

Article

Finite Element Method for the Estimation of Insertion Loss of Noise Barriers: Comparison with Various Formulae (2D)

Nikolaos M. Papadakis ^{1,2,*} and Georgios E. Stavroulakis ¹

- ¹ Institute of Computational Mechanics and Optimization (Co.Mec.O), School of Production Engineering and Management, Technical University of Crete, 73100 Chania, Greece; gestavr@dpem.tuc.gr
- ² Department of Music Technology and Acoustics, Hellenic Mediterranean University, 74100 Rethymno, Greece
- * Correspondence: nikpapadakis@isc.tuc.gr

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Abstract: Noise barriers are a critical part of noise mitigation in urban and rural areas. In this study, a comparison of the insertion loss calculations of noise barriers via the Finite Element Method (FEM) and various formulae (Kurze-Anderson, ISO 9613-2/Tatge, Menounou) is presented in the case of two-dimensional acoustic radiation problems. Some of the cases explored include: receiver in the illuminated zone, in the shadow zone, in the shadow border, source in medium, long, short distance from the barrier, source and receiver near barrier, and source above the barrier. Comparisons of the results indicate that FEM results comply well (less than 1 dB in each case) with Menounou's formula which in turn complies with the analytic solution (MacDonald Solution). In certain cases, the differences between FEM and Menounou's formula compared to Kurze-Anderson and ISO 9613-2/Tatge formulae are substantial (source and receiver near the barrier (10 dB) and source near the barrier and receiver in the shadow border (5 dB)). Similar differences are also confirmed by the analytic solution. The findings suggest that FEM can be applied effectively for the precise estimation of the insertion loss of noise barriers. Especially in cases where ISO 9613-2 formula shows large deviations from the analytic solution (e.g., near barrier), possible applications may arise in cases such as balconies, facades, etc. Furthermore, the study supports the idea that FEM could possibly be effectively utilized in real life applications for microscale urban acoustic modeling as a viable alternative to expensive noise prediction software.

Keywords: noise barriers; insertion loss; finite element method; microscale urban acoustic modeling; sound screen; ISO 9613-2; perfectly matched layer; environmental acoustics; noise pollution; soundscape design

1. Introduction

A noise barrier can be considered as any solid obstacle that impedes the line of sight between the source and receiver and thus creates a sound shadow [1]. Noise barriers are an important aspect of fighting noise pollution both in urban and rural areas caused by major infrastructure projects such as roads, railways, and airports. In the context of improving the urban environment and in order to meet recommended guideline values for community noise (e.g., World Health Organization (WHO) [2]), implementing noise barriers is one of the most used and effective methods.

Noise barriers come in many forms and shapes. The use of numerical methods is of great importance in their development as well as in the evaluation of their effectiveness. We can mention barriers with diffracting edge modifications such as T-shaped barriers [3], multiple-edge barriers [4],



Y-shaped [5], with tubular cappings [6], with fir-tree profile [7], with passive phase interference devices [8], and with absorptive treatment [9,10]. Other forms include earth mounds [11], cantilevered and galleried barriers [12], picket [13] and louvered barriers [14], sloped [15] and dispersive barriers [16], barriers with vegetation [17], biobarriers [17], sonic crystals [18], barriers that fight air pollution [17], exploit solar energy [17], with active noise control [19], and barriers that are used for energy harvesting [20]. Noise barriers can be made with a range of materials including timber, sheet-metal, concrete, brick, plastic, PVC, and fiberglass [17]. The optimization of barriers has also been applied through scaled experiments [21], genetic algorithms [22], topology optimization [23,24], and artificial neural networks [25]. For a more detailed description, the reader can refer to [1,17,26]. Also, it must be noted that noise barriers are also used indoors e.g., in open plan offices (usually named as screen barriers or acoustic screens) [27–29].

The main phenomenon characterizing the acoustic behavior of a noise barrier is diffraction, while absorption and transmission are also important. The performance of a noise barrier is measured by insertion loss which is defined in ISO 9613-2 [30] as: 'difference, in decibels, between the sound pressure levels at a receiver in a specified position under two conditions: (a) with the barrier removed, and (b) with the barrier present (inserted), and no other significant changes that affect the propagation of sound'. However, it must be noted that the effectiveness of a noise barrier regarding its perceived loudness attenuation is also affected by its visual characteristics [31,32].

1.1. Mathematical Formulation, Exact Solutions and Approximate Analytical Solutions

The first mathematically formulation for the diffraction of a plane wave by a semi-infinite plane screen was given by Sommerfeld [33]. Thereafter, MacDonald [34] developed a solution in a spherical polar coordinate system that was subsequently recast in the cylindrical polar system by Bowman and Senior [35]. An accurate integral representation of the diffracted wave from a semi-infinite wedge has been given by Hadden and Pierce [36].

Many approximate analytical solutions for diffraction by a half plane can be found such as the Fresnel–Kirchhoff approximation [37] and in studies by Rubinowicz [38] and Embleton [39], with the former being the most common one. The Fresnel–Kirchhoff approximation is a mathematical representation of the Huygens–Fresnel principle which is in wide use in optics. In this approximation the Helmholtz equation is solved with the aid of Greens theorem. The sound pressure at a receiver can be written as an integral to be evaluated over a surface of infinite extent. An extensive overview of all the above can be found in the study by Li and Wong [40].

1.2. Formulae of Insertion Loss

Simple formulae and charts [37–41] are proposed for the calculation of insertion loss of semi-infinite noise barriers, since exact and approximate solutions are not easily applicable for engineering purposes and software implementations due to their mathematical complexity.

The first known attempt was developed by Redfearn [41], while Maekawa [42] presented the most influential work. Maekawa, in his study, used pulsed tones of short duration to measure the attenuation of a thin, rigid barrier, for different source and receiver positions. The results were presented in a chart where the attenuation was plotted against a single parameter known as the Fresnel number (numerical ratio of the path difference between the diffracted path and the direct path of sound to the half of a sound wavelength). In the same period, Rathe [43] also presented an empirical table for sound attenuation by a thin, rigid barrier due to a point source.

A well-known formula for calculation of insertion loss is that of Kurze and Anderson [44,45] which is referred in most relevant textbooks [1,17]. In their work, Kurze and Anderson reviewed diffraction theory from Keller [29] and used Maekawa's and Redfearn's experimental data to derive a simple formula for barrier attenuation.

Another simple formula that fits the Maekawa data quite well is that of Tatge [46] which can also be found in ISO 9613-2 [30] (case for single diffraction, no ground reflections). The importance of this equation lies in the fact that various sound mapping software comply with ISO 9613-2 requirements.

More recently, Menounou [47] presented a new, optimized formula as a correction to the Kurze–Anderson formula. In her study, a comparison of the results between Maekawa's curve and the MacDonald solution [33] was presented, especially for configurations where both source and receiver were close to the barrier and where the receiver was at the shadow border (the line where the barrier nearly breaks the line of sight between the source and the receiver). Discrepancies, 15 dB and 3 dB, respectively, were observed. Similar experimental results, in agreement with the MacDonald solution but with a great deviation from Maekawa's curve, were reported by Kawai et al. [48] in the case when either the source or the receiver is comparatively near the barrier. The same conclusion was also reported by Hu and Wong [49]. The goal of Menounou's work was to bridge the Maekawa's curve and the Kurze–Anderson formula with the exact solutions by providing a simple and accurate formula with results similar to the analytical solution.

1.3. FEM, Other Numerical Methods and Noise Barriers

Numerical methods such as Finite Element Method (FEM), Boundary Element Method (BEM), Finite Difference Time Domain (FDTD) method, and Pseudo Spectral Time Domain (PSTD) method have also been applied for noise barriers. FEM has been used for studies for the estimation of the reflection index of multiple acoustic layered noise barriers [50], for modeling of the acoustic performance of sonic crystals [51–53], for topology optimization [24,54,55], for the investigation of the structural performance of a noise barrier [56], and for calculation of insertion loss [57]. However, it seems that more numerical studies have used BEM, for modeling of noise barriers with various shapes and configurations [58–65] and for barrier optimization [66–69]. The FDTD and PSTD methods have been applied for studies to a much lesser extent, [70–73] and [74,75] respectively.

FEM is probably one of the most (or the most) widely used numerical method with many software implementations and has been applied for modeling of wave phenomena in acoustics for various applications (e.g., room acoustics [76]). It can simultaneously incorporate the effects of diffraction, absorption, and transmission both in the frequency and time domains [77]. However, despite its widespread use, fewer studies have utilized FEM for studying noise barriers compared to BEM even though both methods allow any kind of shape and impedance condition values on the surfaces of the barrier. Probably, this is due to the fact that BEM appears more appropriate in an infinite space than FEM, because only the surface of the domain boundary must be discretized. However, studies show that the computational cost of the methods in exterior problems can be competitive [78] and for the same domain FEM computational cost can be lower than BEM [79]. This study supports the notion that FEM is suitable for noise barrier research and probably for urban acoustic modeling as it will be discussed in Section 4 of this paper.

1.4. Aims and Novelties

The aims of this study are to:

- Validate of the accuracy of FEM for calculation of insertion loss of noise barriers.
- Present a simple and applicable methodology for the accurate calculation of insertion loss utilizing commercial software which can be extended to various cases (e.g., predict the behavior of noise barriers with various shapes, with a profile which absorbs or disperses sound, in 3D space, etc.).
- Lay the groundwork for application of FEM for urban acoustic microscale modeling.

The novelties of this study, in relation to earlier publications, can be considered to consist of the following points:

 To the best of our knowledge this is the first study that extensively compares insertion loss results of FEM with Kurze–Anderson, ISO 9316-2/Tatge and Menounou formulae results. • This is the first study to present the accuracy of FEM for the calculation of insertion loss of noise barriers especially in the cases where the receiver is near the barrier or in the shadow border and when both source and receiver are near the barrier.

This paper is organized as follows. Section 2 presents the methodology employed for FEM, relevant information regarding insertion loss, and the various formulae used in the study. Section 3 presents the findings of the research, while the Section 4 analyses the data, addresses the research questions, and identifies areas for further research. Finally, Section 5 gives a brief summary and contextualizes the study.

2. Methods

The section begins with an introduction to the subject of insertion loss, containing all the relevant information necessary for the next chapters. Thereafter, the FEM setup and methodology applied for the calculation of insertion loss is presented as well as the formulae that were used in this study.

2.1. Elements Regarding Insertion Loss

Elements that are going to be presented regarding insertion loss and noise barriers are: definitions, basic terminology, coordinate system, and equations that were used throughout the text.

As stated in the introduction, insertion loss is defined as: 'difference, in decibels, between the sound pressure levels at a receiver in a specified position under two conditions: (a) with the barrier removed, and (b) with the barrier present (inserted), and no other significant changes that affect the propagation of sound' [30]. Therefore, insertion loss can be expressed as Equation (1):

$$IL = L_b - L_a = 10 \log \left[\frac{p_b^2}{p_a^2}\right] \tag{1}$$

where L_b , p_b and L_a , p_a are the sound pressure levels and the acoustic pressures measured at the same location before and after the insertion of a noise barrier.

Areas around the noise barrier can be divided into zones (Figure 1). The shadow zone is the area where the barrier breaks the line of sight between source and receiver, while in the illuminated zone there is a direct line of sight between source and receiver. The shadow border is the line between the shadow zone and the illuminated zone. For a thorough mathematic description of the different regions the reader can refer to [40,80].

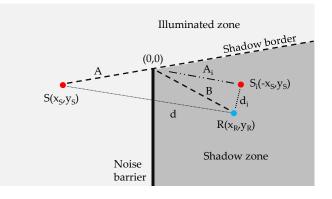


Figure 1. Elements regarding noise barriers and insertion loss. Axes are in meters (m).

The theory developed for noise barriers [42] calculates the acoustic performance in terms of the Fresnel number N_1 , which is defined as:

$$N_1 = 2\frac{\delta}{\lambda} \tag{2}$$

where λ is the wavelength of sound in air and δ is the path length difference (diffracted path length minus direct path length), which can be defined as:

$$\delta = (A+B) - d \tag{3}$$

(A + B) is the shortest path over the edge, from the source to the receiver in the barrier shadow zone, *d* is the direct path distance between source and receiver, through the barrier. The path length difference is positive in the shadow zone of the barrier and negative in the illuminated zone.

A rectangular coordinate system with its origin at the intersection of the diffracted ray and the top edge is going to be used throughout the text, which is particularly convenient for the software implementations (for FEM and formulae). The rectangular coordinate system can also be used in 3D [44]. Subscripts *S* and *R* identify the coordinates of the source (x_S , y_S) and receiver (x_R , y_R) positions respectively. Therefore, *d*, *A* and *B* can be defined as:

$$d = \sqrt{(x_S - x_R)^2 + (y_S - y_R)^2}$$
(4)

$$A = \sqrt{\left(x_S^2 + y_S^2\right)} \tag{5}$$

$$B = \sqrt{\left(x_R^2 + y_R^2\right)} \tag{6}$$

The parameter N_2 , introduced by Menounou [47], can be thought of as a second Fresnel number that is associated with the relative position of the image source to the barrier and the receiver. It is defined as the extra distance sound travels from the image source to the receiver after diffraction by the barrier edge, normalized by half the wavelength of the incident wave [47].

$$N_2 = 2\frac{(A_i + B) - d_i}{\lambda} \tag{7}$$

2.2. Formulae for the Calculation of Insertion Loss

The formulae that were used for the calculation of insertion loss are Kurze–Anderson, ISO 9613-2/Tatge and Menounou. The software Matlab v. R2015a (Mathworks, Natick, MA, USA) was used for the calculations.

2.2.1. Kurze-Anderson Formula

As stated in the introduction, probably the most well-known formula for calculation of insertion loss, which is in good agreement with Maekawa's curve [42], is that of Kurze and Anderson [44,45]. If we assume that the sound is emitted by a point source and the barrier can be considered to be thin and infinitely long, then the insertion loss can be calculated by the following equation:

$$IL = 20 \log \frac{\sqrt{2\pi N_1}}{\tanh(\sqrt{2\pi N_1})} + 5 dB$$
(8)

In their study, Kurze and Anderson [44] found that the formula is in good agreement with Maekawa's curve for $N_1 > -0.2$. The formula is also in good agreement with Rathe's experimental results for $0.1 < N_1 < 12.5$. However for $N_1 > 12.5$, Rathe's data show that there is an upper limit of 24 dB [43].

2.2.2. ISO 9613-2/Tatge Formulae

Tatge, in his study [46], presented a formulae that fits well with the Maekawa curve [42]. The formula is applied for $N_1 \ge 0$. The same formula can be found in ISO 9613-2 [30] (case for single diffraction, no ground reflections). However, in the ISO it is stated that: 'For large distances

and high barriers, the insertion loss calculated (by the formula) is not sufficiently confirmed by the measurements'. The importance of this equation lies in the fact that various sound mapping software comply with ISO 9613-2 requirements. The ISO 9613-2/Tatge formula is expressed as:

$$IL = 10\log(3 + 20N_1) \tag{9}$$

2.2.3. Menounou Formula

Menounou, in her work [47], presented the following formula (Equation (10)) as an improvement to the Kurze–Anderson formula. As discussed in the introduction, Maekawa's curve and Kurze–Anderson formula give predictions that deviate largely from experimental data and analytical solutions when the source or receiver is very close to the barrier surface, or when the receiver is very close to or at the shadow border.

The first term of Menounou's formula (nomenclature of the study will be used), ILs, is a function of N_1 , which is a measure of the relative position of the receiver to the source. The second term is a function of N_2/N_1 , which is a measure of the proximity of either the source or the receiver to the barrier surface. The third term is appreciable and needs to be computed only when N_1 is very small, which in turn is a measure of the proximity of the receiver to the shadow border. Finally, the fourth term, ILsp, is a term that depends on the type of incident radiation and is a function of the ratio (A + B)/d. The Menunu formula is:

$$IL = IL_s + IL_b + IL_{sb} + IL_{sp}$$
(10)

where:

$$IL_{s} = 20 \log \frac{\sqrt{2\pi N_{1}}}{\tanh\left(\sqrt{2\pi N_{1}}\right)} - 1 \tag{11}$$

$$IL_{b} = 20 \log \left[1 + \tanh \left(0.6 \log \frac{N_2}{N_1} \right) \right]$$
(12)

$$IL_{sb} = \left(6 \tanh \sqrt{N_2} - 2 - IL_b\right) \left(1 - \tanh \sqrt{10N_1}\right)$$
(13)

$$\mathrm{IL}_{\mathrm{sp}} = -10\log\frac{1}{\left(\frac{A+B}{d}\right)+1} \tag{14}$$

2.3. FEM Setup and Methodology for the Calculation of Insertion Loss

Elements that are going to be presented regarding FEM setup and methodology for the calculation of insertion loss are: models created, mesh creation, and the modeling of the open pressure acoustic domain through a Perfectly Matched Layer (PML), FEM formulation.

2.3.1. FEM Models

Two models were created: for the first one the sound pressure at the receiver point was calculated without the presence of a sound barrier and for the second one with a sound barrier for the same source position. The insertion loss was calculated as the difference in sound level at receiver location with and without the presence of a noise barrier. The point source and receiver positions in relation to the sound barrier are presented in Figure 1.

For the mesh creation the rule of thumb $\lambda/h = 5$ was applied where λ and h respectively denote wavelength of upper limit frequency and the maximum nodal distance. Five elements per wavelength are typical [81] for acoustic modeling in the frequency domain, while different considerations apply for modeling in the time domain [82]. The domain was discretized with an unstructured mesh of quadratic Lagrange triangular elements. The Delaunay triangulation [83] was used in this study for automatic mesh generation. The highest frequency considered in this study was 500 Hz. The maximum element

sized used was approximately 0.1 m while the minimum element size was 0.004 m. The number of total elements used was 926,958.

For modeling the open pressure acoustic domain (Sommerfeld radiation condition [84]) an appropriate Absorbing Boundary Condition (ABC) had to be applied. The Perfectly Matched Layer (PML) was used which is considered to be one of the best ABC available (for a review of ABC's the reader can refer to [85,86]). The PML is an approximation methodology originally developed by Berenger [87] and later applied in the field of acoustics [88]. The key property of a PML, that distinguishes it from an ordinary absorbing material, is that it is designed so that waves incident upon the PML from a non-PML medium are absorbed without any (or better minimum) reflections at any frequency and at any incidence angle.

However, it must be noted that the performance of a PML is not perfect. Berenger, in his study, [87] stated that 'small amount of numerical reflection occurs in practical computations, but with a magnitude that can be reduced by tuning some parameters of the layer, especially its thickness'. In his research, Zampolli et al. [89] (utilizing the same software as this research), used PMLs with different layers of quadratic elements (3, 6, and 12 layers). It was found that PMLs suffer from inaccuracies at very low frequencies in the case a small number of layers used. For this study, the thickness of the PML was chosen so that it consists of a larger number of layers than the maximum studied by Zampolli so that there are no (or minimum) reflections. As can be seen in, e.g., Figures 2–4, a 10 m thickness was used for the PML, which with a maximum element size of 0.1 m and an unstructured mesh, resulted in a number of layers approximately between 140 and 165.

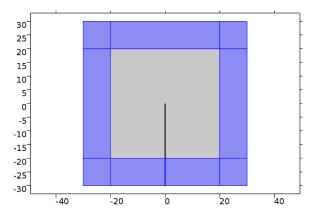
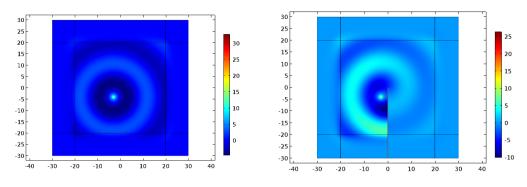


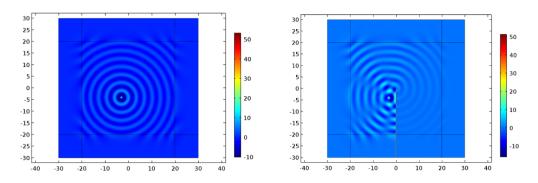
Figure 2. Finite Element Method (FEM) model with sound barrier and Perfectly Matched Layer (Violet color). Axes are in meters (m).

The FEM model with the PML is presented in Figure 2. The specific geometry of the PML area was chosen as it has been used in other studies [87,88] and successfully in the past by the authors [90], while other geometries can probably be used (e.g., circular). The same type of element was used in the whole domain (however hybrid meshes have been used for the same purpose-triangular elements for the main domain and rectangles for the PML [91]).

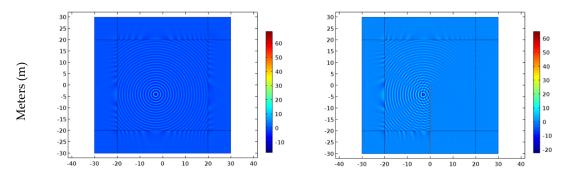
In this study the commercial software Comsol Multiphysics v.5.1. (Comsol inc., Burlington, VT, USA) was utilized for the 2D sound field models.



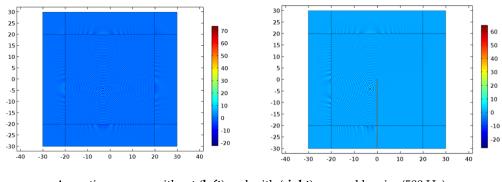
Acoustic pressure without (left) and with (right) a sound barrier (20 Hz)



Acoustic pressure without (left) and with (right) a sound barrier (100 Hz)



Acoustic pressure without (left) and with (right) a sound barrier (300 Hz)



Acoustic pressure without (**left**) and with (**right**) a sound barrier (500 Hz) Meters (m)

Figure 3. Acoustic pressures of the domain calculated via FEM for different frequencies. Colorbar units are in Pascal (Pa). Axis units are in meters (m).

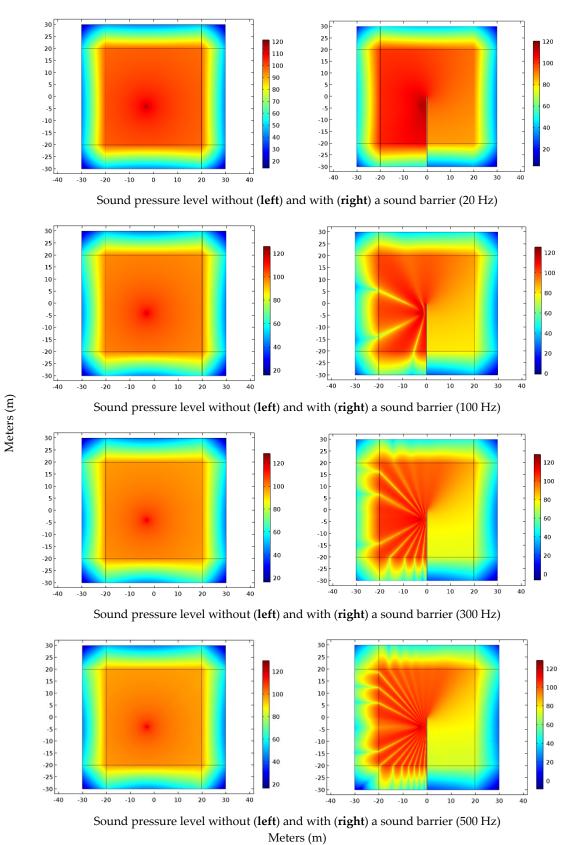


Figure 4. Sound pressure levels of the domain calculated via FEM for different frequencies. Colorbar

units are in SPL (dB). Axis units are in meters (m).

2.3.2. FEM Formulation

For the Helmholtz equation, *p* is the acoustic pressure, Δ is the Laplacian operator, *k* is the wave number and is given by:

$$\Delta p(\mathbf{x}) + k^2 p(\mathbf{x}) = 0 \tag{15}$$

The normal fluid particle velocity u_f is related to the normal derivative of the acoustic pressure p in the frequency domain by:

$$u_f(\mathbf{x}) = \frac{1}{i\omega\rho_f} \frac{\partial p(\mathbf{x})}{\partial n(\mathbf{x})}$$
(16)

where $n(\mathbf{x})$ represents an outward normal vector at a field point \mathbf{x} , $\frac{\partial}{\partial n}$ is the derivative in the normal direction, ω is the angular frequency, and ρ_f is the average density of the fluid.

By introducing a weak formulation with weighting function $\chi(\mathbf{x})$, the Helmholtz equation is transformed as follows [92]:

$$\int_{\Omega} \chi(\mathbf{x}) \Big(\Delta p(\mathbf{x}) + k^2 p(\mathbf{x}) \Big) d\Omega(\mathbf{x})$$

$$= \int_{\Gamma} \chi(\mathbf{x}) i \omega \rho_f u_f(\mathbf{x}) d\Gamma(\mathbf{x}) + \int_{\Omega} \Big(\nabla \chi(\mathbf{x}) \nabla p(\mathbf{x}) - k^2 \chi(\mathbf{x}) p(\mathbf{x}) \Big) d\Omega(\mathbf{x})$$

$$= 0$$
(17)

where Ω and Γ are the domain and boundary respectively. The physical quantities (acoustic pressure and particle velocity) in a discretized domain are respectively given by [92]:

$$p(\mathbf{x}) = \sum_{n=1}^{N} \Phi_n(\mathbf{x}) p_n$$

$$u_f(\mathbf{x}) = \sum_{n=1}^{N} \Phi_n(\mathbf{x}) u_n$$
(18)

where p_n and u_n correspond to the discrete acoustic pressure and fluid particle velocity at point **x**. $\Phi_n(\mathbf{x})$ is a basis function. Substituting Equation (18) into Equation (17) and considering source terms yields [92]:

$$\left(\mathbf{K} - \mathbf{i}k\mathbf{C} - k^2\mathbf{M}\right)\mathbf{p} = \mathbf{f}$$
(19)

where **K**, **C**, and **M** are the stiffness, damping and mass matrices of the acoustic domain, respectively. The excitation vector **f** represents the source and the pressure vector, **p** represents the sound pressure values at the nodal locations in the acoustic domain.

3. Results

In this section, we present results from the application of FEM as well as various formulae regarding the acoustic behavior of noise barriers. Initially, the results of FEM for sound pressure levels and acoustic pressures are shown in the whole domain in cases with and without a barrier for different frequencies. The main part of the section presents FEM and various formulae comparison of insertion loss for various source and receiver positions in the shadow zone, near the shadow border, and near the barrier.

3.1. Sound Pressure Levels and Acoustic Pressures of the Domain via FEM

Acoustic pressures and sound pressure levels (SPL's) were calculated via FEM. In Figures 3 and 4, the acoustic pressures and SPL's in the whole domain are presented for frequencies of 20 Hz, 100 Hz, 300 Hz, and 500 Hz respectively with and without the presence of a sound barrier. The effect of diffraction is evident in the shadow zone. Also, in the illuminated zone the interaction between the

wave from the source and the reflected wave from the noise barrier can be seen. Finally, in Figure 4 in particular the effect of PML's is apparent.

3.2. Calculation of Insertion Loss via FEM and Various Formulae

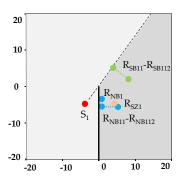
The insertion loss calculated via FEM and various formulae is presented and compared for various source and receiver positions. For the calculations, four different source positions were used:

- S₁: source in medium distance from the barrier (4 m)
- S₂: source in long distance from the barrier (16 m)
- S₃: source in short distance from the barrier (0.2 m)
- S₄: source above the barrier (6 m)

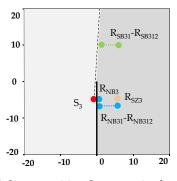
For each source position, insertion loss was investigated for the following receiver positions:

- R_{SZ}: receiver in the shadow zone
- R_{SB}: receiver near the shadow border
- R_{NB}: receiver near the barrier

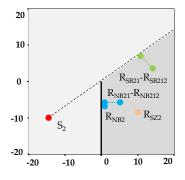
Source and receiver positions are presented in Figure 5, while the exact positions are given in Appendix A (Table A1).



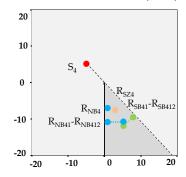
(a) Souce position S1: source in medium distance from the barrier (4 m)



(c) Souce position S₃: source in short distance from the barrier (0.2 m)



(**b**) Souce position S₂: source in long distance from the barrier (16 m)



(d) Souce position S4: source above the barrier (6 m)

Figure 5. Source and receiver positions for calculation of insertion loss via FEM and various formulae (source (S): red, receiver in the shadow zone (R_{SZ}): orange, receiver near shadow border (R_{SB}): green, receiver near barrier (R_{NB}): blue). The exact positions for each source and receiver are presented in the Appendix A (Table A1).

3.2.1. Receiver in the Shadow Zone

A comparison of insertion loss results between FEM and various formulae for the four source positions and receiver positions in the shadow zone is presented in Figure 6. The range of the scale on

the y axis has been kept the same in each case (20 dB), so that there can be a direct comparison of the results and differences can be better discerned.

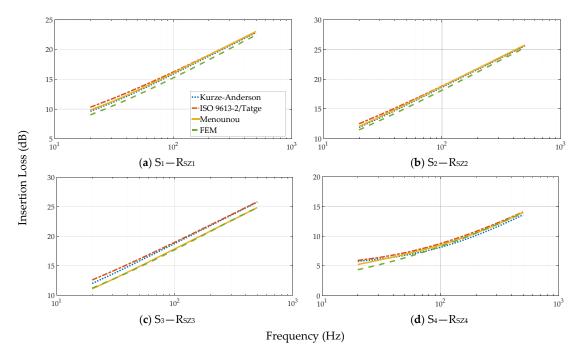


Figure 6. Comparison of insertion loss results between FEM and various formulae for various source and receiver positions in the shadow zone.

3.2.2. Receiver near Barrier (0.1 m)

A comparison of insertion loss results between FEM and common formulae for the four source positions and receiver positions near the barrier (0.1 m) is presented in Figure 7. The range of the scale on the y axis has been kept the same in each case (30 dB), so that there can be a direct comparison of the results and differences can be better discerned.

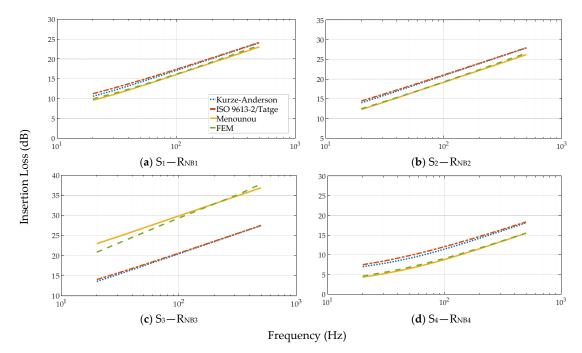


Figure 7. Comparison of calculation of insertion loss between FEM and various formulae for various source and receiver positions near the barrier inside the shadow zone.

3.2.3. Receiver in Increasing Distance from the Barrier (0.1 m–5 m)

A comparison of insertion loss results between FEM and various formulae for the four source positions and receiver positions near the barrier (0.1 m–5 m) is presented in Figure 8. The range of the scale on the y axis has been kept the same in each case (8 dB), so that there can be a direct comparison of the results and differences can be better discerned.

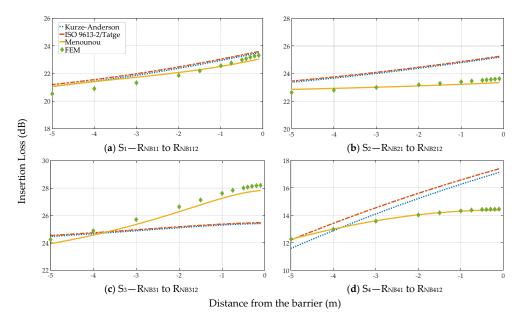


Figure 8. Comparison of calculation of insertion loss between FEM and various formulae for various source and receiver positions near the barrier inside the shadow zone (300 Hz).

3.2.4. Receiver near the Shadow Border (0.1 m)

A comparison of insertion loss results between FEM and common formulae for the four source positions and receiver positions near the shadow border (0.1 m) is presented in Figure 9. The range of the scale on the y axis has been kept the same in each case (6 dB), so that there can be a direct comparison of the results and differences can be better discerned.

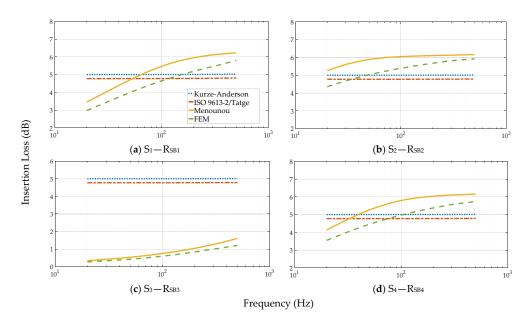


Figure 9. Comparison of calculation of insertion loss between FEM and various formulae for various source and receiver positions in the shadow border.

3.2.5. Receiver in Increasing Distance from the Shadow Border (0.1 m-5 m)

A comparison of insertion loss results between FEM and various formulae for the four source positions and receiver positions near the shadow border (0.1 m–5 m) is presented in Figure 10. The range of the scale on the y axis has been kept the same in each case (20 dB), so that there can be a direct comparison of the results and differences can be better discerned.

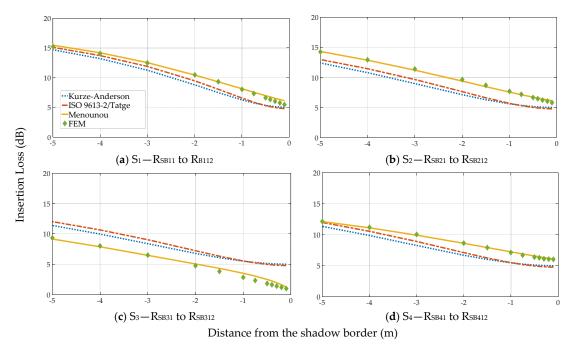


Figure 10. Comparison of calculation of insertion loss between FEM and various formulae for various source and receiver positions near the barrier inside the shadow zone (300 Hz).

4. Discussion

The topics of this section are:

- FEM and various formulae insertion loss calculations.
- Future work and further applications of FEM for noise barriers and microscale urban acoustic modeling.

4.1. FEM and Various Formulae Insertion Loss Calculations

In the previous chapter, FEM modeling for the whole domain as well as a comparison of insertion loss calculations between FEM and various formulae for different source and receiver positions was studied.

FEM modeling in the whole domain for the acoustic pressure and the sound pressure levels is presented in Figures 3 and 4. The effect of the noise barrier is evident in every area around the barrier. In particular, an interaction between the source and reflections from the noise barrier can be observed in the illuminated zone, which has a different form for each frequency. The significance of this lies in the fact that FEM allows the calculation of the sound field in the whole domain (and in the illuminated zone) where common formulae cannot apply. This is of great importance for the issue of microscale urban acoustic modeling, as the calculation of the acoustic field is important for the whole domain and is going to be discussed in the following chapter.

The comparison of insertion loss calculations between FEM and various formulae for different source and receiver positions that was presented in the results can be categorized into the following cases: receiver in the shadow zone, receiver near the barrier and receiver near the shadow border.

In the case where the receiver is in the shadow zone (Figure 6), results from FEM and all various formulae have small differences for every source position (source in medium, long, short distance and above the barrier). Especially the differences between FEM and Menounou's formula are less than 1 dB. We must also note that in the case where the source is close to the barrier (Figure 6c), the results of FEM and Menounou's formula are almost identical and differ from Kurze–Anderson and Tatge/ISO 9613-2 results. This is also evident in all the cases where the source is near the barrier for all the receiver positions (Figures 7c, 8c, 9c and 10c). A possible explanation for the above result, is that since some of the formulae have emerged from semi-empirical results mainly in the shadow zone (Maekawa chart and thereafter Kurze–Anderson, Tatge/ISO 9613-2), their validity applies mainly for this area.

In the case where the receiver is near the barrier (Figures 7 and 8), the results from FEM and Menounou's formula are similar with differences less than 1 dB for almost every source position and frequency (slightly larger difference exists in the low frequency range of Figure 7c). Also, Kurze–Anderson and Tatge/ISO 9613-2 formulae follow the same pattern and present similar results. The differences between the two (Kurze-Anderson, Tatge/ISO 9613-2 and FEM, Menounou formulae) are significant especially in the case where the source is close to the barrier (about 10 dB for the whole frequency range (Figure 7c)). These results are in line with comparison of the analytical solution (McDonald solution [34]) and Kurze–Anderson formula presented in [47], where similar results were found (in the case of source and receiver close to the barrier). This is particularly important as it shows the agreement of FEM with the Menounou's formula in the case where the receiver is near the barrier, which in turn is in agreement with the analytical solution (McDonald solution). The same trend exists at close distances (0.1 m–5 m) from the barrier (Figure 8), where FEM and Menounou's formula seem to follow the same pattern and have similar results. Again, a possible explanation for the differences observed, is that some of the formulae have arisen from semi-empirical data mainly in the shadow zone (Maekawa chart and thereafter Kurze-Anderson, Tatge/ISO 9613-2), therefore, their validity near the noise barrier is not as good.

In the case where the receiver is near the shadow border (Figures 9 and 10), once more FEM and Menounou's formula have similar patterns and results with differences less than 1 dB. The results of Kurze–Anderson and Tatge/ISO 9613-2 formulae close to the shadow border (0.1 m) are about 5 dB in the whole frequency range for every source position. The differences between the two (Kurze–Anderson, Tatge/ISO 9613-2 and FEM, Menounou formulae) are again significant, especially in the case where the source is close to the barrier (about 5 dB for the whole frequency range (Figure 7c)). As also stated in the previous paragraph, these results are again in line with the comparison of the analytical solution (McDonald solution [34]) and Kurze–Anderson formula presented in [47], where similar results were found in the case of the receiver close to the shadow border. This result is important as it shows the agreement of FEM with Menounou's formula in the case where the receiver is near the shadow border, which in turn is in agreement with the analytical solution (McDonald solution). The same can be observed at close distances (0.1 m–5 m) from the shadow border (Figure 10), where FEM and Menounou's formula seem to follow the same pattern and have similar results.

In summary, there is satisfactory agreement (less than 1 dB difference in every case) of FEM and Menounou's formula which in turn agrees with the analytical solution (McDonald solution). Especially in the cases where the receiver is near the barrier or the shadow border, FEM, and Menounou's formula follow the same pattern and have similar results, unlike Kurze–Anderson and Tatge/ISO 9613-2, which show large deviations. In this research a large number of source and receiver positions were investigated, resulting in a wide range of applicability according to the Fresnel number. The minimum Fresnel number was 1.937×10^{-5} (Source: S3, Receiver: R_{SB31} , Frequency: 20 Hz), while the maximum was 18.374 (Source: S2, Receiver: R_{SZ2} , Frequency: 500 Hz). Previous research has indeed shown that the Menounou's formula is very close in each case to the analytical solution. There are differences with the other formulae when the receiver is near the barrier and near the shadow border. The differences between the FEM/Menounou and the other formulae, have arisen probably because these formulae have been formed from semi-empirical data (e.g., Maekawa chart and thereafter Kurze–Anderson,

Tatge/ISO 9613-2) in which the cases close to the barrier and near the shadow border have not been properly taken into account.

It should also be noted that FEM has advantages over Menounou's formula for practical applications. Menounou's formula is essentially a simple and accurate formula that provides very good results for the calculation of insertion loss in any position similar to the analytical solution for a semi-infinite noise barrier in a two-dimensional space. Therefore, it is limited to two-dimensional space and simple forms of sound barriers. The advantages of FEM are that it can be directly applied to three-dimensional space and to complex forms of noise barriers.

The results support the idea of the accuracy of FEM for the calculation of insertion loss of noise barriers. This result has further strengthened our confidence that FEM is suitable for modeling the acoustic behavior of noise barriers and its use is likely to have many applications in the future. In other words, the analytical and numerical models are very much in agreement. Their difference with the standard models is especially obvious in this case where the receiver is near the barrier or the shadow border, which in turn may have practical applications which will be discussed in the next section.

4.2. Future Work and Further Applications of FEM for Noise Barriers and Microscale Urban Acoustic Modeling

In terms of direction for future work we believe that this study provides a blueprint that can be directly utilized for modeling the acoustic behavior of noise barriers in a variety of applications. Further studies with the use of FEM could be undertaken for modeling of barriers with various shapes and configurations (e.g., in a tilt angle, galleried and cantilevered barriers etc.), for barriers that employ materials that absorb or diffuse sound, with layered materials [50], or employing atmospheric and ground absorption for a more comprehensive approach.

In terms of direction for further applications, our approach would lend itself well for use for noise barrier modeling tailored to real life problems. A common issue that has been reported regarding noise barriers is their visual impact [93], while significant positive correlations were found between aesthetic preference and environmental impact reduction, implying the importance of barrier aesthetics [94]. For barrier design 'the best results are likely to be achieved through the co-ordinated services of qualified acousticians, civil and structural engineers, landscape architects and architects' [17]. Due to the accuracy of FEM for modeling noise barrier, as well as its widespread use that can easily incorporate Computer-Aided Designs (CAD) (e.g., from landscape architects and architects), it could possibly applied in practice for the creation of effective and aesthetic designs that can be successfully integrated into the landscape.

A further application of FEM, utilizing similar methodology presented in this study, could possibly be for urban microscale acoustic modeling (microscale refers to small and medium-scale urban areas such as a street or a square [95]). FEM has some advantages over practices used (e.g., noise mapping software) and possibly over other wave based methods which justify further investigation for its practical application. The advantages are:

- Accuracy
- Availability
- Low cost

In real life problems, expensive noise-mapping software is used which is based on a series of algorithms specified in various standards (e.g., ISO 9613-2 [30]). A number of software packages have been developed were terms are provided for the modeling of various physical effects (e.g., screening by obstacles). A drawback associated with this approach is the neglection of the wave nature of sound, where on wave based methods (such as FEM) all wave phenomena are included in the theoretical background. Also, as presented in this study, FEM seems to provide superior results than ISO 9613-2 [30] especially in cases where the receiver or/and the source is near the barrier. This is also likely to provide better results in cases such as e.g., balconies, facades.

In terms of availability and low cost, FEM is probably the most widespread numerical method. Reliable open source FEM software exists (e.g., [96]) while also FEM is integrated in many CAD software, hence noise barrier or urban microscale acoustic modeling could possibly be incorporated in these programs, reduce application cost and spread the usage.

In general, advantages of FEM far outweigh the disadvantages which are mainly related to the computational cost. New techniques are applied in practice in order to make the computations more feasible. Utilization of Graphics Processing Unit (GPU) [97,98] has shown some remarkable results that are likely to further be improved in the future. Another way to deal with the computational issue is to use a hybrid approach in which the FEM will be applied in the low frequency range while for the higher frequencies more standard approaches will be used. FEM can also be applied in the time domain [99] for the extraction of a variety of acoustic parameters, can incorporate the effect of ground (e.g., by assigning acoustic impedance characteristics to the ground surface) [100], can model successfully the meteorological conditions [101] and since it requires discretization of the whole domain it can model an inhomogeneous atmosphere incorporating the effects of refraction [102]. A discussion of wave based methods used for microscale urban acoustic modeling can be found in [103].

5. Conclusions

We assessed the accuracy and applicability of FEM for the calculation of insertion loss of noise barriers for two dimensional acoustic radiation problems. Results obtained with FEM were compared with various formulae and especially the Menounou formula which comply well with the analytic solution. Different source and receiver positions were tested in the shadow zone, illuminated zone and in the shadow border. Particular attention was paid in the cases where the source and receiver are near the barrier and the receiver is in the shadow border, as it has been shown that results from the common Kurze–Anderson formula deviate from the analytical solution.

The findings of this study in the context of improving the urban acoustic environment support the idea that FEM can be used effectively for the accurate calculation of the insertion loss of noise barriers for various source and receiver positions and consists and excellent option for noise barrier modeling. The same scheme used in this research could be directly applied for modeling the behavior of noise barriers with various shapes and configurations and for barriers in 3D space. Our study provides practical steps that can be followed for easy implementation of FEM while strong point of our approach lies in the fact that commercial or even free software can be used. This could lead to noise barrier designs tailored to real life noise problems, thus improving the urban acoustic environment.

Although this study focuses on the implementation of FEM for noise barriers, the findings may well have a bearing on applying the method for microscale urban acoustic modeling. Although the biggest limitation lies in the computational cost, this will be less of a problem in the future while there is also the possibility of using the method in a hybrid approach for the low frequency range. This research leads to the further utilization of FEM in the context of microscale acoustic modeling, which we believe could be an important contribution as the efficiency and availability of the method can be applied in practice for the improvement of the urban environment.

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Abbreviations

The following abbreviations are used in this manuscript:

ABC	Absorbing Boundary Condition
BEM	Boundary Element Method
CAD	Computer-Aided Design
FDTD	Finite-Difference Time-Domain
FEM	Finite Element Method
GPU	Graphics Processing Unit
IL	Insertion Loss
PML	Perfectly Matched Layer
PSTD	Pseudo-Spectral Time-Domain
R _{NB}	Receiver Near the Barrier
R _{SB}	Receiver in the Shadow Border (near)
R _{SZ}	Receiver in the Shadow Zone
SPL	Sound Pressure Levels
WHO	World Health Organization

Appendix A

Table A1. Source and receiver positions for calculation of insertion loss via FEM and common formulae (correspond to positions shown in Figure 5).

Receiver Area	Distance d(m)	Source Positions (x,y)				
		$S_1(-4.00, -4.00)$	S ₂ (-16.00, -10.00)	S ₃ (-0.20, -5.00)	S ₄ (-6.00, 6.00)	
			Receiver Positions (x,y)			
Shadow zone		$R_{SZ1}(4.00, -4.00)$	R _{SZ2} (10.00, -9.00)	$R_{SZ3}(5.00, -4.00)$	R _{SZ4} (3.00, -8.00)	
Shadow border (0.10 m in the shadow zone)		R _{SB11} (4.07, 3.93)	R _{SB21} (12.05, 7.42)	R _{SB31} (0.50, 10.00)	R _{SB41} (8.93, -9.07)	
Near barrier		R _{NB1} (0.10, -3.00)	R _{NB2} (0.10, -8.00)	R _{NB3} (0.10, -5.00)	R _{NB4} (0.10, -7.00)	
	0.10	R _{SB11} (4.07, 3.93)	R _{SB21} (12.05, 7.42)	R _{SB31} (0.50, 10.00)	R _{SB41} (8.93, -9.07)	
	0.20	R _{SB12} (4.14, 3.86)	R _{SB22} (12.11, 7.33)	R _{SB32} (0.60, 9.99)	R _{SB42} (8.86, -9.14)	
	0.30	R _{SB13} (4.21, 3.79)	R _{SB23} (12.16, 7.25)	R _{SB33} (0.70, 9.99)	R _{SB43} (8.79, -9.21)	
	0.40	R _{SB14} (4.28, 3.71)	R _{SB24} (12.21, 7.16)	R _{SB34} (0.80, 9.98)	R _{SB44} (8.72, -9.28)	
	0.50	R _{SB15} (4.35, 3.65)	R _{SB25} (12.27, 7.08)	R _{SB35} (0.90, 9.98)	R _{SB45} (8.65, -9.35)	
Varying distance d from shadow border (in the shadow zone)	0.75	R _{SB16} (4.53, 3.47)	R _{SB26} (12.40, 6.86)	R _{SB36} (1.15, 9.97)	R _{SB46} (8.47, -9.53)	
varying distance d nom shadow border (in the shadow zone)	1.00	R _{SB17} (4.71, 3.29)	R _{SB27} (12.53, 6.65)	R _{SB37} (1.40, 9.96)	R _{SB47} (8.29, -9.71)	
	1.50	R _{SB18} (5.06, 2.94)	R _{SB28} (12.80, 6.23)	R _{SB38} (1.90, 9.94)	R _{SB48} (7.94, -10.06	
	2.00	R _{SB19} (5.41, 2.59)	R _{SB29} (13.06, 5.80)	R _{SB39} (2.40, 9.92)	R _{SB49} (7.59, -10.41	
	3.00	R _{SB110} (6.12, 1.88)	R _{SB210} (13.59, 4.96)	R _{SB310} (3.40, 9.88)	R _{SB410} (6.88, -11.12	
	4.00	R _{SB111} (6.83, 1.17)	R _{SB211} (14.12, 4.11)	R _{SB311} (4.40, 9.84)	R _{SB411} (6.17, -11.83	
	5.00	R _{SB112} (7.54, 0.46)	R _{SB212} (14.65, 3.26)	R _{SB312} (5.40, 9.80)	R _{SB412} (5.46, -12.54	
	0.10	R _{NB11} (0.10, -5.00)	R _{NB21} (0.10, -7.00)	R _{NB31} (0.10, -7.00)	R _{NB41} (0.10, -12.0	
	0.20	R _{NB12} (0.20, -5.00)	R _{NB22} (0.20, -7.00)	R _{NB32} (0.20, -7.00)	R _{NB42} (0.20, -12.0	
	0.30	R _{NB13} (0.30, -5.00)	R _{NB23} (0.30, -7.00)	R _{NB33} (0.30, -7.00)	R _{NB43} (0.30, -12.00	
	0.40	R _{NB14} (0.40, -5.00)	R _{NB24} (0.40, -7.00)	R _{NB34} (0.40, -7.00)	R _{NB44} (0.40, -12.00	
	0.50	R _{NB15} (0.50, -5.00)	R _{NB25} (0.50, -7.00)	R _{NB35} (0.50, -7.00)	R _{NB45} (0.50, -12.00	
Varying distance d near barrier (in the shadow zone)	0.75	R _{NB16} (0.75, -5.00)	R _{NB26} (0.75, -7.00)	R _{NB36} (0.75, -7.00)	R _{NB46} (0.75, -12.00	
varying distance d near barrier (in the shadow zone)	1.00	R _{NB17} (1.00, -5.00)	R _{NB27} (1.00, -7.00)	R _{NB37} (1.00, -7.00)	R _{NB47} (1.00, -12.00	
	1.50	R _{NB18} (1.50, -5.00)	R _{NB28} (1.50, -7.00)	R _{NB38} (1.50, -7.00)	R _{NB48} (1.50, -12.00	
	2.00	R _{NB19} (2.00, -5.00)	R _{NB29} (2.00, -7.00)	R _{NB39} (2.00, -7.00)	R _{NB49} (2.00, -12.00	
	3.00	R _{NB110} (3.00, -5.00)	R _{NB210} (3.00, -7.00)	R _{NB310} (3.00, -7.00)	R _{NB410} (3.00, -12.0	
	4.00	R _{NB111} (4.00, -5.00)	R _{NB211} (4.00, -7.00)	R _{NB311} (4.00, -7.00)	R _{NB411} (4.00, -12.0	
	5.00	R _{NB112} (5.00, -5.00)	R _{NB212} (5.00, -7.00)	R _{NB312} (5.00, -7.00)	R _{NB412} (5.00, -12.0	
Shadow border line equations		y = x	y = 0.625x	y = 25x	y = -x	
Perpendicular line equations (for varying distance from the shadow border points)		y = 8 - x	y = 26.7 - 8x/5	y = 1252/125 - x/25	y = -18 + x	
Points of intersection of the above lines (x,y)		(4.00, 4.00)	(12.00, 7.50)	(0.40, 10.00)	(9.00, -9.00)	

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