



# Comprehensive Understanding of Hillocks and Ion Tracks in Ceramics Irradiated with Swift Heavy Ions

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**Abstract:** Amorphizable ceramics (LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub>) were irradiated with 200 MeV Au ions at an oblique incidence angle, and the as-irradiated samples were observed by transmission electron microscopy (TEM). Ion tracks in amorphizable ceramics are confirmed to be homogenous along the ion paths. Magnified TEM images show the formation of bell-shaped hillocks. The ion track diameter and hillock diameter are similar for all the amorphizable ceramics, while there is a tendency for the hillocks to be slightly bigger than the ion tracks. For SrTiO<sub>3</sub> (STO) and 0.5 wt% niobium-doped STO (Nb-STO), whose hillock formation has not been fully explored, 200 MeV Au ion irradiation and TEM observation were also performed. The ion track diameters in these materials are found to be markedly smaller than the hillock diameters. The ion tracks in these materials exhibit inhomogeneity, which is similar to that reported for non-amorphizable ceramics. On the other hand, the hillocks observed in non-amorphizable ceramics. No marked difference is recognized between the nanostructures in STO and those in Nb-STO. The material dependence of the nanostructure formation is explained in terms of the intricate recrystallization process.

Keywords: swift heavy ion; hillocks; ion tracks; ion irradiation; TEM

# 1. Introduction

Long nanometer-sized damage trails are created in ceramics continuously along the trajectories of swift heavy ions (SHIs), if the energy transfer from a SHI to an electron system of ceramics is sufficiently high [1–3]. Such characteristic damage is called an ion track. The mechanism of ion track formation has been extensively studied so far, and it has been one of the central topics in the research on ion-solid interactions. Ceramics can be categorized into two groups; amorphizable and non-amorphizable ceramics. If amorphous ion tracks are created, the ceramics are called amorphizable ceramics. The electronic stopping power dependence of ion track sizes in many amorphizable ceramics has been successfully predicted using the thermal spike model [4–8]. According to the model, the amorphous ion track formation is attributable to a local temperature rise sufficient to cause local melting along an ion path. On the other hand, there are non-amorphizable ceramics in which a crystal structure within an ion track region is not amorphized [9-14]. It has been found that in non-amorphizable ceramics, ion track size is markedly smaller than the size of the melt predicted by the thermal spike models [13,14]. Recent molecular dynamics (MD) simulation has revealed that the small ion tracks in non-amorphizable ceramics are attributable to fast recrystallization after transient melting [15–18]. It has been pointed out that the ionic nature of atomic bonding in non-amorphizable ceramics may be responsible for such fast recrystallization in non-amorphizable ceramics [9,19]. However, there is

currently no consensus on which material property makes the distinction between amorphizable and non-amorphizable ceramics. Therefore, it is important to examine the material dependence of ion track formation in terms of amorphization/recrystallization.

Ion track formation caused by SHIs is often accompanied by the formation of hillocks (so-called surface ion tracks) [20–35]. Our recent studies revealed that both ion tracks and hillocks are amorphous in the case of amorphizable ceramics ( $Y_3Fe_5O_{12}$  (YIG)) [36,37], whereas crystalline hillocks are found in the case of non-amorphizable ceramics (CaF<sub>2</sub>, SrF<sub>2</sub>, BaF<sub>2</sub>, and CeO<sub>2</sub>) [36,38]. Since the surface protrusion is a direct consequence of local melting along the ion path (melting of the ion track region), the observation of crystalline hillocks in non-amorphizable ceramics also provides a strong evidence of recrystallization after melting of the ion track region. It was also found that the hillock diameter always coincides with the diameter of a melt predicted by the thermal spike model for both amorphizable and non-amorphizable ceramics. This means that a hillock diameter value is affected by a melting process, but it remains unchanged after the subsequent recrystallization process. It is likely that a hillock size reflects melting, whereas an ion track size reflects both melting and subsequent recrystallization. Therefore, a comparative analysis of ion tracks and hillocks allows us to elucidate the whole processes of melting and amorphization/recrystallization. Moreover, there must be a variety of hillock and ion track morphologies due to an intricate recrystallization process, which can be the origin of the material dependence of nanostructure formation.

We recently proposed a method for precise measurement of a hillock size by transmission electron microscopy (TEM) [36–38]. The method is useful for the direct observation of a hillock side-view. It allows the accurate measurement of hillock dimensions and the identification of hillock crystal structure. In our previous study, we have studied hillocks and ion tracks in non-amorphizable ceramics such as CaF<sub>2</sub>, SrF<sub>2</sub>, and BaF<sub>2</sub>, whereas only one amorphizable ceramic (YIG) has been studied [36,37]. In the present study, we have further studied the relationship between the hillock diameter and ion track diameter for various types of ceramics. First, we show results of the TEM observations for SHI-irradiated amorphizable ceramics such as LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub> (GGG) and then for SrTiO<sub>3</sub> (STO) and 0.5 wt% niobium-doped STO (Nb-STO), whose hillock formation has not been fully explored. The electrical resistivity of STO increases by more than nine orders of magnitude by doping with 0.5 wt% Nb, whereas its crystal structure remains unaffected by the doping [39]. The effect of Nb doping on its hillock morphology is also investigated in this study. Based on the TEM investigations of both amorphizable and non-amorphizable ceramics, we discuss how the SHI-induced nanostructure formation depends on the intricate recrystallization process.

#### 2. Experiments

Thin samples for TEM observations were prepared before irradiation by the following procedure. The original materials were ZrSiO<sub>4</sub> (98%) powder (Kojundo Chemical Laboratory Co., Ltd., Saitama, Japan), LiNbO3 single crystals (Onizawa Fine Product Co., Ltd., Ibaraki, Japan), Gd3Ga5O12 (GGG) single crystals (Rare Metallic Co., Ltd., Tokyo, Japan), SrTiO<sub>3</sub> (STO) single crystals (Shinkosha Co., Ltd., Kanagawa, Japan), and 0.5 wt% niobium-doped STO (Nb-STO) single crystals (Shinkosha Co., Ltd., Kanagawa, Japan). The original materials were finely ground using an agate mortar and pestle. For the preparation of LiNbO<sub>3</sub> specimens, first, 3 mm diameter nickel grids with 2000 lines/inch were coated using 0.5% Neoprene W in toluene (Nisshin EM Co., Ltd., Tokyo, Japan), which works as an adhesive agent, and then the ground  $LiNbO_3$  powder was randomly dispersed on the grids. For the preparation of materials other than LiNbO<sub>3</sub>, the ground samples were dispersed in ethanol by an ultrasonic bath for a few minutes, and then the ethanol was dropped on 3 mm diameter 200 mesh copper grids covered with porous carbon films. The grids were then air-dried at room temperature. The samples on the grids were subsequently irradiated with 200 MeV Au<sup>32+</sup> ions at an oblique incidence angle (45° relative to normal direction) at room temperature in a tandem accelerator at JAEA-Tokai (Japan Atomic Energy Agency, Tokai Research and Development Center, Tokai, Japan). The charge state (32+) was chosen to ensure the charge of the incident ions to have the average value of the equilibrium charge. The samples

were irradiated with ions at  $1 \times 10^{11}$  ions/cm<sup>2</sup>. The as-irradiated samples were examined using a transmission electron microscope (TEM, Model 2100F, JEOL Ltd., Tokyo, Japan) operated at 200 kV. The ion track size was measured using the TEM images taken at a low magnification, wherein clear line-like contrasts were expected to be imaged. On the other hand, the hillock size was measured using the TEM images taken at a high magnification, wherein a clear contour of hillocks was expected to be obtained. The electronic stopping power (S<sub>e</sub>) was estimated using SRIM-2008 [40,41].

## 3. Results and Discussions

## 3.1. Dimensions of Hillocks and Ion Tracks in LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG

We have observed nanostructures created by SHI irradiation in amorphizable ceramics using TEM. Figure 1a–c show the bright field images of ion tracks in LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub> irradiated with 200 MeV Au at an oblique incidence angle. In the figures, the ion tracks are imaged as line-like contrasts. The diameter of the ion tracks can be estimated by measuring the width of the line-like contrasts. However, for most of the ion track images, it is difficult to distinguish the ion track contrasts from hillock contrasts. However, if the hillocks are created at the edge of the samples, it is possible to infer the hillock side-view. It can be concluded from the images that hillocks have similar diameters to those of ion tracks. Size distribution of ion tracks is shown in Figure 2. The average sizes of the hillocks and ion tracks are summarized in Table 1.



**Figure 1.** Bright field images of ion tracks induced in (**a**)  $\text{LiNbO}_3$ , (**b**)  $\text{ZrSiO}_4$ , and (**c**)  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle. The images were taken at relatively low magnification.



**Figure 2.** Size distribution of the track diameter, the hillock diameter, and the hillock height in (**a**) LiNbO<sub>3</sub>, (**b**) ZrSiO<sub>4</sub>, and (**c**)  $Gd_3Ga_5O_{12}$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle.

**Table 1.** Average diameter of ion tracks (D<sub>track</sub>), average diameter of hillocks (D<sub>hillock</sub>), average height of hillocks (H<sub>hillock</sub>) are listed with standard deviations for LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG irradiated with 200 MeV Au<sup>32+</sup>. The corresponding S<sub>e</sub> values are also listed.

	D <sub>track</sub> (nm)	D <sub>hillock</sub> (nm)	H <sub>hillock</sub> (nm)	Se (keV/nm)
LiNbO <sub>3</sub>	$11.7 \pm 1.3$	$13.2 \pm 1.5$	$5.8 \pm 1.2$	28.1
$ZrSiO_4$	$9.5 \pm 0.5$	$11.6 \pm 1.1$	$5.3 \pm 0.8$	29.6
GGG	$11.3\pm0.9$	$14.7\pm2.0$	$4.7\pm1.0$	34.2

Previous literatures have reported ion track sizes in LiNbO<sub>3</sub> [42–45], ZrSiO<sub>4</sub> [46,47], and GGG [45,48]. They have confirmed that the ion tracks in these ceramics are amorphous. A good summary of the ion track data in LiNbO<sub>3</sub> is given in Ref. [45], in which the dependence of ion track size on the electronic stopping power (S<sub>e</sub>) is shown. The S<sub>e</sub>-dependence demonstrates that an ion track size depends primarily on the electronic stopping power, whereas low ion velocity acts as a secondary factor that contributes to a bigger ion track owing to the velocity effect [49]. The literature also demonstrates that ion track sizes are in accordance with the values predicted by the thermal spike model. The present study shows that the ion track diameter in LiNbO<sub>3</sub> irradiated with 200 MeV Au (S<sub>e</sub> = 28.1 keV/nm) is  $11.7 \pm 1.3$  nm, whereas the previous study showed that the ion track diameter in LiNbO<sub>3</sub> irradiated with 201 MeV U

ions ( $S_e = 28.1 \text{ keV/nm}$ ) was around 13 nm [44,45], indicating that the present study is in accordance with the previous results within the experimental error.

Previous studies reported that the ion track diameter for  $ZrSiO_4$  irradiated with 10 GeV Pb ions (S<sub>e</sub> = 20.0 keV/nm) was 5.2 ± 0.2 nm [46] and that for  $ZrSiO_4$  irradiated with 2.9 GeV Pb ions (S<sub>e</sub> = 33.6 keV/nm) [47] was 8 nm. The present study shows that the ion track diameter for  $ZrSiO_4$  irradiated with 200 MeV Au ions is 9.5 ± 0.5 nm, exhibiting large ion tracks. Since the large ion tracks observed in the present study could be due to the relatively high electronic stopping power (S<sub>e</sub> = 29.6 keV/nm) and the velocity effect [49], there is no contradiction between the present and previous results.

A good summary of the previous ion track data in GGG is given in Ref. [45]. The present study shows that the ion track diameter for GGG irradiated with 200 MeV Au ( $S_e = 34.0 \text{ keV/nm}$ ) is  $11.3 \pm 0.9 \text{ nm}$ , whereas a previous study shows a similar ion track diameter ( $12.4 \pm 1.6 \text{ nm}$  for GGG irradiated with 250 MeV Pb ions ( $S_e = 34.0 \text{ keV/nm}$ )) [45]. Therefore, the present result is consistent with the previous results. The present results are also consistent with the prediction made by the thermal spike model.

Figure 3a–c show magnified images of hillocks in LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG, respectively, irradiated with 200 MeV Au at an oblique incidence angle. As shown in the figures, hillocks are successfully observed in those materials. It is also found that the hillocks are clearly amorphous, which confirms the amorphizable nature of these ceramics. The side-view of the hillocks allows measuring both hillock diameter and height. The distribution of the hillock sizes is shown in Figure 2 together with that of the ion track sizes. The average sizes of the hillocks and track sizes are summarized in Table 1. As demonstrated in the table, the hillock diameter is always similar to the ion track size, although the former tends to be slightly larger than the latter. A hillock height seems nearly half of the hillock diameter.



**Figure 3.** Bright field images of hillocks induced in (**a**) LiNbO<sub>3</sub>, (**b**) ZrSiO<sub>4</sub>, and (**c**)  $Gd_3Ga_5O_{12}$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle. The images were taken at relatively high magnification.

Although the hillock shape seems to be semi-spherical in the low magnification images, the magnified images demonstrate the formation of bell-shaped hillocks. Bell-shaped hillocks can also be found in  $Y_3Fe_5O_{12}$  [36,37] and  $Y_3Al_5O_{12}$  [16], that are also categorized as amorphizable ceramics.

### 3.2. Formation Process of Hillocks and Ion Tracks in LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG

The present study shows that both hillocks and ion tracks exhibit amorphous features, and they have similar sizes in amorphizable ceramics (LiNbO<sub>3</sub>,  $ZrSiO_4$ , and GGG). The present results agree with the prediction of the thermal spike model. According to the thermal spike model, SHIs cause transient melting along the ion path, when the electronic stopping power exceeds a certain threshold value. During such transient melting, thermal pressure and volume change caused by solid-liquid transition lead to surface protrusion of the melt. In the amorphizable ceramics, rapid cooling after melting results in the formation of amorphous ion tracks and hillocks.

It is important to note that, although the hillock diameter appears to be similar to the ion track diameter, the magnified TEM images shows that the former is always slightly larger than the latter. This can be ascribed to the spreading tendency of a liquid on a solid surface. It is likely that the hillock shape is determined by the balance of the adhesive (the liquid wanting to maintain contact with the solid) and cohesive forces within the liquid (both internal cohesive force and surface tension) during melting. If the adhesive force dominates, the protruded part of the melt can spread over the surface, leading to the formation of bell-shaped hillocks. Conversely, it can turn into a spherical shape, if the cohesive force dominates. Such spherical hillocks have been reported in some ceramics irradiated with high-energy fullerene ions having a very high  $S_e$  [50,51]. Large volume of surface protrusion induced by high  $S_e$  may be closely related to the formation of spherical hillocks.

#### 3.3. Hillocks and Ion Tracks in SrTiO<sub>3</sub> and Nb-Doped SrTiO<sub>3</sub>

Figures 4 and 5 show the bright field image of the ion tracks in STO and Nb-STO irradiated with 200 MeV Au at an oblique incidence angle, respectively. The ion track has a bright core surrounded by a dark fringe in the underfocus condition (Figures 4a and 5a), whereas it has a dark core surrounded by a bright fringe in the overfocus condition (Figures 4b and 5b). The Fresnel fringe is an indication of the formation of ion tracks with a lower density than that of the surrounding matrix [52,53]. Such focus-dependent Fresnel contrast is not found in amorphizable ceramics (e.g., YIG, LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG).



**Figure 4.** Bright field images of ion tracks induced in  $SrTiO_3$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle. The images were taken in (**a**) underfocus and (**b**) overfocus conditions.



**Figure 5.** Bright field images of ion tracks induced in Nb-doped  $SrTiO_3$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle. The images were taken in (**a**) underfocus condition and (**b**) overfocus condition.

The ion tracks in STO and Nb-STO have inhomogeneous morphology in contrast to the homogenous morphology of the ion tracks in amorphizable ceramics. The inhomogeneity of the ion tracks is a common feature observed in non-amorphizable ceramics such as CeO<sub>2</sub> [38], CaF<sub>2</sub>, SrF<sub>2</sub>, and BaF<sub>2</sub> [36], in which partial recrystallization after transient melting is the likely cause of the inhomogeneous ion track formation. Black contrasts corresponding to hillocks are found at the end of the ion tracks. Figures 6 and 7 show magnified images of a hillock created at the edge of the thin TEM samples of STO and Nb-STO, respectively. Bell-shaped hillocks are observed in STO and Nb-STO. In both materials, hillocks are found to be amorphous. It is interesting to find that amorphous hillocks are created, although the ion track region is recrystallized.



**Figure 6.** Bright field images of hillocks induced in  $SrTiO_3$  irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle.



**Figure 7.** Bright field images of hillocks induced in Nb-doped SrTiO<sub>3</sub> irradiated with 200 MeV Au<sup>32+</sup> at an oblique incidence angle.

Since it is difficult to find inhomogeneous ion tracks in TEM, we could not find sufficient numbers of ion tracks and hillocks to perform a statistical analysis. Therefore, in this study, we only show the size range of ion tracks and hillocks observed in STO and Nb-STO in Table 2. As demonstrated in the table, there is a marked difference in the diameters of ion tracks and hillocks in both STO and Nb-STO. The large hillock diameter compared with the ion track diameter is also found in typical non-amorphizable ceramics (CaF<sub>2</sub>, SrF<sub>2</sub>, and BaF<sub>2</sub>). The present result can be a strong evidence that supports the recrystallization of the ion track regions in STO and Nb-STO. Conversely, the amorphous hillocks are signs of the failure of recrystallization. It seems that STO and Nb-STO are intermediate ceramics between amorphizable and non-amorphizable ceramics.

**Table 2.** Approximate values of ion track diameter ( $D_{track}$ ), hillock diameter ( $D_{hillock}$ ), and hillock height ( $H_{hillock}$ ) in SrTiO<sub>3</sub> (STO) and 0.5 wt% niobium-doped STO (Nb-STO). The corresponding S<sub>e</sub> values are also listed.

	D <sub>track</sub> (nm)	D <sub>hillock</sub> (nm)	H <sub>hillock</sub> (nm)	Se (keV/nm)
STO	3~5	12~15	4~5	28.6
Nb-STO	3~4	11~13	4~5	28.5

Here, it is important to discuss whether the ion tracks are actually crystalline or not, since some of the previous studies claimed that they are amorphous in STO. According to Ref. [54], analysis of X-ray diffraction peaks in ion-irradiated STO supports creation of amorphous ion tracks due to single impacts. In the same literature, although crystalline tracks containing defects are observed by TEM, the authors claimed that the crystalline tracks are created owing to 200 keV electron beam exposure which can cause amorphous–crystalline transition of ion track areas. Conversely, our TEM results of STO and Nb-STO support creation of crystalline ion tracks rather than amorphous ion tracks. For example, an inhomogenous feature of ion tracks in STO and Nb-STO is similar to that observed in partially recrystallized ion tracks in non-amorphizable ceramics. Moreover, the markedly smaller ion track diameter than the hillock diameter demonstrates that the ion track region is partially recrystallized after transient melting.

The clear difference in the morphology between the hillocks in STO and Nb-STO was not observed in this study. Therefore, the influence of Nb-doping on the hillock formation is not found in this study. A previous study using TEM and small angle X-ray scattering (SAXS) reported that 1 wt% Nb-doping does not affect track formation [55]. Track formation is easy in insulators since the energy of hot electrons is transferred to the lattice in insulators before being cooled down by free electrons. In contrast, track formation is difficult in metals since high electronic conductivity allows rapid energy diffusion in an electron subsystem. Although the electrical conductivity of Nb-STO is more than nine orders of magnitude higher than that of STO, the electron density may still be too low to influence the formation of hillocks and ion tracks. It should be noted that the electrical conductivity of metals is still much higher than that of Nb-STO. The difference of bonding character (metallic bonding in metals vs. ionic/covalent bonding in STO) should be also contributing to the less sensitivity of track formation in metals [55].

#### 3.4. Factors That Determine the Recrystallization Process

The presence of recrystallization process separates non-amorphizable ceramics from amorphizable ceramics. Two factors that determine the recrystallization process have been proposed; (1) simplicity of lattice structure and (2) the strength of ionic bonding. The previous literature [15] proposed that a simple lattice structure with the smallest number of the peaks in the pair correlation function is in correlation with the recrystallization efficiency. Actually, amorphous ion tracks and hillocks are observed in YIG and GGG that have complicated crystal structure, whereas crystalline ion tracks and hillocks are observed in rather simple structured compounds (CaF<sub>2</sub>, SrF<sub>2</sub>, BaF<sub>2</sub>, and CeO<sub>2</sub> with fluorite structure). STO has a relatively simple cubic structure with space group of Pm3m, where there are only 5 atoms in the unit cell. The relatively simple crystal structure of STO can be the origin of the recrystallization of the ion track region. However, creation of amorphous hillocks in STO demonstrates that STO and Nb-STO are intermediate ceramics between amorphizable and non-amorphizable ceramics. Here, it is worth noting that STO has a perovskite structure which is composed of TiO<sub>2</sub> planes and SrO planes, which make the structure somehow complicated. This unique structure of STO seems to be responsible for the intermediate behavior of ion-induced nanostructure formation. Therefore, we believe that the correlation of recrystallization effectiveness with the simplicity of the crystal structure is one of the promising hypotheses, and its validity should be further examined.

Another possible factor is the strength of ionic bonding, i.e., materials with a higher degree of ionicity recrystallize easily [19,56]. Non-amorphizable ceramics include many ionic crystals. It is conceivable that long-range ionic forces rather than short-range covalent interaction contribute to rapid recrystallization [19,57]. STO has mixed ionic-covalent bonding properties. While a hybridization of the O-2p states with the Ti-3d states within the TiO<sub>6</sub> octahedra leads to a pronounced covalent bonding, Sr<sup>2+</sup> and O<sup>2-</sup> ions exhibit an ionic bonding character. Although STO is one of the complex oxides, the ionic bonding character in STO may be also responsible for the partial recrystallization of ion tracks. Therefore, the two factors mentioned above is important to explain why STO and Nb-STO are intermediate ceramics between amorphizable and non-amorphizable ceramics.

It is worth discussing why the hillock region fail to recrystallize, whereas the ion track region recrystallizes in STO. The previous MD simulation demonstrated that oxygen atoms settle in their original sites faster than metal atoms in SHI-irradiated MgO and Al<sub>2</sub>O<sub>3</sub>, and metallic atoms then adjust to a layer of oxygen that has already been built [15]. The study concluded that that the ability of oxygen atoms to reach their equilibrium sites governs the recrystallization process after melting. It is conceivable that in STO, oxygen loss in the hillock region effectively hinders recovery of the lattice structure. The hillock region tends to be more oxygen deficient than the ion track region, since oxygen atoms tend to escape from the irradiated surface. An important role of oxygen deficiencies should be further investigated in the future.

#### 3.5. Summary of Formation Processes of Hillocks and Ion Tracks

To understand the difference between nanostructure formation in amorphizable and non-amorphizable ceramics, it is important to describe the process in terms of melting and successive recrystallization.

It is convenient to start the discussion with CeO<sub>2</sub>, which is one of the non-amorphizable ceramics. According to Ref. [38], hillocks are found to be spherical in CeO<sub>2</sub> irradiated with 200 MeV Au. It was found that hillocks (spherical objects) have crystalline features, where the lattice orientation of hillocks was aligned with that of the matrix. This points out to the process consisting of the following three steps as explained in Figure 8a. (1) A molten region is created along the ion path. A part of the molten region protrudes above the surface because of the thermal pressure and additional pressure due to volume change caused by solid-liquid transition. (2) During cooling, the molten region embedded in the matrix begins to recrystallize. The partial recrystallization results in ion tracks smaller than those expected from the size of the melt. The shape change (spheroidization) of the protruded part strongly suggests that the protruded part remains liquid for a long period of time which is long enough for the molten protrusion to change its shape. The protruded part of the molten region can spheroidize if the surface tension is strong enough. (3) A droplet at the surface starts to recrystallize epitaxially using the matrix as a template lattice, so that a crystalline nanosphere having the same crystal orientation as that of the matrix is formed. This result strongly suggests that the molten region embedded in the matrix is solidified before the protruded part of the melt is solidified. It is reasonable to assume that this sequence of the solidification process applies to all SHI-irradiated ceramics. Such a sequence of solidification process is supported by the MD simulation of the nanostructure formation in  $CaF_2$  [16].



**Figure 8.** Schematic formation processes of ion tracks and hillocks in (**a**) CeO<sub>2</sub>, (**b**) fluorides (CaF<sub>2</sub>, SrF<sub>2</sub>, and BaF<sub>2</sub>), (**c**) STO and Nb-STO, and (**d**) amorphizable ceramics (YIG, LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG).

The likely process of nanostructure formation in fluorides (CaF<sub>2</sub>, SrF<sub>2</sub>, and BaF<sub>2</sub>) irradiated with 200 MeV Au is presented in Figure 8b. According to our previous study [36], most of the crystalline hillocks in these fluorides are nearly semispherical, although some of the hillocks have nearly spherical shape. Since recrystallization plays an important role in both fluorides and CeO<sub>2</sub>, the formation process in the fluorides should be similar to that of CeO<sub>2</sub> (Figure 8a). The difference between the spherical shape of hillocks and non-spherical shape can be explained by the difference in volume of protrusion.

If the volume of protrusion is large, the hillock shape tentatively has an unstable shape because of its high aspect ratio of height to width. It is conceivable that the unstable shape can rapidly turn into a stable spherical shape. Similar spherical hillocks have been already reported in some ceramics (Gd<sub>2</sub>Zr<sub>2</sub>O<sub>7</sub> [50] and YIG [51]) irradiated with high-energy fullerene ions with very high S<sub>e</sub>, supporting the proposition that larger volume of the protrusion is the key to the formation of spherical hillocks.

The likely process of nanostructure formation in STO and Nb-STO is presented in Figure 8c. Although the first and second steps of the process in the figure are the same as those in Figure 8b, the third step of the process is different. Even though the molten region embedded in the matrix recrystallizes partially, the protruded part of the melt failed to recrystallize, resulting in amorphization. The failure of recrystallization only in the hillock region can be ascribed to oxygen deficiencies as discussed above.

The likely process in amorphizable ceramics (YIG, LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and GGG) is presented in Figure 8d. The process consists of the following three steps. (1) A molten region is created along the ion path. A part of the molten region protrudes above the surface. (2) During cooling, the molten region embedded in the matrix starts to solidify, resulting in the amorphization of the molten region. Herein, the size of the molten region corresponds to that of the ion tracks. (3) The protruded part of the melt also starts to amorphize. This means that the hillock diameter is always similar to the ion track diameter. A subtle change of hillock shape leading to a slightly larger hillock diameter than the ion track diameter is not specified in the schematic, since this effect produces only a small difference between the hillock diameter and ion track diameter.

# 4. Conclusions

Amorphizable ceramics such as LiNbO<sub>3</sub>, ZrSiO<sub>4</sub>, and Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub> were irradiated with 200 MeV Au ions at an oblique incidence angle. Line-like homogeneous ion tracks and bell-shaped hillocks are observed by TEM. The ion track and hillock diameters are similar for all the amorphizable ceramics, although the hillock diameter is found to be slightly larger than the ion track diameter. The TEM images of ion tracks in STO and Nb-STO irradiated with 200 MeV Au show similar features to those observed in the non-amorphizable ceramics. For example, the ion track diameter is markedly smaller than the hillock diameter, and they exhibit inhomogeneity. However, the hillocks in these ceramics are found to be amorphous which is in contrast to the crystalline feature of hillocks observed in the non-amorphizable ceramics. Therefore, it can be concluded that STO and Nb-STO are intermediate ceramics between amorphizable and non-amorphizable ceramics. No marked difference is observed between hillock formation in STO and that in Nb-STO. The material dependence of nanostructure formation can be ascribed to the intricate recrystallization process. The present results support that (1) simplicity of lattice structure and (2) the strength of ionic bonding can be the factors that determine the recrystallization effectiveness.

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