	1.170		71			
mine	Exptl. [7]			392		2151		
		r(MC)	r(MN)	r(CN)	ω_1	ω_2	ω_3	D
	Exptl. [9]	2.366	2.243	1.169				
Na[CN]	Exptl. [45]				368	168	2047	
	CCSD(T) [11]	2.39	2.23	1.18				3.48
	Exptl. [12]	2.716	2.549	1.169				
K[CN]	Exptl. [45]				288	139	2050	
	CCSD(T) [11]	2.73	2.55	1.18				4.04

Unusually flat bending potentials and large amplitudes of zero-point vibrations in Al, Ga and In isocyanides were discussed in Reference [42]. The shape of the bending potential of the TINC isomer (Figure 2) apparently indicates that the bending motion is fairly free in the range $\theta = 140^{\circ}...220^{\circ}$. Note that the computed TICN bending frequency $\omega_2 = 101.2 \text{ cm}^{-1}$ also corresponds to the significant zero-point vibration amplitude.

The calculated TICN equilibrium geometry corresponds to the rotational constant value $B_e = 2.406$ GHz. The *l* doubling interval can be roughly estimated as $B^2/\omega_2 = 1.9$ MHz. This value is significantly smaller than its counterparts for the systems recently proposed for the search for NSD-PV and P, T-odd effects, RaOH (3.1 MHz) [1] and YbOH, where the value of *l*-doubling splitting was estimated to be ≈ 10 MHz [3]. The TICN *l*-doubling interval is expected to be the smallest one for group 13 (iso)cyanide molecules; even for the rather heavy and flexible InNC molecule, the *l*-doubling interval should be about 4.6 MHz. Thus full polarisation of the TICN molecule can be reached in electric fields smaller than 100 V/cm, which allows much better control of the systematic effects in high-precision experiments.

For all group 13 and group 1 atoms, the C \equiv N stretching frequencies in M·CN are in the ranges ca. 2125–2150 cm⁻¹ for cyanide isomers and ca. 2040–2050 cm⁻¹ for isocyanide or T-shaped isomers. The only unexpected experimental value for the AlCN molecule obtained by Fukushima [41] ($\omega_3 = 1974.5 \text{ cm}^{-1}$) disagrees with another experimental estimate ($\omega_3 = 2143.7 \text{ cm}^{-1}$ [7]) and the

results of electronic structure calculations. Our estimate $\omega_3 = 2163 \text{ cm}^{-1}$ for TlCN is in line with this pattern.

The RCCSD(T) dipole moment values for TICN seem unexpectedly small even compared to that of AICN and AINC molecules where the covalent contribution to AI-CN bonding is believed significant.

Schiff moment. The values of the X parameter for the TICN molecule obtained within different basis sets and methods are given in Table 3. One can see a good convergence of the results with increasing basis set size. In particular, the contribution of the perturbative triple cluster amplitudes is almost independent of basis set size, being smaller than 3%. This also demonstrates a good convergence with respect to the level of the electron correlation treatment.

Table 3. Calculated values of the X parameter for TICN. The recommended estimate is given in boldface.

Basis S	Set	<i>X</i> , a.u.			
T1	C, N	Hartree-Fock	RCCSD	RCCSD(T)	
[6s7p5d4f1g]	[5s4p3d2f]	8997	7119	6939	
[9s9p8d4f1g]	[5s4p3d2f]	9093	7263	7076	
[7s8p7d5f4g1h]	[6s5p4d3f]	9105	7351	7150	

The final X value (7150 a.u.) is close to that obtained earlier for the ²⁰⁵TlF molecule (7635 a.u., [27]).

If the properties of the excited electronic states in TlCN resemble those in TlF, one would also expect amenability of TlCN for cooling with lasers. This would open an exciting perspective for the ultra-precision spectroscopy of polyatomic molecules with closed electronic shells. The resulting value of the *X* parameter is also close to that for the ²²⁵RaO (7532 a.u. [46]) and ²⁰⁷PbO [30] molecules and about two times larger than in the ²²⁵RaF molecule [47]. Just to compare the Schiff moment enhancement factor with non-molecular systems, we notice that the *X* parameter, for example, liquid xenon is almost 40 times smaller [48].

4. Conclusions

The results of relativistic calculations on the ground electronic state of the TI-CN system in the framework of the coupled cluster (RCCSD(T)) method with the extrapolation to the complete basis set limit demonstrate unambiguously that the lowest-energy isomer has a linear cyanide-like (TICN) equilibrium structure. The isocyanide-like isomer has equilibrium energy 11 kJ/mol above the global minimum and is extremely non-rigid with respect to bending deformations. Similar results were obtained within the simple relativistic density functional computational scheme. In the Al–TI row of cyanides and isocyanides the TI-CN system is probably the first wherein the cyanide TICN is the most stable isomer. Along this row, the rigidity of cyanides and isocyanides gradually decreases. Our estimate of the parameter characterising the interaction of the TI nuclear Schiff moment with electrons in the TICN isomer is close to that obtained earlier for TIF [27] and the analogous parameter for the Ra nucleus in RaO [46]. We conclude that the TICN molecule has good prospects for searching for effects outside of the Standard Model.

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