



Article Binary Aquila Optimizer for Selecting Effective Features from Medical Data: A COVID-19 Case Study

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Abstract: Medical technological advancements have led to the creation of various large datasets with numerous attributes. The presence of redundant and irrelevant features in datasets negatively influences algorithms and leads to decreases in the performance of the algorithms. Using effective features in data mining and analyzing tasks such as classification can increase the accuracy of the results and relevant decisions made by decision-makers using them. This increase can become more acute when dealing with challenging, large-scale problems in medical applications. Nature-inspired metaheuristics show superior performance in finding optimal feature subsets in the literature. As a seminal attempt, a wrapper feature selection approach is presented on the basis of the newly proposed Aquila optimizer (AO) in this work. In this regard, the wrapper approach uses AO as a search algorithm in order to discover the most effective feature subset. S-shaped binary Aquila optimizer (SBAO) and V-shaped binary Aquila optimizer (VBAO) are two binary algorithms suggested for feature selection in medical datasets. Binary position vectors are generated utilizing S- and V-shaped transfer functions while the search space stays continuous. The suggested algorithms are compared to six recent binary optimization algorithms on seven benchmark medical datasets. In comparison to the comparative algorithms, the gained results demonstrate that using both proposed BAO variants can improve the classification accuracy on these medical datasets. The proposed algorithm is also tested on the real-dataset COVID-19. The findings testified that SBAO outperforms comparative algorithms regarding the least number of selected features with the highest accuracy.

Keywords: transfer function; medical data; nature-inspired algorithm; binary metaheuristic algorithm; feature selection

MSC: 68T20

1. Introduction

It is difficult and frequently imprecise to analyze big amounts of data in real-world problems such as engineering, health, biology, or tourism, due to the presence of massive volumes of data. This massive data, often called big data, contains a combination of features with relevant/irrelevant, redundant, or noisy characteristics [1]. Therefore, selecting effective features is an essential pre-processing technique and prominent data analysis task. Feature selection is regarded as a searching or optimization task since its objective is to find effective features that utilize to enhance classification performance [2]. Furthermore, reducing the complexity and ditching irrelevant and redundant features while enhancing the algorithms' performance are the main aims of feature selection approaches. Feature



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). selection is also often called dimensionality reduction, which has a variety of applications in various areas, including but not limited to image analysis, biomedical problems, text mining, and industrial applications.

The literature classifies feature selection strategies into two categories, filter and wrapper approaches, depending on their interaction with the classifier [3]. The former method finds the optimum subset of features based on measures such as distance, dependency, or consistency of the features. The latter method employs a learning algorithm, such as a classifier, to continuously assess the feature subset during the search process to locate optimal solutions from an exponential collection of features [3]. Although filter techniques are faster than wrapper methods since they do not consume additional processing time to invoke the learning algorithm [4], their major drawback is that features do not affect the classifier's performance [5]. Meanwhile, the wrapper approaches are more accurate but computationally more costly [6]. Thus, it is required to employ an optimization algorithm in order to achieve an optimal set of features.

As mentioned above, the process of selecting features can be considered an optimization issue since it aims to identify a subset of features with near-optimal fitness. Considering the proof that the number of the proper subsets in a dataset with Q features is 2^{Q} -1, feature selection can be regarded as an NP-hard problem. Thus, finding the best subset of features is impractical by using exact search strategies [7], and approximate approaches such as metaheuristic algorithms can be used to select effective features within a reasonable time [8]. Optimization algorithms have numerous advantages over conventional search algorithms, including the capability of identifying the optimal subset of features within a reasonable time. Furthermore, the conventional search algorithms require generating all possible feature subsets to find the optimum solution, which is unsuitable and time-consuming for large datasets [9].

Metaheuristics are designed to solve challenging optimization problems and provide acceptable solutions in a reasonable time [8]. Such general-purpose algorithms have the potential to locate the search space promising regions and the ability to estimate an appropriate solution for a particular optimization issue. In addition, metaheuristic algorithms utilize stochastic strategies to foster population diversity in the early stages of iterations by searching in the target domain. Meanwhile, the algorithm searches for potential solutions locally in the exploitation phase to improve upon the quality of solutions found in the exploration phase. After a limited number of iterations, a reasonable convergence occurs, meaning that the algorithm does not provide more improvement to the solution. Black-box nature, simplicity, ease of use, and high global search capability are the main reasons for the popularity of such algorithms in diverse areas [10]. Some of the trending application areas are: classification [11,12], power and energy management [13–16], structural engineering [17–19], community detection [20], clustering [21–24], image segmentation [25–28], global optimization [29-35], industrial engineering [36,37], life-cycle cost analysis in structural optimization [38], engineering design problem [39–41], task scheduling [42–44] and virtual machine placement [45,46] in cloud computing, navigation planning [47–49], and wind speed prediction [50,51].

Metaheuristic algorithms are mostly nature-inspired and are designed to emulate the biological, physical, and social behaviors of species found in nature. We can group them into three categories: evolution-based, swarm intelligence-based, and physics-based algorithms [52]. Evolution-based algorithms tend to mimic creatures' evolutionary behavior concepts in nature. Some of the most well-regarded evolutionary algorithms are genetic programming (GP) [53], evolution strategy (ES) [54], differential evolution (DE) [55], evolutionary programming (EP) [56], genetic algorithm (GA) [57], and biogeography-based optimization (BBO) [58]. The social and collective behavior of swarms in nature, such as those in colonies of bees, ants, animal herds, and birds' flocks, are the source of inspiration for swarm intelligence algorithms. Among this category, the most popular algorithms are particle swarm optimization (PSO) [59], ant colony optimization (ACO) [60], artificial bee colony (ABC) [61], and bat algorithm (BA) [62]. Algorithms based on the fundamental physical rules existing in nature comprise the last category. Simulated annealing (SA) [63], thermal exchange optimization (TEO) [64], big bang-big crunch (BB-BC) [65], and atom search optimization (ASO) [66] are some notable examples of this category. Although the proposed algorithms are designed and evaluated on different kinds of problems, the No-free-lunch (NFL) theorem [67] states that there is no general-purpose algorithm that is suitable for tackling all problems with various characteristics. Thus, the algorithms such as multi-trial vector-based differential evolution (MTDE) [68], multi-strategy enhanced HHO algorithm (RLHHO) [69], and gaze cues learning-based grey wolf optimizer (GGWO) [70] were proposed to overcome the shortcoming of the existing algorithms.

This paper attempts to find effective features by utilizing the Aquila optimizer (AO) [71] algorithm, which is one of the most recent optimization algorithms to be published. The AO mimics Aquila's hunting strategies in nature. Fast-moving prey hunting techniques reveal the algorithm's global exploration capability, whereas slow-moving prey hunting strategies show the algorithm's local exploitation capability. The canonical AO operates on the continuous solution search space and cannot be performed on problems with discrete, binary, or mixed-integer variables. Thus, we propose a wrapper-based binary metaheuristic algorithm named BAO to select effective features from seven medical datasets. The BAO algorithm calculates the position of solutions in the binary space using S and V-shaped transfer functions while the AO's search space remains continuous.

The following is how the rest of this article is structured: Section 2 provides a literature review of binary metaheuristic algorithms applicable to feature selection. The continuous Aquila optimizer algorithm is discussed in Section 3. Section 4 describes the suggested binary versions of the Aquila optimizer algorithm. Section 5 discusses the suggested algorithms for the feature selection problem, whereas Section 6 shows the experimental findings and statistical analysis on medical datasets. In Section 7, the applicability of the proposed algorithm on the COVID-19 dataset is assessed and compared with comparative algorithms. Finally, Section 8 concludes the work, and future research is suggested.

2. Related Work

In applications that rely on machine learning classifiers such as data mining, classification is considered to be an essential process. However, the type of features used, some of which are usually irrelevant and noisy, has a significant effect on the performance of these classifiers. Feature selection can minimize the dimensionality of data, reduce classifier learning time, and enhance classification result by choosing the most effective features and eliminating the redundant and irrelevant features [72]. Many practical applications have used feature selection including intrusion detection [73,74], software fault prediction [75,76], speech emotion recognition [77,78], bankruptcy prediction [79,80], credit scoring [81], stock trend prediction [82], emotion analysis [83], spam detection [84,85], digital soil mapping [86], diseases prediction and detection [87–90], breath analysis [91], biodiesel property selection [92], gene selection [93,94], and wind forecasting [95,96].

As stated, feature selection has an essential role in dimensionality reduction since it removes irrelevant and redundant features from the original dataset to find an optimal subset of features. In the following paragraphs, our focus is on reviewing the feature selection methods that use metaheuristics as search algorithms and rely on using transfer functions. The challenge of selecting effective features from an entire set of features is a discrete optimization problem that can be handled by metaheuristics. Metaheuristic algorithms, in which the search is directed by information gained during the optimization process, are practical approaches for solving feature selection problems. Most of the well-regarded nature-inspired algorithms were designed to address continuous optimization issues, whereas some problems are binary in nature. Furthermore, other strategies for adapting continuous metaheuristic algorithms into discrete domains have also been proposed, such as normalizing, rounding, and utilizing binary operators [97]. The transfer

function can also be used as another method of converting continuous components into binary values.

Due to the binary nature of feature selection, transfer functions are efficient yet easy ways to limit the result such that 0 means the feature is redundant and not chosen, and 1 represents the feature is useful and chosen. Transfer functions based on their shape have been divided into three groups S-shaped, V-shaped, and U-shaped transfer functions [98–101]. In prominent algorithms such as BPSO [98], binary differential evolution (binDE) [102], and altruistic whale optimization algorithm (AltWOA) [103], the S-shaped transfer function was employed to estimate the probabilities of shifting positions. In [104], a V-shaped transfer function is applied to the velocity parameter of the continuous gravitational search algorithm to handle the feature selection.

In [105], two binary variants were suggested for feature selection with the GWO algorithm as a state-of-the-art algorithm. In the first version, the position changing estimation for each wolf is accomplished by utilizing an S-shaped transfer function to their respective positions. The second variant converted the continuous GWO to a binary version via stochastic crossover. In [106], the binary butterfly optimization algorithm (bBOA) was proposed to address feature selection issues by using both S-shaped and V-shaped transfer functions. Each feature subset is represented as a butterfly, and global and local strategies are used during the search process. However, there are certain flaws with bBOA, such that it cannot balance the exploration and exploitation, and in the local search strategy, butterflies merely change their position at random, which is regarded as insufficient [107]. In another similar work [108], a wrapper-based binary SCA (WBSCA) was proposed that transformed continuous SCA to binary search space by utilizing the V-shaped transfer function. An improved binary PSO algorithm (ISBPSO) [109] is proposed for selecting features and used in classification in recent work. The performance of the canonical PSO algorithm is improved by adapting three strategies to obtain a better initial population, global search, and convergence property. The proposed ISBPSO is used as a wrapper to select features and validated on 12 UCI datasets. The comparison of obtained results by other feature selection algorithms shows that it can obtain higher or similar accuracy with fewer selected features. Another study [110] proposed a wrapper method for selecting features, which used MFO as a search strategy. This method used twelve different transfer functions of S, V, and U-shaped to transform MFO from the continuous version to a binary one. The proposed variants and wrapper-based comparative algorithms were tested and compared on medical datasets to confirm competitive performance.

In [111], a binary horse herd optimization algorithm (BHOA) is proposed to tackle feature selection problems. In BHOA, four configurations of the S, V, and U-shaped functions are utilized for mapping the HOA to its binary equivalent. Another proposed binary algorithm for feature selection is binary biogeography-based optimization based SVM-RFE (BBO-SVM-RFE) [112]. The support vector machine recursive feature elimination is incorporated into the BBO to enhance the quality of the acquired solutions in the mutation operator, thereby improving the balance between the exploitative and exploratory aspects of the original BBO. On the basis of the accuracy and the number of considered features, the BBO-SVM-REF algorithm surpasses the BBO method and other wrapper and filter methods. The usage of optimization algorithms is advantageous in selecting features because they can produce a solution near to the optimum or ideal in a reasonable amount of time. Contrary to this, conventional exhaustive search methods search through every possible combination of features from the entire feature set, which is time-consuming and regarded as an NP-hard task. Despite the fact that various metaheuristic algorithms for dealing with feature selection have been developed over time, the increasing dimensionality of data presents significant challenges; therefore, it is worthwhile to continue searching for effective strategies to improve the performance of metaheuristic algorithms to deal with high-dimensional feature selection issues.

3. Aquila Optimizer (AO)

In accordance with the natural Aquila hunting process, the Aquila optimizer (AO) [71] is a newly proposed algorithm. The hunting process has four steps: expanded exploration by soaring high with a vertical stoop, narrowed exploration by gliding with a contour flight, expanded exploitation by low-flying descent attack, and narrowed exploitation by walking and catching prey. In order to transit from the exploration stage to the exploitation stage, the AO algorithm uses a variety of behaviors. The exploration stage is simulated in the first two-thirds of iterations, while the exploitation stage is imitated in the last one-third of iterations. The following is a mathematical representation of the AO algorithm.

Initializing: The AO algorithm begins by spreading *N* solutions in a *D*-dimensional search space across a preset range [*L*, *U*] by applying Equation (1).

$$X_{i,j} = L_j + r \times (U_j - L_j) \tag{1}$$

where $X_{i,j}$ is the *j*-th dimension of the *i*-th solution, L_j and U_j refer to the lower and upper bound value of the *j*-th dimension in the search space, and *r* is chosen at random from the range of 0 to 1. The position of solutions is kept in matrix $X_{N \times D}$. Then, by $f(X_i)$, the fitness value of each solution is calculated.

Expanded exploration: An Aquila first determines the prey region and picks the optimal hunting location by high-soaring while stooping vertically. This behavior leads to the search space being explored from high altitudes to estimate where the prey can be located. In AO, this behavior is simulated to expand the exploration by Equation (2) and is executed when *iter* < $(2/3 \times MaxIter)$ and randomly generated value < 0.5,

$$X_1(iter+1) = X_{best}(iter) \times (1 - \frac{iter}{MaxIter}) + (X_M(iter) - X_{best}(iter) \times r)$$
(2)

where $X_1(iter + 1)$ is the solution given by the prime method to use in the subsequent iteration and $X_{best}(iter)$ is the best solution found until the current iteration and approximates the position of prey. The $(1 - \frac{iter}{Max|ter})$ term is utilized to regulate the extent of the exploration based on the number of iterations, where *iter* denotes the current iteration and *MaxIter* is the number of iterations that can be performed. In the *iter-th* iteration, $X_M(iter)$ indicates the mean of currently available solutions, as determined by Equation (3),

$$X_M(iter) = \frac{1}{N} \sum_{i=1}^{N} X_i(iter), \, \forall \, j = 1, 2, \dots, D$$
(3)

where *D* denotes the dimension size of the search space and *N* represents the number of solutions.

Narrowed exploration: In the second step, the hunting behavior named contour flight of a short glide attack is performed. Aquila flies over the targeted prey, prepares to descend, and attacks when spotted from a high height. This behavior allows the Aquila to explore a specific region narrowly. In AO, this behavior is simulated to narrow the exploration by Equation (4) and is done when *iter* < $(2/3 \times MaxIter)$ and randomly generated value > 0.5,

$$X_2(iter + 1) = X_{best}(iter) \times Levy(D) + X_R(iter) + (y - x) \times r$$
(4)

where $X_2(iter + 1)$, $X_R(iter)$, and Levy(D) represent the solutions produced by the narrowed exploration strategy, a randomly selected solution from entire solutions in the *iter*-th iteration, and the Levy flight distribution function calculated by Equation (5), respectively.

$$Levy(D) = s \times \frac{u \times \sigma}{|v|^{\frac{1}{\beta}}}, \ \sigma = \left(\frac{\Gamma(1+\beta) \times \sin(\frac{\pi p}{2})}{\Gamma(\frac{1+\beta}{2}) \times \beta \times 2^{(\frac{\beta-1}{2})}}\right)$$
(5)

-0

where s = 0.01, $\beta = 1.5$, and u and v are random integer numbers ranging in [0, 1]. In Equation (4), the spiral form is represented by y and x calculated using Equation (6),

$$y = p \times \cos(\theta), \ x = p \times \sin(\theta)$$
 (6)

where *r* and θ are calculated by Equations (7) and (8),

$$p = r_1 + U \times D_1 \tag{7}$$

$$\theta = -\omega \times D_1 + \theta_1, \ \theta_1 = \frac{3 \times \pi}{2} \tag{8}$$

where the number of search cycles is fixed by the random number r_1 which is between 1 and 20, D_1 is an integer value in the range of 1 to D, U = 0.00565, and $\omega = 0.005$.

Expanded exploitation: Aquila employs the third strategy to pursue prey during the expanded exploitation step. The Aquila has carefully identified the prey zone and is prepared to alight and attack. In order to determine how the prey would respond to the attack, the Aquila descends vertically and performs the first strike. This behavior is named low-flying descent attack and is performed when *iter* > ($2/3 \times MaxIter$) and randomly generated value < 0.5 by Equation (9).

$$X_3(iter+1) = (X_{best}(iter) - X_M(iter)) \times \alpha - r + ((U-L) \times r + L) \times \delta$$
(9)

where $X_3(iter + 1)$ denotes the solutions obtained by the expanded exploitation method and the exploitation adjustment parameters α and δ are set to 0.1.

Narrowed exploitation: The fourth hunting strategy is used during the narrower exploitation step when the Aquila approaches the prey and attacks randomly. This behavior is called walking and grabbing the prey and is done when *iter* > $(2/3 \times MaxIter)$ and randomly generated value > 0.5 by Equation (10).

$$X_4(iter+1) = QF(iter) \times X_{best}(iter) - (G_1 \times X(iter) \times r) - G_2 \times Levy(D) + r \times G_1$$
(10)

where $X_4(iter + 1)$ denotes the generated fourth search solutions, X(iter) is the *iter*-th iteration's current solution, and to balance the search strategy, a quality function called *QF* is calculated by Equation (11).

$$QF(iter) = t^{\frac{2 \times r - 1}{(1 - MaxIter)^2}}$$
(11)

 G_1 and G_2 are values to represent the Aquila's prey tracking movements such that the G_2 's value is decreasing from 2 to 0. The calculation of G_1 and G_2 are done by Equations (12) and (13).

$$G_1 = 2 \times r - 1 \tag{12}$$

$$G_2 = 2 \times \left(1 - \frac{iter}{MaxIter}\right) \tag{13}$$

The AO algorithm is inspired by Aquila's natural behavior and shown a competitive performance when adapted to solve optimization problems [113]. The algorithm's global exploration ability is shown by the hunting strategies for fast-moving prey, while the algorithm's local exploitation capability is demonstrated by the hunting approaches for slow-moving prey. The AO algorithm has a high search efficiency, fast convergence speed, and good global exploration but lacks local exploitation, making it susceptible to get trapped in the local optimum [114]. The BAO's major goal is to tackle the restriction of the continuous AO to solve feature selection problems by utilizing its binary form.

4. Binary Aquila Optimizer (BAO) Algorithm

A binary optimization problem's search space can be considered a hypercube, which allows an individual to move from one point to another by altering one or more bits of its position. Since binary space contains only two values, "0" and "1", the position updating for binary optimization issues such as feature selection cannot be achieved by continuous strategies. Transfer functions are one of the key components of metaheuristic-based feature selection algorithms, in which the continuous search space is mapped to the discrete space. Transfer functions are used to assess the probability of altering the elements of a position vector to 0 or 1 based on the value of the *i*-th solution's vector in the *d*-th dimension. S-shaped and V-shaped transfer functions are the two most prevalent forms of transfer functions [98,99] such that continuous metaheuristic algorithms can be discretized and utilized to solve binary optimization problems by converting a real vector into a binary vector. In Table 1 and Figure 1, formulation and visual representation of these two families of transfer functions are provided.

S-Shaped Tr	ansfer Functions	V-Shaped T	Transfer Functions
Name	Function	Name	Function
S1	$T(x) = \frac{1}{1+e^{-2(x)}}$	V1	$T(x) = \left \frac{\sqrt{2}}{\pi} \int_0^{(\sqrt{\pi}/2)x} e^{-t^2} dt \right $
S2	$T(x) = \frac{1}{1 + e^{-x}}$	V2	$T(x) = \tanh(x) $
S3	$T(x) = \frac{1}{1+e^{(-x/2)}}$	V3	$T(x) = \left (x)\sqrt{1+x^2} \right $
S4	$T(x) = \frac{1}{1+e^{(-x/3)}}$	V4	$T(x) = \left \frac{2}{\pi}\arctan(\frac{\pi}{2})x\right $

Table 1. List of transfer functions.

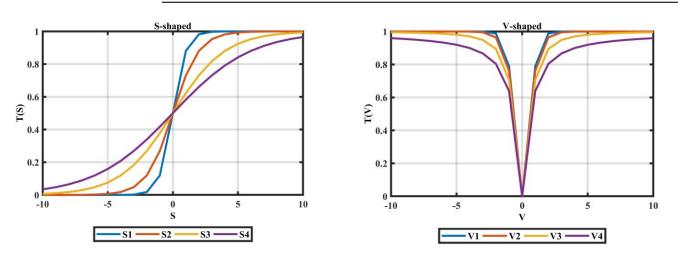


Figure 1. S-shaped and V-shaped transfer functions.

Although the AO algorithm was initially suggested to solve continuous optimization issues, it has to be adapted to accommodate the binary challenge of feature selection. Therefore, in order to solve binary problems through the use of AO, a transfer function needs to be used to convert a solution vector with continuous values into a probability vector. The transfer functions of both families are utilized to adapt continuous AO to binary variants called SBAO and VBAO in this study. Specifically, eight different transfer functions are considered, which result in eight distinct BAO variations.

4.1. S-Shaped Binary Aquila Optimizer (SBAO) Algorithm

The suggested variants of the BAO algorithm treat the search space as a continuous space where every solution has a real-valued position vector. The continuous values in the search space must be mapped to binary values using our proposed algorithms to derive a binary position vector for the solution. Each dimension of the position is taken into account by applying a particular S-shaped transfer function to compel the solution to move around in binary space. Using the floating-point position values, the transfer function calculates a limited probability in the interval [0, 1] for each solution. A floating-point

vector is then converted to a bit-string position vector based on the obtained probabilities. In Equation (14), the S-shaped function is given for generating probability value.

$$S(X_i^d(iter+1)) = \frac{1}{1 + e^{(-X_i^d(iter)/3)}}$$
(14)

The value of $S(X_i^d(iter + 1))$ denotes the possibility of altering the *i*-th solution's binary position value in the *d*-th dimension. After comparing the probability to a threshold value, the binary value is calculated, as shown in Equation (15), where *rand* is a random value between 0 and 1.

$$X_i^d(iter+1) = \begin{cases} 1 & , if rand \le S(X_i^d(iter+1)) \\ 0 & , otherwise \end{cases}$$
(15)

4.2. V-Shaped Binary Aquila Optimizer (VBAO) Algorithm

The V-shaped transfer function is another function used to calculate the possibility of changing positions. Similar to the S-shaped transfer function, the V-shaped transfer function is also used to calculate the probability of changing the search agent's location by Equation (16).

$$V(X_i^d(iter+1)) = \left|\frac{2}{\pi}\arctan(\frac{\pi}{2})(X_i^d(iter))\right|$$
(16)

Following the changing probability values calculation, each search agent's binary position vector is updated using an updating position equation, as shown in Equation (17), where *rand* is a random value between 0 and 1.

$$X_{i}^{d}(iter+1) = \begin{cases} complement(X_{i}^{d}(iter)) & , if rand \leq V(X_{i}^{d}(iter+1)) \\ X_{i}^{d}(iter) & , otherwise \end{cases}$$
(17)

The continuous Aquila Optimizer (AO) is converted into its binary variant (BAO) by transforming each search agent's dimension to a probability value ranging from 0 to 1 as given in Equation (2). This is done utilizing all variations of S-shaped and V-shaped transfer functions. Therefore, the probability of changing each search agent's position is calculated through the use of either S-shaped or V-shaped transfer functions shown by Equations (14) and (16). Then, the binary position of the search agent is obtained by considering the calculated changing probability value using Equation (15) or (17). To identify the appropriate transfer function, eight different variants of the suggested BAO are examined since transforming a continuous search space to a binary domain greatly affects the performance and results of classifiers. The pseudo-code of the proposed BAO algorithm is shown in Algorithm 1. BAO has an O(NDT) computational complexity, where N, D, and T are the population size, the number of features, and the maximum number of iterations, respectively.

Algorithm 1. The binary Aquila optimizer (BAO)Input: N (population size), D (the dimension's number), MaxIter (maximum num iterations)Output: The best solution (X_{best}) 1:Begin2:Initializing iter = 1, $\alpha = 0.1$, $\delta = 0.1$.3:Generating a random initial population X.4:While it $\leq MaxIter$ 5:Evaluating the fitness function values and set the $X_{best}(it)$.6:If iter < (2/3) × MaxIter7:If rand < 0.58:Calculating $X_1(iter + 1)$ using Equation (2).9:Updating $X(iter + 1)$ and $X_{best}(iter)$.10:else11:Calculating $X_2(iter + 1)$ using Equation (4).12:Updating $X(iter + 1)$ and $X_{best}(iter)$.13:End if14:else15:If rand < 0.5 then16:Calculating $X_3(iter + 1)$ using Equation (9).17:Updating $X(iter + 1)$ and $X_{best}(iter)$.	
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7:If $rand < 0.5$ 8:Calculating $X_1(iter + 1)$ using Equation (2).9:Updating $X(iter + 1)$ and $X_{best}(iter)$.10:else11:Calculating $X_2(iter + 1)$ using Equation (4).12:Updating $X(iter + 1)$ and $X_{best}(iter)$.13:End if14:else15:If $rand < 0.5$ then16:Calculating $X_3(iter + 1)$ using Equation (9).	
8 :Calculating $X_1(iter + 1)$ using Equation (2).9 :Updating $X(iter + 1)$ and $X_{best}(iter)$.10 :else11 :Calculating $X_2(iter + 1)$ using Equation (4).12 :Updating $X(iter + 1)$ and $X_{best}(iter)$.13 :End if14 :else15 :If rand < 0.5 then	
9:Updating $X(iter + 1)$ and $X_{best}(iter)$.10:else11:Calculating $X_2(iter + 1)$ using Equation (4).12:Updating $X(iter + 1)$ and $X_{best}(iter)$.13:End if14:else15:If rand < 0.5 then16:Calculating $X_3(iter + 1)$ using Equation (9).	
10:else11:Calculating $X_2(iter + 1)$ using Equation (4).12:Updating $X(iter + 1)$ and $X_{best}(iter)$.13:End if14:else15:If rand < 0.5 then	
11 :Calculating $X_2(iter + 1)$ using Equation (4).12 :Updating $X(iter + 1)$ and $X_{best}(iter)$.13 :End if14 :else15 :If rand < 0.5 then	
12 :Updating $X(iter + 1)$ and $X_{best}(iter)$.13 :End if14 :else15 :If rand < 0.5 then16 :Calculating $X_3(iter + 1)$ using Equation (9).	
13 :End if14 :else15 :If rand < 0.5 then16 :Calculating $X_3(iter + 1)$ using Equation (9).	
$14:$ else $15:$ If rand < 0.5 then	
15:If rand < 0.5 then16:Calculating $X_3(iter + 1)$ using Equation (9).	
16: Calculating $X_3(iter + 1)$ using Equation (9).	
17. Updating $X(iter + 1)$ and X_{i} (iter)	
$\Delta p_{\text{and}} \Delta p_{\text{and}} \Delta p_{\text{and}} \Delta p_{\text{and}} \Delta p_{\text{est}}(\mu \sigma)$	
18 : Else	
19: Calculating $X_4(iter + 1)$ using Equation (10).	
20: Updating $X(iter + 1)$ and $X_{hest}(iter)$.	
21: End if	
22 : End if	
23 : Calculating the probability values using Equation (14) or (16).	
24 : Updating binary position.	
25: <i>iter</i> = <i>iter</i> + 1.	
26 : End while	
27 : Return the best solution (X_{best}).	
28 : End	

5. Binary Aquila Optimizer Algorithm for Feature Selection Problem

Feature selection entails identifying relevant features in a dataset to enhance learning capabilities, reduce computation complexity, and improve classification performance. The optimum feature subset is obtained using a binary algorithm depending on the nature of the feature selection problem. Using the binary approach, each solution is represented by binary vectors with *D* entries, reflecting the number of features in a dataset. Each entry of the solution vector has a value of 0 or 1, where 0 signifies no selection and 1 indicates the selection of that particular feature. The feature selection problem is addressed by utilizing two binary variants of the AO algorithm. As a multi-objective problem, the problem of features selection requires the fulfillment of two conflicting objectives. This is a conflict between objectively maximizing accuracy and minimizing the selection of features. The weighted sum multi-objective fitness function for evaluating each solution is shown in Equation (18).

$$Fitness = \alpha E_R(D) + \beta \frac{|R|}{|C|}$$
(18)

where α and β are two factors that represent the weight of accuracy and the number of selected features and their values are set in the range of $\alpha \in [0, 1]$ and $\beta = 1 - \alpha$ [105]. The classification error, the number of chosen features, and the total number of features are represented by $E_R(D)$, |R|, and |C|, respectively.

6. Experimental Evaluation and Results

An evaluation of the performance of variants of SBAO and VBAO algorithms is presented in this section by presenting detailed experimental results and statistical analysis. To assess the efficiency of the BAO algorithms, these experiments include performance evaluation and convergence evaluation. In the comparative experiment, the gained results are assessed along with the state-of-the-art and recently developed nature-inspired algorithms consisting of binary bat algorithm (BBA) [115], binary gravitational search algorithm (BGSA) [104], binary grey wolf optimization (BGWO) [105], binary dragonfly algorithm (BDA) [116], S-shaped binary sine cosine algorithm (SBSCA) [117], and V-shaped binary sine cosine algorithm (VBSCA) [117]. Moreover, a non-parametric statistical test, known as the Friedman test [118], is used to demonstrate the significance of the difference between the gained results and comparative algorithms. Additionally, we performed an experiment on the COVID-19 dataset and compared the gained results by comparative algorithms.

6.1. Datasets Description and Experimental Environment

The proposed BAO algorithms were validated on seven medical datasets selected from [119,120] with varying numbers of features and instances. A detailed description of each dataset is provided in Table 2, including the number of instances, features, and classes. As part of the evaluation process, each dataset was split into two sets: a training set and a testing set, with 80% of the instances used for training and the remainder for testing. In this wrapper approach, the k-nearest neighbors (k-NN) method is employed to estimate the classification error rate of the selected feature subset. The proposed algorithms were developed by Matlab programming environment R2014b, and all experiments were run on a CPU, Intel Core(TM) i7-3770 at 3.4 GHz and 8.00 GB RAM.

Dataset	No. of Instances	No. of Features	No. of Classes
Heart	270	14	2
Breast Cancer	683	10	2
Pima	768	9	2
Breast-WDBC	569	31	2
Lymphography	148	19	4
Colon	62	2000	2
Leukemia	72	7129	2

Table 2. Statistical information of datasets.

6.2. Experimental Setup

Throughout this work, all of the comparative algorithms' parameters were set as in their original works, as indicated in Table 3. The appropriate values for the parameters α and δ are found by some pretests reported in Appendix A. To gain meaningful results, all experiments were done and evaluated by 30 separate runs. All algorithms' initial settings were set to the same maximum iterations (*MaxIter*) and population size (*N*) to 300 and 20 to ensure fair comparisons. The value of α and β parameters in the fitness function in Equation (18) are set by 0.99 and 0.01, and the value of parameter *k* is set with 5 in the k-NN classifier, respectively. As an evaluation criterion, all algorithms use classification accuracy and the number of selected features. The algorithms' performance was measured using mean and standard deviation (SD) of accuracy, the number of selected features, and the gained fitness.

6.3. Performance Evaluation of SBAO and VBAO

In this subsection, seven medical datasets are used to benchmark various variants of the proposed BAO to determine the impact of different transfer functions on the proposed algorithm's performance. The BAO variants utilize eight transfer functions listed in Table 1. The efficacy of the variants is evaluated by the mean and standard deviation of accuracy, the number of selected features, and the gained fitness. Tables 4–6 provide a summarization of the gained results achieved by the algorithms. In Table 4, the mean and SD for the

accuracy of eight variants of BAO with S-shaped and V-shaped transfer functions in 30 runs are tabulated. As per results in Table 4, the variants SBAO-2, SBAO-3, SBAO-4, and VBAO-1, VBAO-3, and VBAO-4 provided the highest accuracy in the Pima dataset. All the variants gained the same and superior accuracy in the Breast cancer dataset. In Heart and Lymphography datasets, the BAO versions that utilize transfer functions S4 and V4 can achieve better accuracy than the other variants. SBAO-3 and VBAO-3 outperform other variants in terms of accuracy in the Breast-WDBC dataset. In the Colon dataset, SBAO-1, SBAO-2, and VBAO-1 and in the Leukemia dataset, SBAO-2 and VBAO-1 obtain the best results that show the binary AO's performance in selecting features from large datasets.

Algorithm	Parameter	Value
BSCA	а	2
	А	0.5
BBA	r	0.5
DDA	Q _{min}	0
	Q _{max}	2
BGSA	G ₀	100
BGWO	a	[2 0]
BAO	α and δ	0.1

 Table 3. Algorithms parameter settings.

Table 4. The accuracy comparison of SBAO and VBAO.

Dataset	Metric	SBAO-1	SBAO-2	SBAO-3	SBAO-4	VBAO-1	VBAO-2	VBAO-3	VBAO-4
	Mean acc.	0.772	0.773	0.773	0.773	0.773	0.772	0.773	0.773
Pima	SD acc.	0.001	0.000	0.000	0.000	0.000	0.003	0.000	0.000
D	Mean acc.	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
Breast Cancer	SD acc.	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	Mean acc.	0.894	0.896	0.894	0.898	0.887	0.885	0.892	0.896
Heart	SD acc.	0.009	0.009	0.009	0.009	0.010	0.014	0.011	0.012
T 1 1	Mean acc.	0.862	0.864	0.867	0.871	0.862	0.860	0.867	0.869
Lymphography	SD acc.	0.024	0.026	0.028	0.024	0.024	0.025	0.030	0.015
D. HUDDO	Mean acc.	0.967	0.967	0.967	0.967	0.964	0.964	0.965	0.965
Breast-WDBC	SD acc.	0.004	0.004	0.004	0.004	0.002	0.002	0.002	0.000
	Mean acc.	0.950	0.950	0.925	0.925	0.875	0.858	0.850	0.858
Colon	SD acc.	0.056	0.041	0.025	0.045	0.042	0.038	0.033	0.038
	Mean acc.	0.9714	0.9929	0.9786	0.9571	0.9429	0.9357	0.9286	0.9357
Leukemia	SD acc.	0.0356	0.0218	0.0333	0.0356	0.0436	0.0391	0.0325	0.0218

As tabulated in Table 5, the mean and standard deviation of selected features are calculated for 30 independent runs using BAO variants. It can be observed that SBAO-1 and VBAO-2 can be achieved better results in the Pima dataset. The BAO with S-shaped and V-shaped transfer functions except the fourth S-shaped function have achieved the same best number of selected features in the Breast cancer dataset. In the Heart dataset, both transfer functions S1 and V1 in BAO achieved the minimum selection of features. For the Lymphography dataset, SBAO-1, SBAO-3, and SBAO-4 have shown equal performance, whereas VBAO-1 has better performance in comparison to other V-shaped variants. SBAO-2 and VBAO-4 achieved better performance for the Breast-WDBC dataset. In the Colon dataset, SBAO-4 and VBAO-2 and in Leukemia, SBAO-2 and VBAO-1 had better performance than other variants. Table 6 demonstrates the proposed algorithms' results

regarding the mean and SD of the gained fitness values. The results demonstrate the impact of utilizing various transfer functions on the BAO's performance.

Dataset	Metric	SBAO-1	SBAO-2	SBAO-3	SBAO-4	VBAO-1	VBAO-2	VBAO-3	VBAO-4
	Mean	4.97	5.00	5.00	5.00	5.00	4.97	5.00	5.00
Pima	SD	0.18	0.00	0.00	0.00	0.00	0.18	0.00	0.00
D	Mean	3.00	3.00	3.00	3.07	3.00	3.00	3.00	3.00
Breast Cancer	SD	0.00	0.00	0.00	0.25	0.00	0.00	0.00	0.00
	Mean	4.90	5.60	5.00	5.50	5.00	5.10	5.40	6.30
Heart -	SD	1.40	1.45	1.36	1.53	1.20	1.32	1.30	1.02
T 1 1	Mean	5.73	6.27	5.73	5.73	7.20	8.07	7.73	7.47
Lymphography -	SD	1.95	2.18	1.36	1.20	1.45	2.12	1.84	1.57
	Mean	5.00	4.13	4.53	4.87	9.80	10.13	9.80	9.07
Breast-WDBC	SD	2.03	1.22	1.74	1.70	2.41	1.85	1.49	1.08
	Mean	120.10	118.10	133.80	107.60	47.50	35.70	85.60	134.00
Colon -	SD	202.62	281.94	342.86	165.75	55.20	27.25	83.63	108.07
	Mean	1316.70	1151.80	1739.80	2111.30	228.50	1151.90	1457.60	2651.80
Leukemia ⁻	SD	520.27	1300.27	1220.66	1177.89	161.25	1321.51	1483.56	1099.86

Table 5. The number of selected features comparison of SBAO and VBAO.

Table 6. The fitness comparison of SBAO and VBAO.

Dataset	Metric	SBAO-1	SBAO-2	SBAO-3	SBAO-4	VBAO-1	VBAO-2	VBAO-3	VBAO-4
Pima	Mean fitness	0.231	0.231	0.231	0.231	0.231	0.231	0.231	0.231
	SD fitness	0.001	0.000	0.000	0.000	0.000	0.002	0.000	0.000
Breast Cancer	Mean fitness	0.003	0.003	0.003	0.003	0.003	0.003	0.003	0.003
	SD fitness	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Heart	Mean fitness	0.108	0.107	0.108	0.105	0.115	0.117	0.110	0.107
	SD fitness	0.007	0.008	0.007	0.008	0.009	0.013	0.010	0.011
Lymphography	Mean fitness	0.139	0.137	0.135	0.130	0.140	0.143	0.136	0.133
	SD fitness	0.023	0.025	0.026	0.023	0.023	0.024	0.029	0.014
Breast-WDBC	Mean fitness	0.034	0.034	0.033	0.034	0.038	0.038	0.037	0.037
	SD fitness	0.004	0.003	0.004	0.003	0.002	0.002	0.002	0.000
Colon	Mean fitness	0.050	0.050	0.074	0.074	0.124	0.140	0.148	0.140
	SD fitness	0.055	0.041	0.025	0.045	0.041	0.038	0.033	0.038
Leukemia	Mean fitness	0.030	0.008	0.023	0.045	0.056	0.065	0.072	0.067
Deuxennu	SD fitness	0.034	0.021	0.032	0.034	0.043	0.039	0.032	0.022

6.4. Performance Comparison with State-of-the-Art Algorithms

In this subsection, the obtained results of the proposed binary versions of the AO, SBAO, and VBAO for each dataset are compared with other binary state-of-the-art algorithms that are widely used to solve the feature selection problem. To compare with other comparative algorithms, for each dataset, one variant of S-shaped and V-shaped transfer functions was selected such that the variant provides better performance in terms of accuracy. This selection of SBAO and VBAO for each dataset is as follows: Pima (SBAO-1, VBAO-2), Breast cancer (SBAO-1, VBAO-1), Heart (SBAO-4, VBAO-4), Lymphography (SBAO-4, VBAO-4), Breast-WDBC (SBAO-3, VBAO-3), Colon (SBAO-2, VBAO-1), and Leukemia (SBAO-2, VBAO-1). The experimental results are shown in Tables 7–9, in which the best-obtained results are remarked in boldface. The Friedman test [118] was used to examine the accuracy gained by SBAO, VBAO, and comparative algorithms. A comparison of binary AO and comparative algorithms was also performed in order to determine their convergence behavior.

Dataset Metric BBA BGSA **BGWO** BDA SBSCA VBSCA **SBAO** VBAO Mean acc. 0.7540.773 0.7660.669 0.773 0.773 0.773 0.773 Pima SD acc. 0.012 0.000 0.009 0.112 0.000 0.000 0.000 0.000 0.998 0.999 Mean acc. 1.000 0.865 1.000 1.000 1.000 1.000 Breast cancer SD acc. 0.003 0.000 0.001 0.103 0.000 0.000 0.000 0.000 0.852 0.877 0.871 0.697 0.896 0.892 0.899 0.896 Mean acc. Heart 0.017 0.009 0.025 0.237 0.009 0.007 0.009 0.012 SD acc. 0.797 0.834 0.830 0.797 0.871 0.869 Mean acc. 0.877 0.863 Lymphography 0.026 0.015 SD acc. 0.023 0.020 0.217 0.025 0.020 0.024 0.959 0.953 0.951 0.955 0.965 0.967 0.965 Mean acc. 0.967 Breast-WDBC 0.006 0.0040.006 0.067 0.002 0.003 0.002 SD acc. 0.004Mean acc. 0.766 0.7880.794 0.866 0.877 0.838 0.950 0.875 Colon SD acc. 0.034 0.042 0.042 0.041 0.042 0.021 0.0410.042 Mean acc. 0.831 0.864 0.888 0.971 0.971 0.914 0.993 0.942 Leukemia SD acc. 0.078 0.047 0.064 0.035 0.035 0.029 0.021 0.043 Friedman test-Average rank 7.50 5.00 6.14 6.29 2.21 3.93 1.79 3.14 5 7 2 **Overall** rank 8 6 4 1 3

Table 7. The accuracy comparison of SBAO and VBAO with other binary metaheuristic algorithms.

Table 8. The number of selected features comparison of SBAO and VBAO with comparative algorithms.

Dataset	Metric	BBA	BGSA	BGWO	BDA	SBSCA	VBSCA	SBAO	VBAO
D	Mean	3.00	5.00	5.10	5.00	5.00	5.00	5.00	5.00
Pima -	SD	1.53	0.00	0.31	0.00	0.00	0.00	0.00	0.00
D	Mean	3.27	3.20	4.27	3.00	3.00	3.00	3.00	3.00
Breast Cancer -	SD	1.41	0.41	1.08	0.00	0.00	0.00	0.00	0.00
	Mean	5.07	4.97	7.03	5.33	5.27	5.27	5.50	6.30
Heart -	SD	2.07	1.16	0.76	1.42	1.46	1.41	1.53	1.02
T 1 1	Mean	6.33	7.63	9.73	6.03	6.13	7.23	5.73	7.47
Lymphography -	SD	3.07	1.73	2.21	1.33	1.55	2.06	1.20	1.57
	Mean	11.10	12.77	11.93	4.27	4.20	9.33	4.53	9.80
Breast-WDBC -	SD	3.39	2.51	2.46	1.14	1.06	2.25	1.74	1.49
	Mean	687.00	973.03	1061.60	738.23	917.37	109.90	118.10	47.50
Colon -	SD	84.99	28.66	75.54	54.02	21.55	65.74	281.94	55.20
	Mean	2520.17	3537.93	4585.00	3032.17	3426.40	1579.40	1151.80	228.50
Leukemia -	SD	325.76	41.25	340.83	217.44	44.33	996.49	1300.27	161.25
Friedman test-Av	verage rank	4.00	5.79	7.86	3.79	3.86	3.57	3.21	3.93
Overall rank		6	7	8	3	4	2	1	5

Dataset	Metric	BBA	BGSA	BGWO	BDA	SBSCA	VBSCA	SBAO	VBAO
Pima	Mean fitness	0.249	0.231	0.237	0.330	0.231	0.231	0.231	0.231
	SD fitness	0.011	0.000	0.009	0.108	0.000	0.000	0.000	0.002
Breast Cancer	Mean fitness	0.005	0.003	0.005	0.135	0.003	0.003	0.003	0.003
	SD fitness	0.003	0.000	0.001	0.102	0.000	0.000	0.000	0.000
Heart	Mean fitness	0.149	0.125	0.132	0.302	0.106	0.110	0.105	0.107
	SD fitness	0.017	0.008	0.025	0.233	0.008	0.006	0.008	0.011
Lymphography	Mean fitness	0.204	0.168	0.173	0.219	0.125	0.139	0.130	0.133
, , , , , , , , , , , , , , , , , , , ,	SD fitness	0.022	0.020	0.026	0.256	0.024	0.019	0.023	0.014
Breast-WDBC	Mean fitness	0.050	0.044	0.050	0.045	0.033	0.037	0.033	0.037
	SD fitness	0.005	0.004	0.006	0.067	0.004	0.002	0.004	0.002
Colon	Mean fitness	0.233	0.213	0.208	0.135	0.125	0.160	0.050	0.124
	SD fitness	0.033	0.041	0.041	0.041	0.041	0.020	0.041	0.041
Leukemia	Mean fitness	0.170	0.139	0.117	0.032	0.033	0.087	0.008	0.056
	SD fitness	0.077	0.046	0.063	0.035	0.035	0.027	0.021	0.043

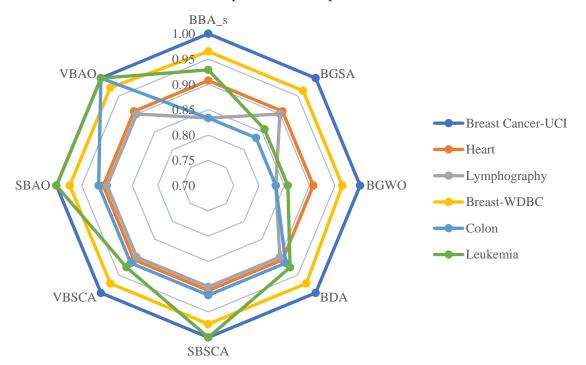
Table 9. The fitness comparison of SBAO and VBAO with other binary metaheuristic algorithms.

As demonstrated in Table 7, the gained results of SBAO, VBAO, and comparative algorithms on the basis of mean and standard deviation of the estimated accuracy for 30 separate runs on each of seven datasets are summarized. The BAO algorithm produces superior and competitive results on the datasets evaluated, as shown in Table 7. In the Pima and Breast cancer datasets, BAO produces the same results as BGSA, SBSCA, and VBSCA, while outperforming the rest of the algorithms on the Heart, Colon, and Leukemia datasets. According to the results, the proposed BAO algorithm was significantly more accurate than the comparative algorithms.

In Figure 2, the proposed BAO algorithm compares to the comparative algorithms in terms of the best-obtained classification accuracy in 30 runs. Additionally, the mean and standard deviation for the number of selected features are shown in Table 8. The plotted results show how the BAO can explore the search space for the most effective feature subset with the greatest classification accuracy. The suggested BAO beats the comparative algorithms when it comes to determining the effective subset with the fewest number of features, as shown in Table 8. It can be observed that SBAO and VBAO, like BDA, SBSCA, and VBSCA, performed best on the Breast cancer dataset, but SBAO and VBAO performed better on the Lymphography, Colon, and Leukemia datasets.

Figures 3 and 4 show a comparison between the proposed BAO and the comparative algorithms on four small datasets Breast cancer, Heart, Lymphography, and Breast-WDBC, and large datasets Colon and Leukemia. These figures show the number of selected features by considering the best-achieved accuracy. Table 9 shows the gained results of the SBAO and VBAO compared to comparative algorithms in terms of fitness value. BAO's ability to intensively explore promising regions of feature space and intensely exploit near solutions is the reason for this performance.

The average fitness convergence curves obtained by the suggested variations of BAO and comparative algorithms are shown in Figure 5. For the proposed BAO and comparative algorithms, the convergence curves are based on the optimal fitness function as well as mean convergence curves. The minimum fitness functions' convergence curves illustrate the highly qualified performance of the proposed BAO algorithm. The plotted curves



demonstrate that BAO can develop more effective solutions and strike a more favorable balance between exploration and exploitation.

Figure 2. Average accuracy gained by BAO and comparative algorithms.

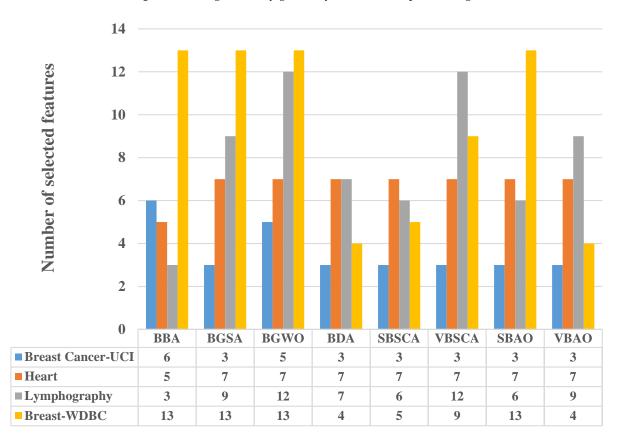


Figure 3. The Number of selected features comparison on small datasets.

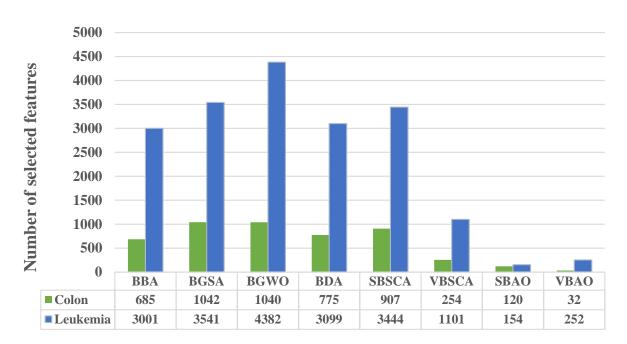
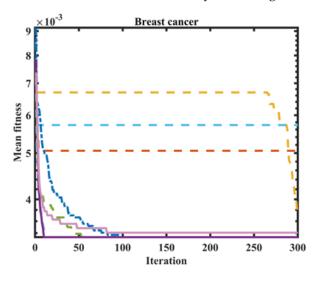
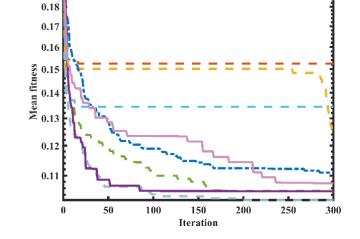


Figure 4. The Number of selected features comparison on large datasets.

0.19

Figure 5 shows with the exception of the Lymphography dataset, two variations of BAO discover superior fitness than other algorithms in all datasets. BGSA, unlike BAOs, shows a substantial decrease in fitness value in the early iterations, but the fitness value stayed constant for almost remained iterations, and eventually, it exhibits a significant loss in fitness value in the last iterations. While the BBA and BGWO algorithms demonstrate a steady convergence, the search process results in stagnation in non-optimal solutions. Finally, both SBSCA and VBSCA algorithms demonstrate a similar behavior to BAOs with a delayed convergence characteristic throughout the search phase.





Heart

Figure 5. Cont.

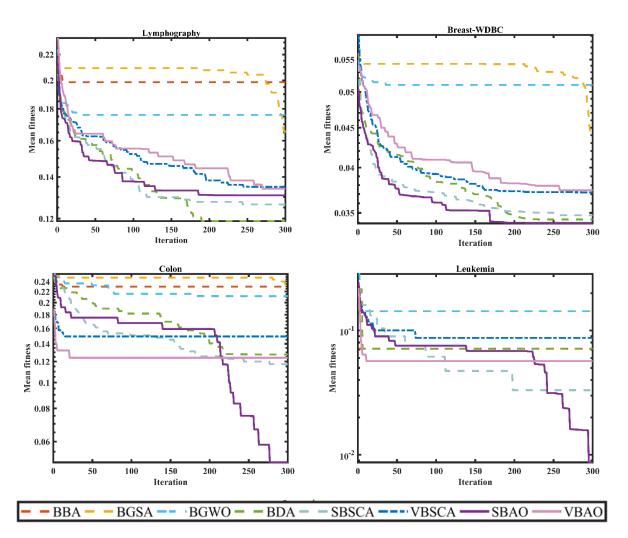


Figure 5. The convergence curves of BAO and comparative algorithms on all datasets.

7. Using BAO for COVID-19 Case Study

The suggested BAO is used to diagnose COVID-19 patient health in this section. The COVID-19 patient dataset was obtained from [121]. The dataset includes 864 instances and 15 features, as shown in Table 10. This experiment aims to anticipate the patients' mortality and recovery status based on the supplied criteria. In the main dataset, patients whose death or recovery status is missing are removed. The feature id was removed from the dataset, and all features were transformed to numeric form. In this case, we use k-fold cross-validation with K = 10 for the validation process. Figures 6 and 7 demonstrate the accuracy and selected feature size of the proposed BAO and comparative algorithms on the COVID-19 dataset. SBAO, which took into account seven features, had the greatest classification accuracy of 96.80%. On the other hand, the gained results reveal that VBAO only needed three features to diagnose the patient's health.

The BAO's major goal is to overcome the restriction of the canonical continuous AO algorithm in solving the feature selection issue, the use of its binary form resolves this. The algorithm provides fast convergence speed, strong global exploration capabilities, and high search efficiency during the search process, resulting in a better performance than other algorithms. Furthermore, the BAO's performance demonstrates its capability to search the feature space for effective features while maintaining balance exploration and exploitation over several iterations.

No.	Features	Description
1	Id	The patient's id
2	Location	The location where patient belongs to
3	Country	The country where patient belongs to
4	Gender	The patient's gender
5	Age	The patient's age
6	Sym-on	The date patient started noticing the symptoms
7	Hosp_vis	The date patient visited the hospital
8	Vis_wuhan	Whether the patient visited Wuhan, China
9	From_wuhan	Whether the patient from Wuhan, China
10	Symptom1	Symptom of patient (Fever)
11	Symptom2	Symptom of patient (Cough)
12	Symptom3	Symptom of patient (Cold)
13	Symptom4	Symptom of patient (Fatigue)
14	Symptom5	Symptom of patient (Body pain)
15	Symptom6	Symptom of patient (Malaise)
	Death	Whether the patient passed away due to COVID-19
	Recov	Whether the patient recovered

 Table 10. Description of COVID-19 dataset.



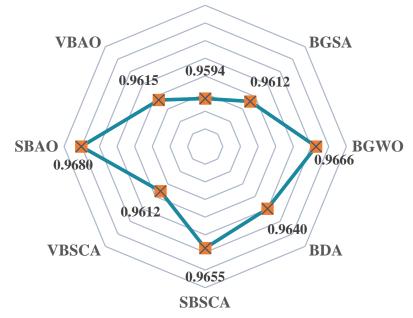


Figure 6. Accuracy gained by BAO and comparative algorithms.

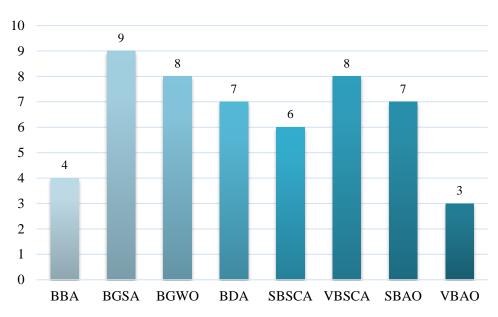


Figure 7. The number of selected features gained by BAO and comparative algorithms.

8. Conclusions and Future Works

In this article, two binary variations of the Aquila optimizer (AO) were introduced in this article and utilized to discover the wrapper approach's effective features. S-shaped and V-shaped transfer functions are utilized to alter the continuous version of AO into two binary algorithms, SBAO and VBAO. Then, the effective features from the medical datasets were selected for disease detection using the proposed algorithms. The gained results of the SBAO and VBAO were compared to six binary algorithms on seven medical datasets. The experimental findings demonstrate that the SBAO method can compete and/or achieve superior results on most datasets. In addition, the proposed algorithm was tested using the COVID-19 real-dataset. As a result of the findings, SBAO significantly outperforms other comparative algorithms and has shown to be more accurate than other comparative algorithms regarding predicting accuracy and minimizing the number of selected features. The BAO's performance over numerous iterations indicates its ability to find effective features while balancing exploration and exploitation. The algorithm provides speedy convergence, global exploration capabilities, and good search efficiency during the search process. In future research, the BAO variants can be applied to a variety of datasets and real-world situations by using various classifiers. Using the BAO to solve issues with many objectives might also be interesting.

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Appendix A

The appropriate values for the parameters α and δ used in the BAO are found using some pretests on the Leukemia dataset. Table A1. shows the comparison of mean accuracy and selected number of features by the different variants of SBAO and VBAO using values from set {0.1, 0.5, and 0.9}. The results indicate that the BAO can achieve better performance when $\alpha = 0.1$ and $\delta = 0.1$.

			$\alpha = 0.1$			$\alpha = 0.5$			$\alpha = 0.9$	
BAO Variants	Metric	$\delta = 0.1$	$\delta = 0.5$	$\delta = 0.9$	$\delta = 0.1$	$\delta = 0.5$	$\delta = 0.9$	$\delta = 0.1$	$\delta = 0.5$	$\delta = 0.9$
SBAO-1	Acc.	0.9714	0.9762	1.0000	1.0000	0.9762	1.0000	1.0000	0.9762	0.9762
3 D AO-1	#SF.	1316.70	486.00	2147.33	1581.67	1318.66	1375.00	2236.33	1513.00	1809.67
SBAO-2	Acc.	0.9929	0.9762	1.0000	1.0000	0.9524	1.0000	1.0000	1.0000	0.9762
50110 2	#SF.	1151.80	3049.00	2079.00	1955.33	1310.667	1717.00	1738.00	1284.67	1516.00
SBAO-3	Acc.	0.9786	0.9524	0.9762	1.0000	1.0000	0.9762	0.9762	1.0000	0.9762
50110 5	#SF.	1739.80	1043.00	2858.67	2845.67	2703.667	1948.00	3050.00	2092.67	1791.67
SBAO-4	Acc.	0.9571	0.9762	0.9762	1.0000	1.0000	1.0000	1.0000	0.9762	0.9524
obito 1	#SF.	2111.30	2804.00	2383.00	2412.67	3626	2306.67	3518.00	2143.67	2123.00
VBAO-1	Acc.	0.9429	0.9286	0.9524	0.9524	0.9524	0.9048	0.9286	0.9286	0.9286
v bito 1	#SF.	228.50	1292.00	265.33	1278.67	464.6667	501.33	163.00	1752.67	1497.67
VBAO-2	Acc.	0.9357	0.9524	0.9048	0.9286	0.9286	0.9286	0.9224	0.9286	0.9124
10110 2	#SF.	1151.90	745.67	1195.67	308.67	2570.667	741.33	347.33	2073.00	161.67
VBAO-3	Acc.	0.9286	0.9124	0.9286	0.9162	0.9286	0.9086	0.9048	0.9286	0.9286
v brie v	#SF.	1457.60	1975.33	1603.33	1471.00	1822.667	1854.33	2413.33	1490.00	1624.33
VBAO-4	Acc.	0.9357	0.9286	0.9286	0.9048	0.9286	0.9286	0.9286	0.9286	0.9286
. 2.10 1	#SF.	2651.80	2045.33	2003.33	1396.67	1563.333	2866.67	2818.33	1940.33	701.00

Table A1. The pretests' results for tuning the parameters α and δ .

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